

Active and Passive MHD Spectroscopy on Alcator C-Mod



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Motivation and Background



Unstable TAE's in C-Mod first observed in 1996 with current rise ICRF

- Low density ramping up with $I_p \rightarrow$ fast ion tail ~ 150 keV
- Upward and downward frequency chirping with $150 < f < 450$ kHz, $n \leq 3$
- Low or reversed shear q profiles maintained with ICRF

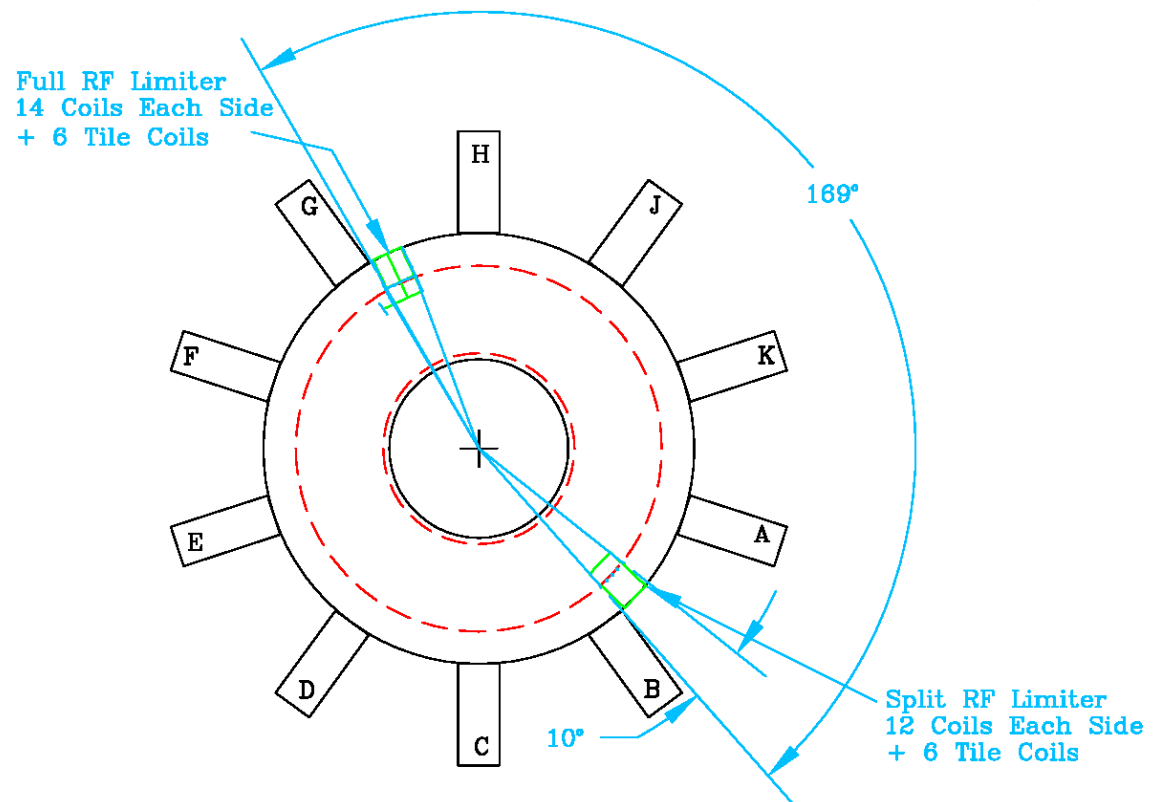
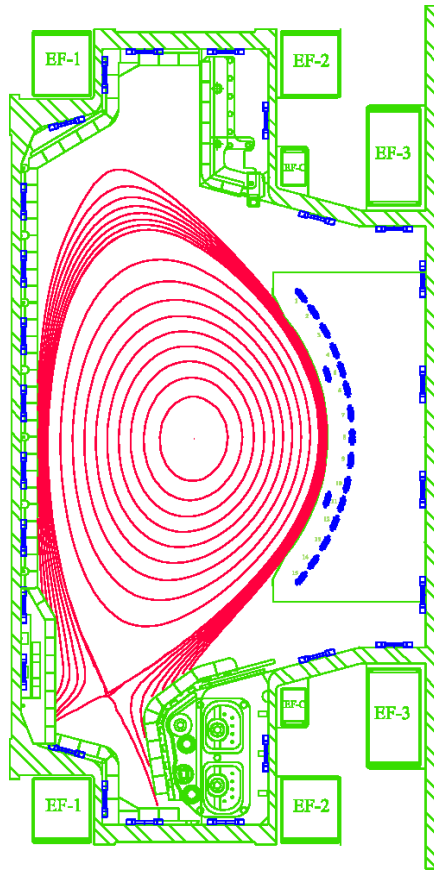
AE's also found in ICRF heated Enhanced D_α H-modes (EDA)

- High density $> 2 \times 10^{20} \text{ m}^{-3} \rightarrow$ weak fast ion tail ~ 50 keV
- Constant frequency in the range $600 < f < 900$ kHz, $n = 5 - 7$

