

$$B_s \longrightarrow \mu\mu$$

theory perspective

*Flip Tanedo*

Cornell  University

LEPP JC, 9 September 2011

# Grad Student Joint Meetings

PSB 470, 1:30-2pm Monday before the 'grown up' meeting  
<http://www.lepp.cornell.edu/~pt267/journal.html>

Next joint hep-ex/ph student meeting

**10 Oct**, Nic Eggert, *Status of Higgs Searches* (TBC)

Next week: Bibhushan Shakya, *Deconstructing the 5<sup>th</sup> Dimension*  
All LEPP students are welcome, hep-ph students are implored to attend

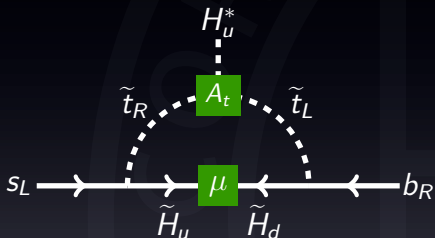
# Implications of $B_s \rightarrow \mu\mu$

- Significance of large  $\tan \beta$  in the MSSM
- Beyond MFV in the MSSM
- Relation to  $\Delta M_s$

# Two Higgs Doublet Models

**Type II 2HDM:** (e.g. **MSSM**) avoid tree-level FCNC by having  $H_u$  only talk to  $u_R$  and  $H_d$  only talk to  $d_R$  and  $e_R$ .

**But:** violated at loop-level by **SUSY** terms.



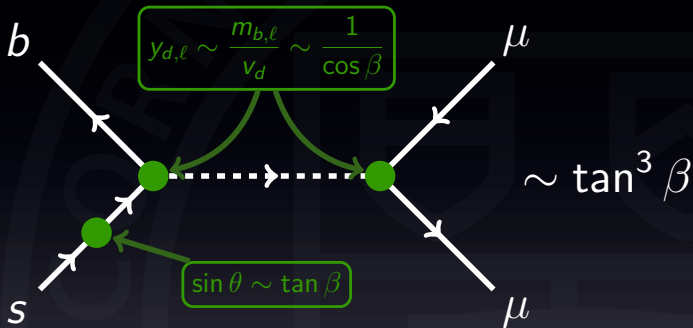
$$\begin{pmatrix} m_s & 0 \\ y_b \epsilon V_u & m_b \end{pmatrix}$$

$$\epsilon \sim y_t V_{ts} / (16\pi)^2$$

Loop-level  $s_L$ - $b_L$  mixing:

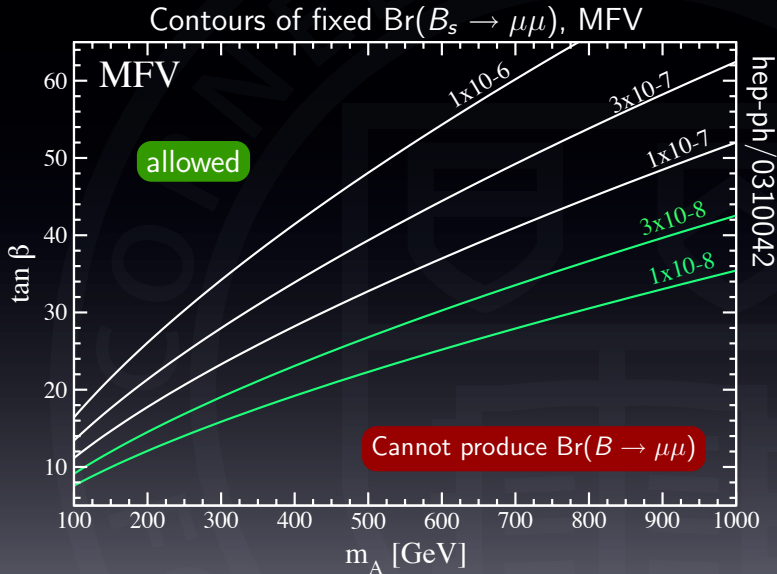
$$\sin \theta \sim \frac{y_b \epsilon V_u}{m_b} \sim \epsilon \tan \beta$$

# Enhancement by $\tan^6 \beta$ in SUSY



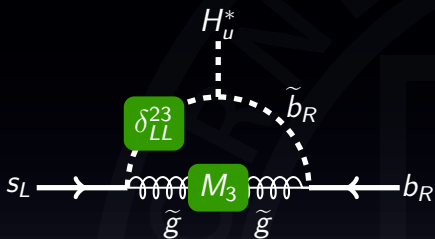
Other SUSY diagrams are negligible in the large  $\tan \beta$  limit.