Fasoli's Active MHD results on JET inspired C-Mod Active MHD

- Excite stable Alfvén eigenmodes at prescribed resonant frequencies
- To measure TAE damping rates at ITER toroidal fields and densities

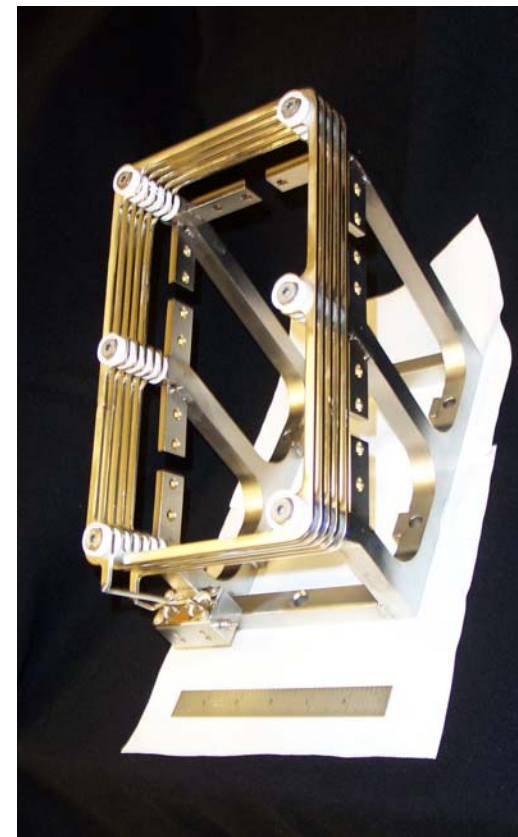
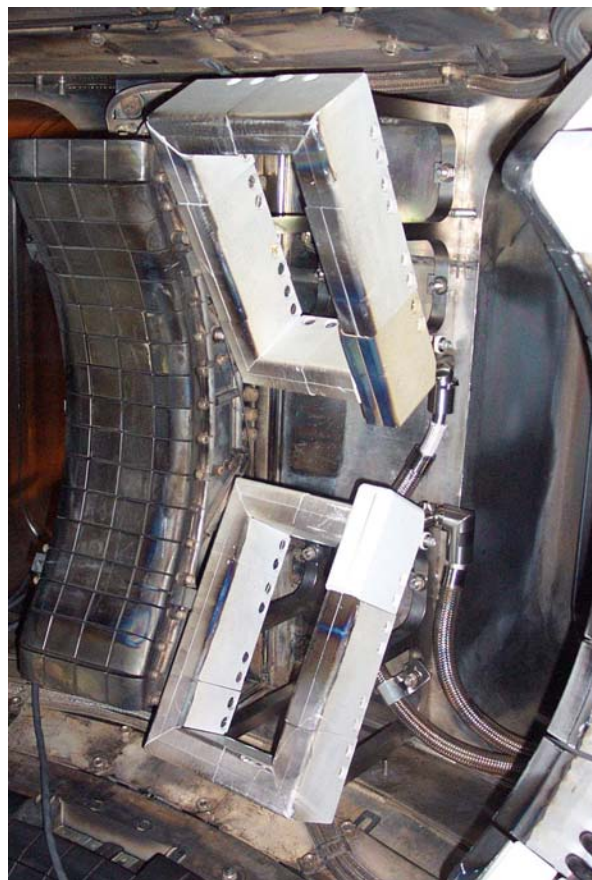
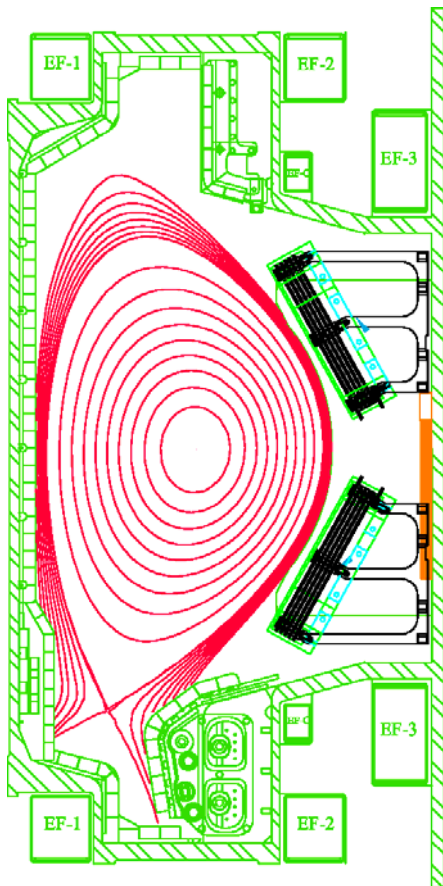
Experimental Setup – Pick-up Coils



Outboard Limiter Coils Toroidal View

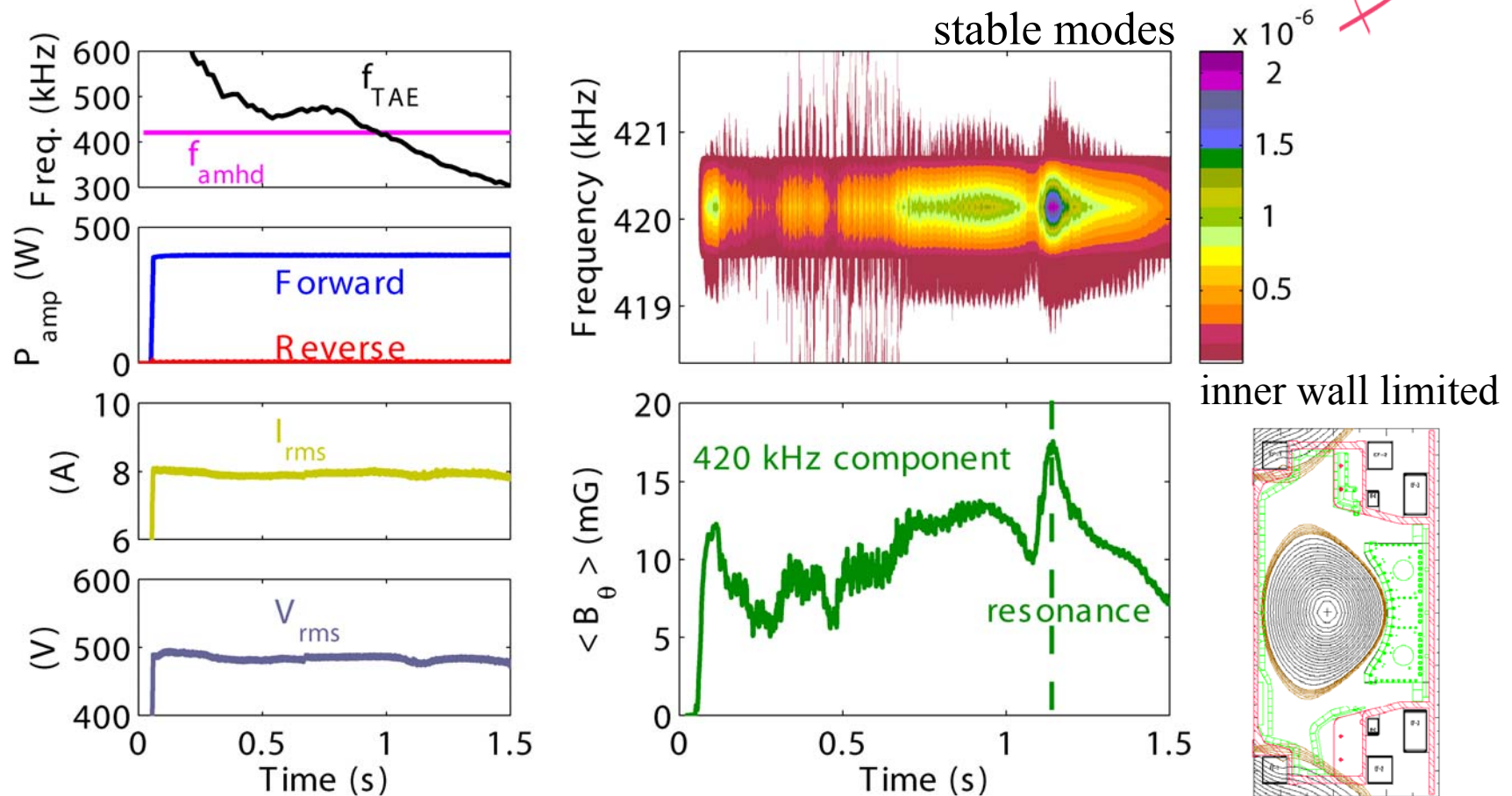
- 65 poloidal field pick-up coils in poloidal and toroidal arrays
- Can measure $m < 14$ and $n < 75$, sampling between 1 – 2.5 MHz

Experimental Setup – Active MHD Antennas



Presently 2 antennas above and below the outboard midplane
Previous amplifier drives ~ 12 A producing $\tilde{B}_r \sim 0.5$ G at $q=1.5$
 $1 \text{ kHz} < f < 1 \text{ MHz}$, high toroidal spectrum $1 < n < 20$ FWHM