# MFV bound



# Beyond MFV in the MSSM

Parameterize new flavor structure with squark mass insertions



$$\delta_{LL}^{ij} = \frac{(\Delta m_{LL}^2)_{ij}}{m_{LL}^2}$$

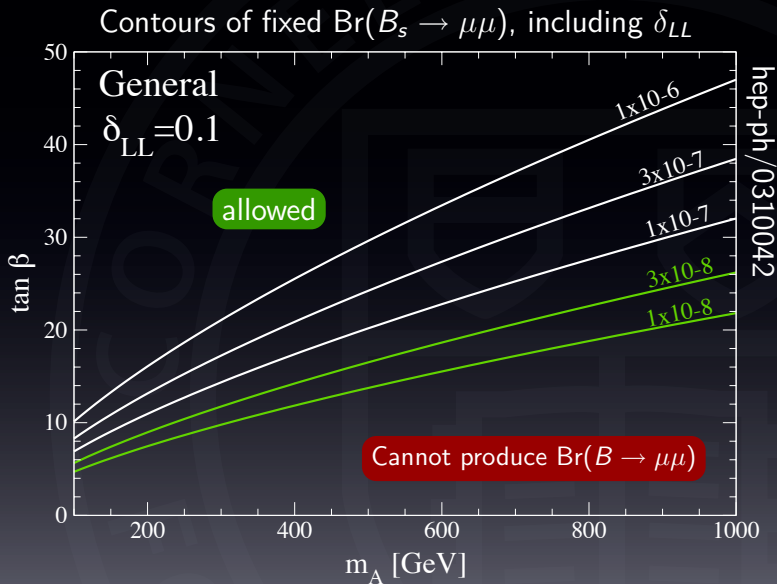
Also  $LL \rightarrow RR$

see, e.g. 0712.2074

**Danger:** constraints from  $B \rightarrow K^* \gamma$  and  $B \rightarrow \phi K_S$ , but those carry additional powers of  $(m_{LL})^{-2}$ .

**Remark:** Renormalization generates  $\delta_{LL}^{ij} \lesssim \mathcal{O}(V_{ts})$

# Beyond MFV bound





# Relation to $\Delta M_s$ MSSM

Another observable sensitive to  $\delta_{LL}^{23}$  is  $\Delta M_s$  in  $\bar{B}_s$ - $B_s$  mixing

$$\Delta M_s \approx \left| (\Delta M_s)_{\text{SM}} + \left( \frac{3.5 \text{ TeV}}{\tilde{m}} \right)^2 (\delta_{LL}^{23})^2 \right|$$

hep-ph/0112303, hep-ph/0206297

**But:**  $\left| \Delta M_s^{(\text{new})} / \Delta M_s^{(\text{SM})} \right| \lesssim 20\% \Rightarrow$  large  $\tilde{m}$  or small  $\delta_{LL}^{23}$ .

Suppresses  $B_s \rightarrow \mu\mu$  and tightens  $\tan\beta$  bound for given  $\text{Br}(B_s \rightarrow \mu\mu)$ .

**CP observables?**  $B_d \rightarrow \phi K_S$ ,  $\Delta\Gamma_s$ ,  $B_s \rightarrow J/\psi \phi$ , ...

# Relation to $\Delta M_s$ , MFV

**Minimal Flavor Violation:** NP (not necessarily SUSY) carries the same flavor structure as the SM:  $V_{CKM}$ .

hep-ph/0303060: Ratios can reduce uncertainties from  $f_{B_{d,s}}$

See also 1004.3982 for an alternate approach

$$\frac{\text{Br}(B_s \rightarrow \mu\mu)}{\text{Br}(B_d \rightarrow \mu\mu)} = \frac{(\text{non-perturbative})_s \tau(B_s) \Delta M_s}{(\text{non-perturbative})_d \tau(B_d) \Delta M_d}$$

- (non-pert.) is independent of  $f_B$  and RG invariant
- UV model-dependence cancels in the ratio

# Relation to $\Delta M_s$ , simple models

Alternate approach (0903.2830, 1102.0009)

$$\mathcal{H} \sim \sum_i g_i \bar{b} \gamma^\mu s V_\mu + g'_i \bar{l} \gamma^\mu l V_\mu + \dots$$

- $\Delta M_s$  operators expressed in terms of  $g_i g_j$
- $B \rightarrow \mu\mu$  operators expressed in terms of  $g_i g'_j$

Relations can reduce (sometimes eliminate) low-energy new physics parameters.

**Comment:** the  $\Delta M_{B_s}$  bounds are much more stringent than  $\Delta M_D$ , in which one could assume  $\Delta M_D$  came entirely from NP and then predict  $D \rightarrow \mu\mu$ .