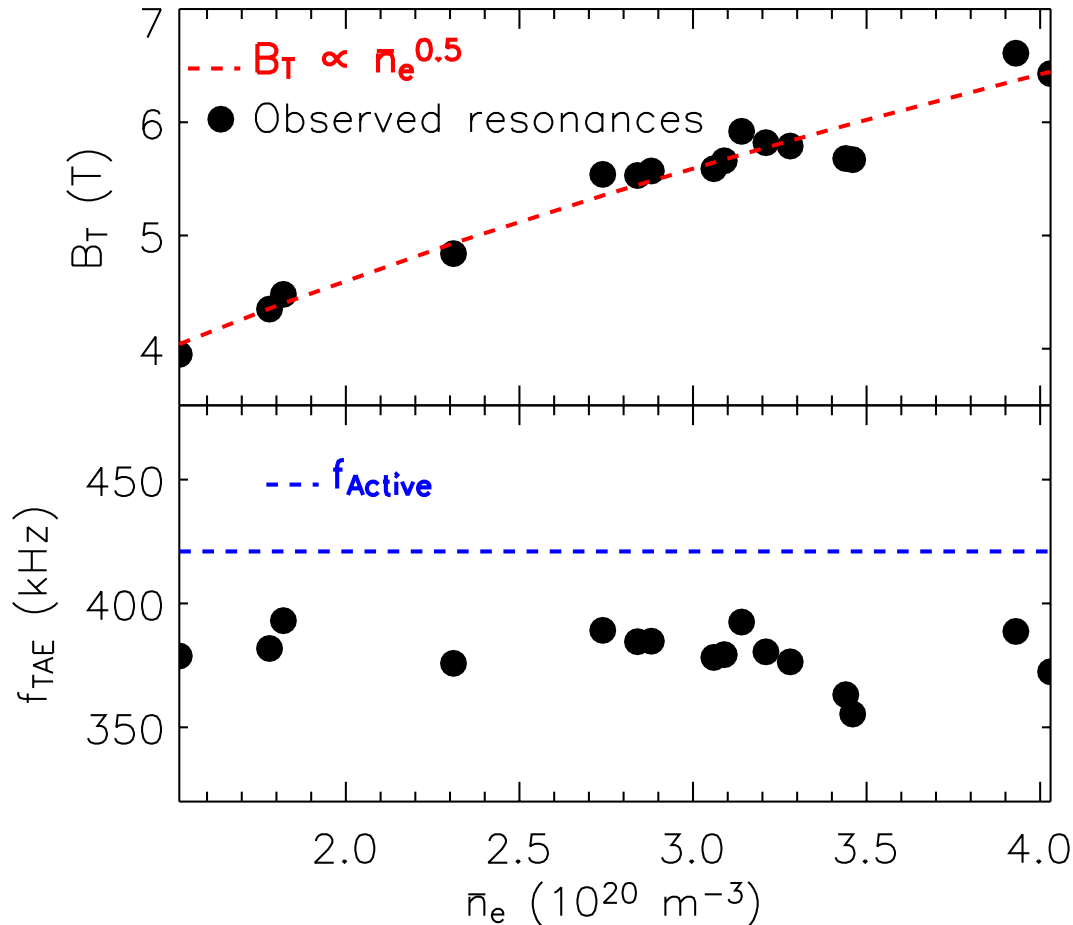
Active MHD Spectroscopy at Constant Frequency Alcator C-Mod



➤ Initial experiments at constant excitation frequency $f_{\text{amhd}} \sim 420$ kHz

➤ Ramping B_T makes f_{TAE} cross f_{amhd} at observed resonance condition

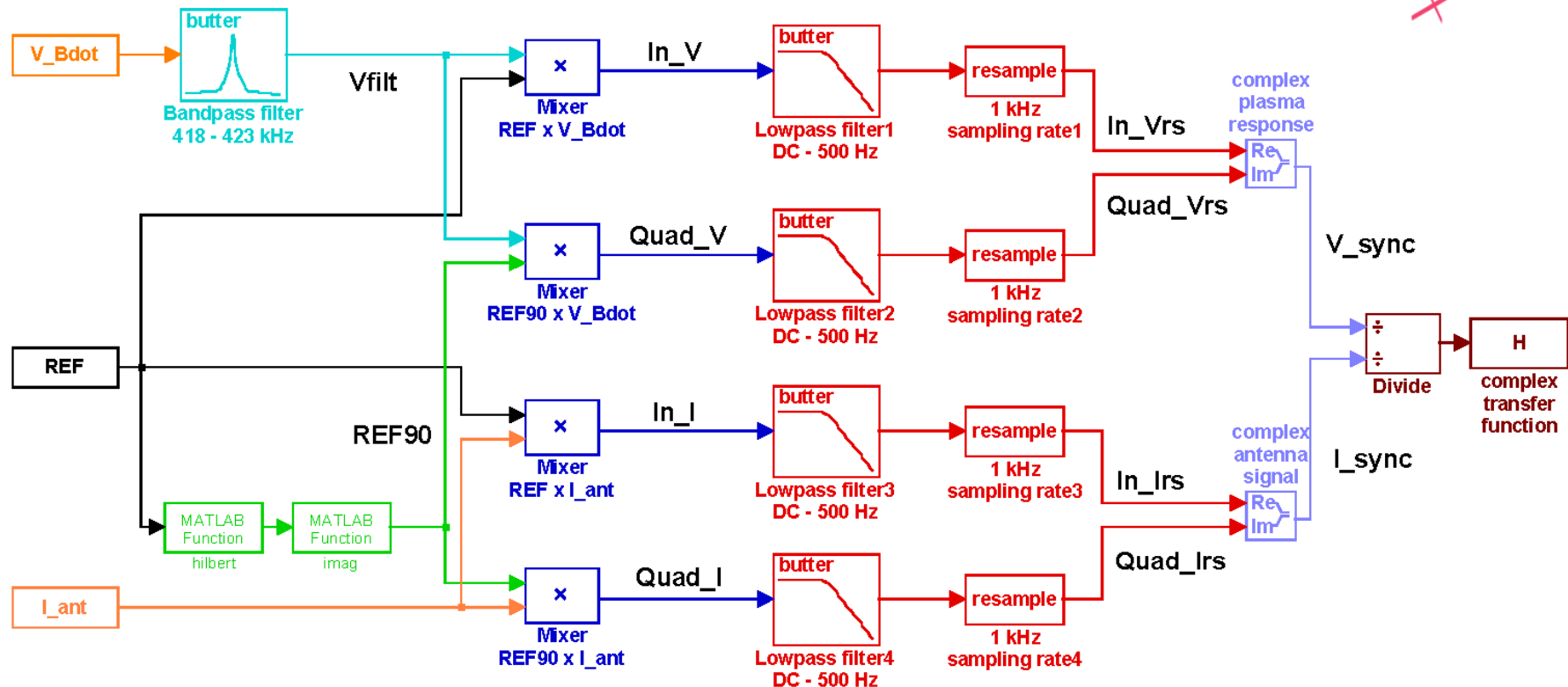
Observed Resonances agree with TAE Frequency Alcator C-Mod



- Ramping B_T from 6 – 4 T
- Shot-to-shot density scan
- Constant $f_{Active} = 420 \text{ kHz}$
- $B_T \propto n_e^{1/2}$ at resonances
- Observed resonant frequencies fall within the TAE gap 10 – 15% above the center of the gap at $q=1.5$

$$\omega_{TAE} = \frac{v_A}{2qR} \propto \frac{B_T / n_e^{1/2}}{2qR}$$

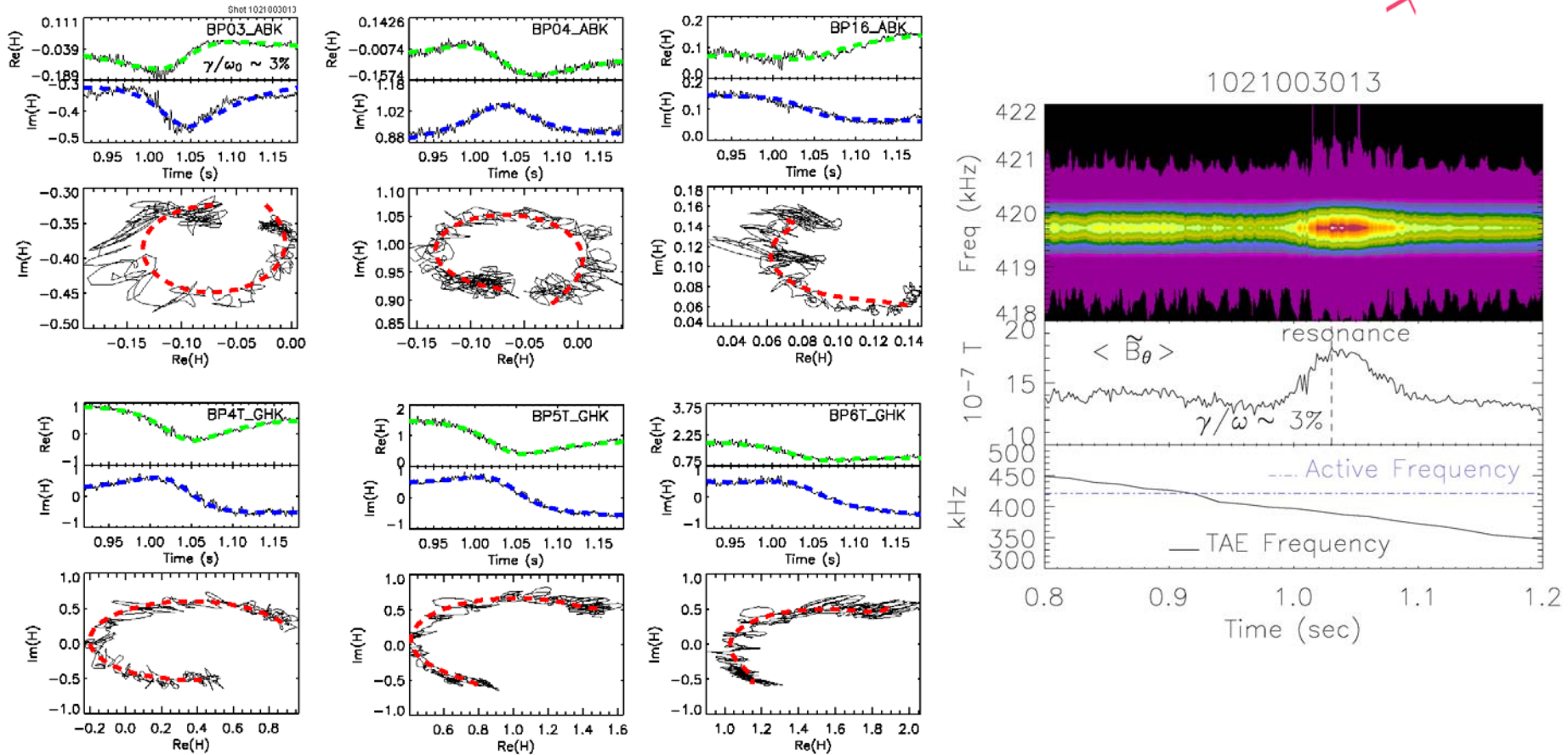
Software Synchronous Detection Algorithm