# Remarks

- Photon penguin does not contribute (Ward identity)
- $s$ -channel scalar does not contribute ( $0^-$ )



# Relation to $\Delta M_s$ , simple models

Ex: **Flavor-changing  $Z'$**  (e.g. RS models)

$$\Delta M_s^{(Z')} = \frac{M_s f_{B_s}^2 B_{B_s} r_1(m_b, M_{Z'})}{3} \cdot \frac{g_{Z' sb}^2}{M_{Z'}^2}$$

$$\text{Br}(B_s \rightarrow \mu\mu) = \frac{G_F f_{B_s}^2 m_\mu^2 M_{B_s}}{16\sqrt{2}\pi\Gamma_{B_s}} \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} \cdot \frac{g_{Z' sb}^2}{M_{Z'}^2} \cdot \frac{M_Z^2}{M_{Z'}^2}$$

NP parameters completely fixed, end up with

$$\text{Br}(B_s \rightarrow \mu\mu) \leq 0.25 \cdot 10^{-9} \left( \frac{1 \text{ TeV}}{M_{Z'}} \right)^2$$

Similar story for **gauged family symmetry**,  $\text{Br}(B_s \rightarrow \mu\mu) \lesssim 10^{-12}$

# Relation to $\Delta M_s$ , simple models

## Ex: R-parity violating MSSM

$$W_{\mathcal{R}} = \lambda LLE^c + \lambda' LQD^c + \lambda'' U^c D^c D^c$$

Assume  $\lambda'' = 0$  for  $B$  conservation,  $\lambda, \lambda' \in \mathbb{R}$  for CP

Tree-level contributions from sneutrino exchange (dominated by  $\tilde{\nu}_k$ )

$$\Delta M_s^{(R)} \sim \sum_i \frac{\lambda'_{isd} \lambda'_{ids}}{M_{\tilde{\nu}_i}^2}$$

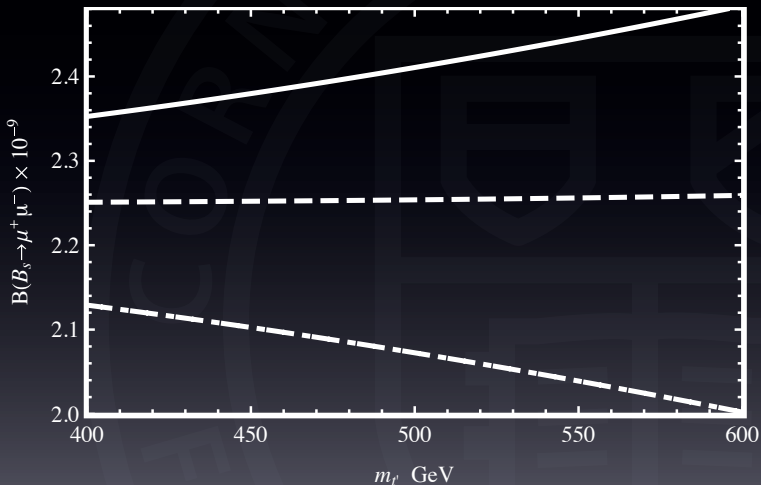
$$\text{Br}(B_s \rightarrow \mu\mu)^{(R)} \sim \left( \frac{\lambda_{k\mu\mu} \lambda'_{kbs}}{M_{\tilde{\nu}_k}^2} \right)$$

Sets upper bound on  $\lambda_{i\mu\mu} \lambda'_{ibs}$  in terms of  $M_{\tilde{\nu}_i}^2$ . If  $\lambda'_{ibs} = \lambda'_{isb}$ , then

$$\text{Br}(B_s \rightarrow \mu\mu)^{(R)} \sim \chi_{B_s}^{(R)} \frac{\lambda_{k\mu\mu}^2}{M_{\tilde{\nu}_k}^2}$$

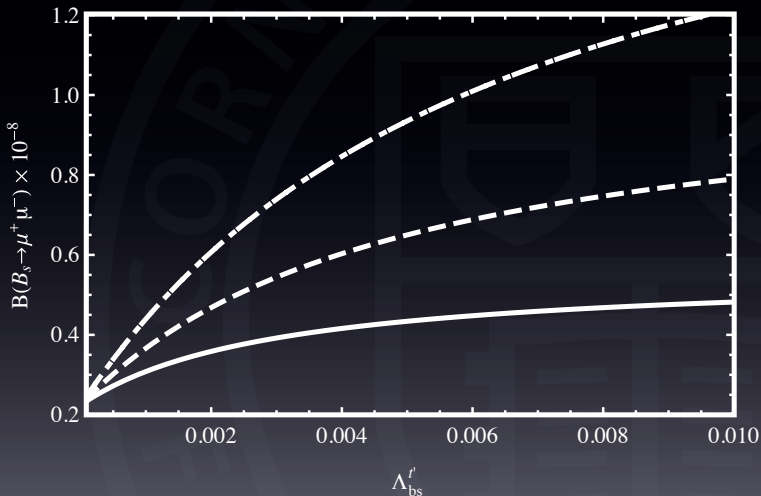
# Relation to $\Delta M_s$ , simple models

Ex: **Fourth generation** 1002.0595, 1102.0009



# Relation to $\Delta M_s$ , simple models

Ex: **Fourth generation** 1002.0595, 1102.0009





# Thanks

That's all I've got. . . discuss!