- Pick-up coils synchronously detected in software with Active MHD antenna current to calculate the complex transfer function

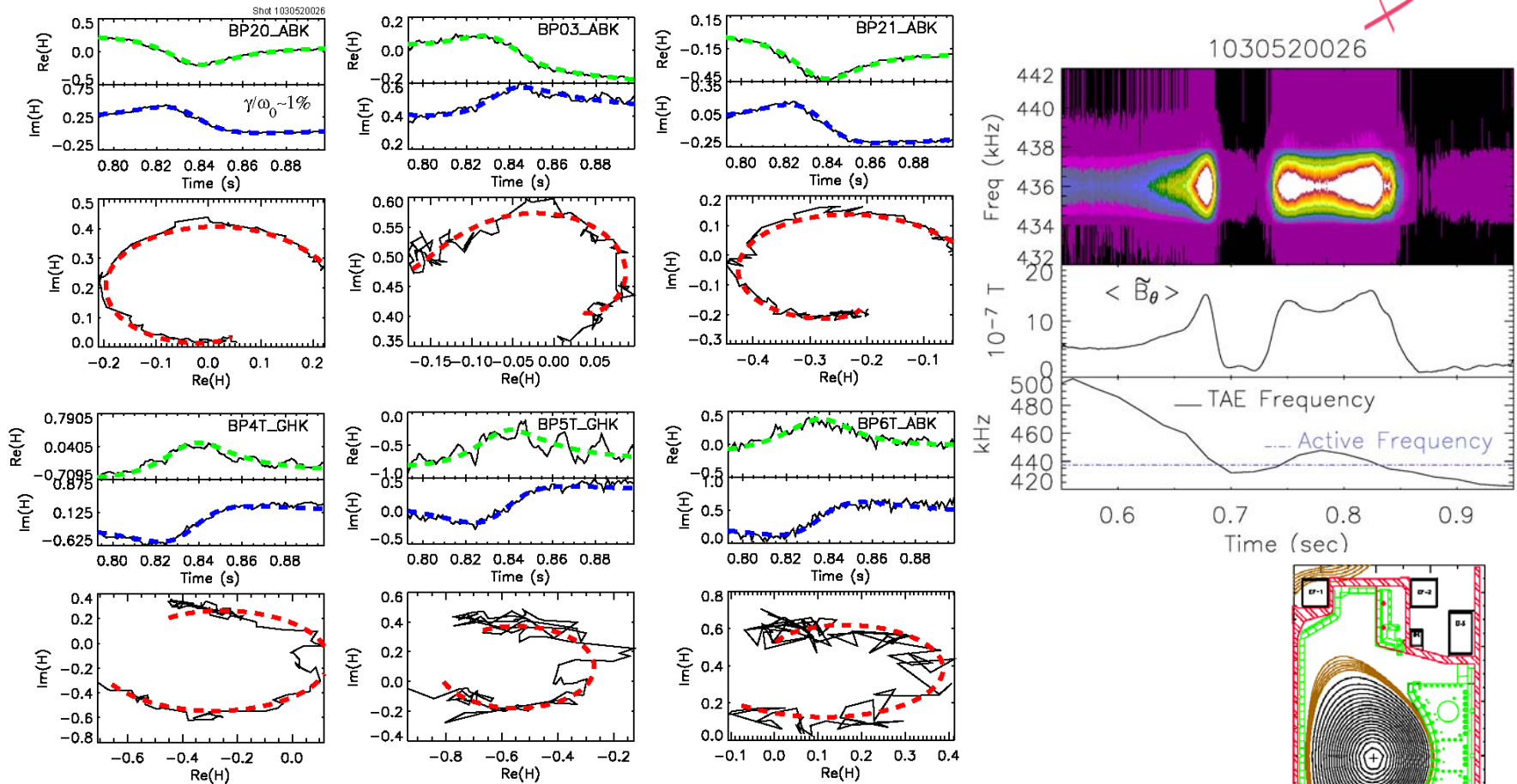
$$H(\omega, x) = \frac{V_{sync}}{I_{sync}} = \frac{1}{2} \left[\frac{r(x)}{i\omega - p} + \frac{r^*(x)}{i\omega - p^*} \right] + D(\omega, x) = \frac{B(\omega, x)}{A(\omega)}$$

Synchronous Detection with Multiple Coils



- Multiple pick-up coils synchronously detect an active TAE resonance in an inner wall limited plasma. Best fit gives $\gamma/\omega \sim 3\%$ and $n=4$.

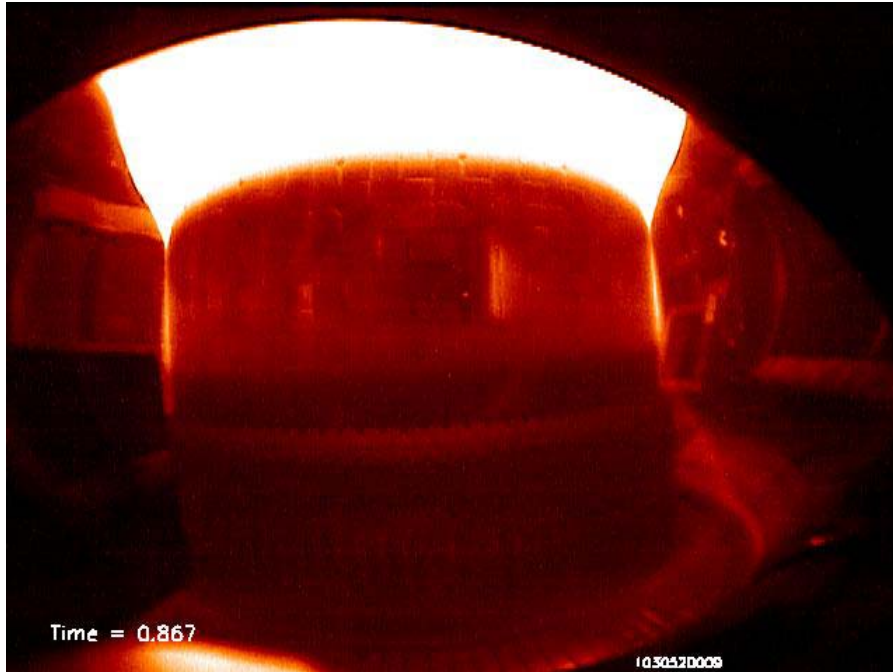
Active TAE Resonances in Diverted Plasmas



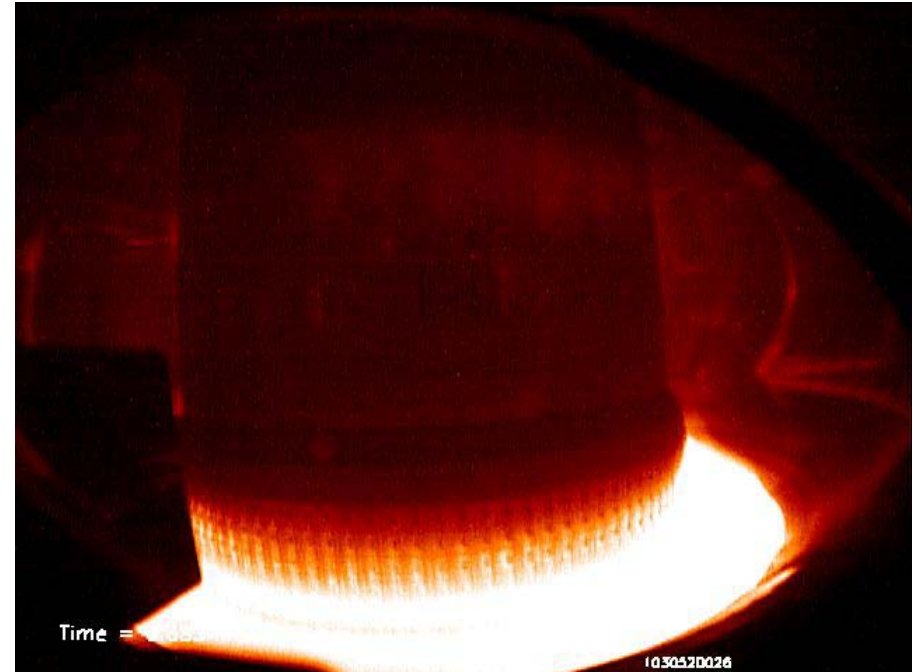
- Three TAE resonances as f_{TAE} crosses the active frequency in a diverted plasma with outer gap < 2.5 mm

Limited vs Diverted Plasma Outer Gap Scan

inner wall limited

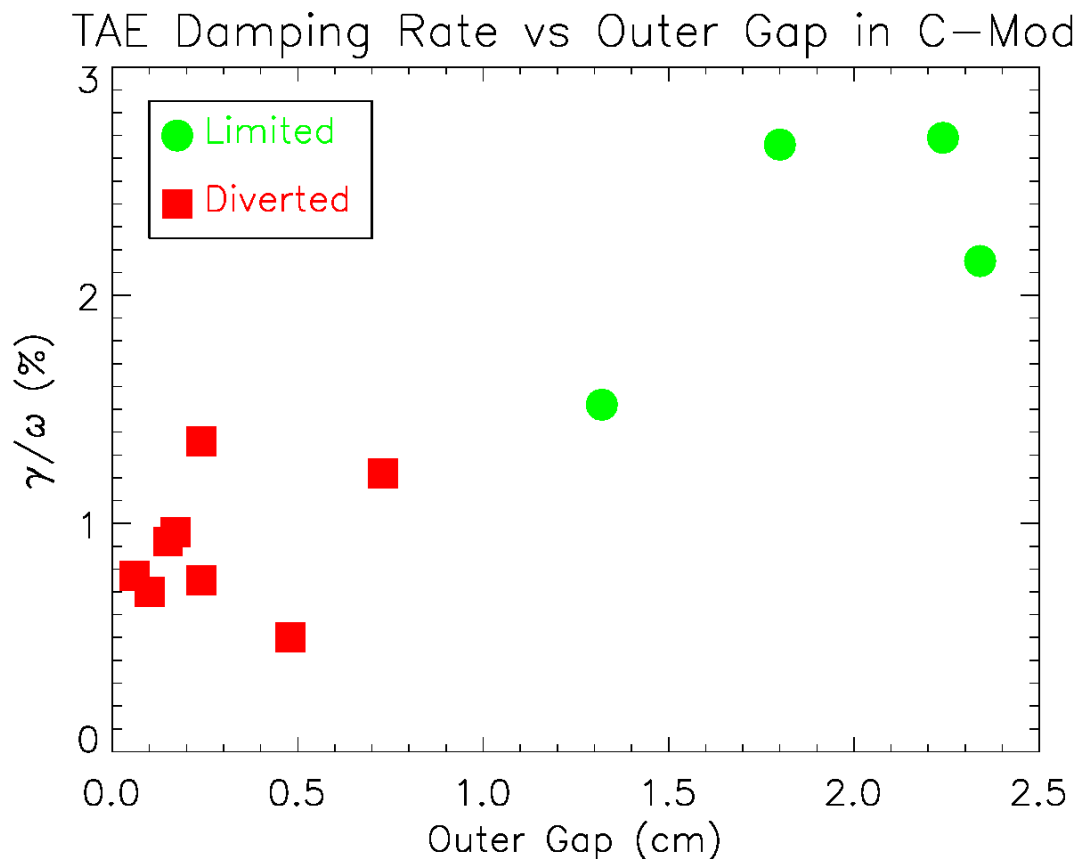


diverted with < 1 mm outer gap



- Even with < 1 mm outer gap the lower single null diverted plasma remains clearly diverted with no interaction on the inner or outer walls compared to a strong plasma interaction with inner wall limited plasma

Limited vs Diverted Plasma Outer Gap Scan

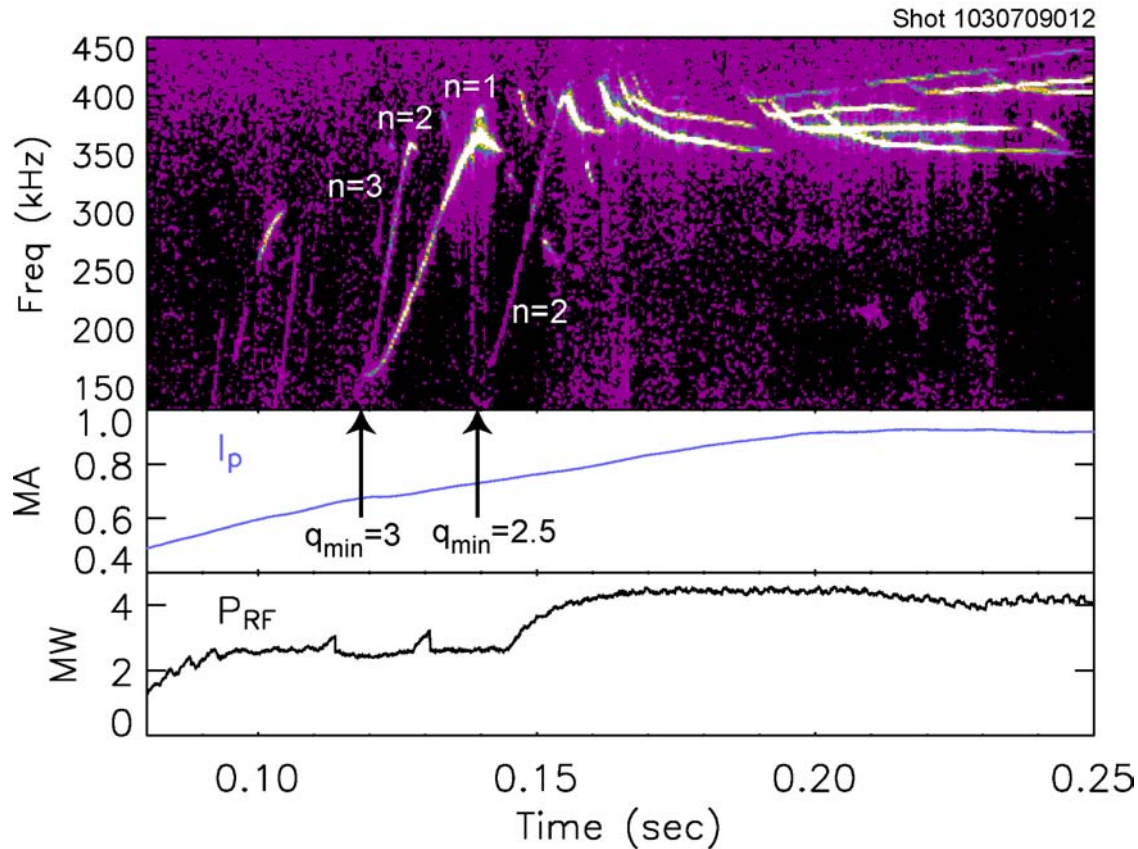


Active TAE resonances were only observed

- with moderate outer gaps in inner wall limited plasmas or
- with small outer gaps in diverted plasmas

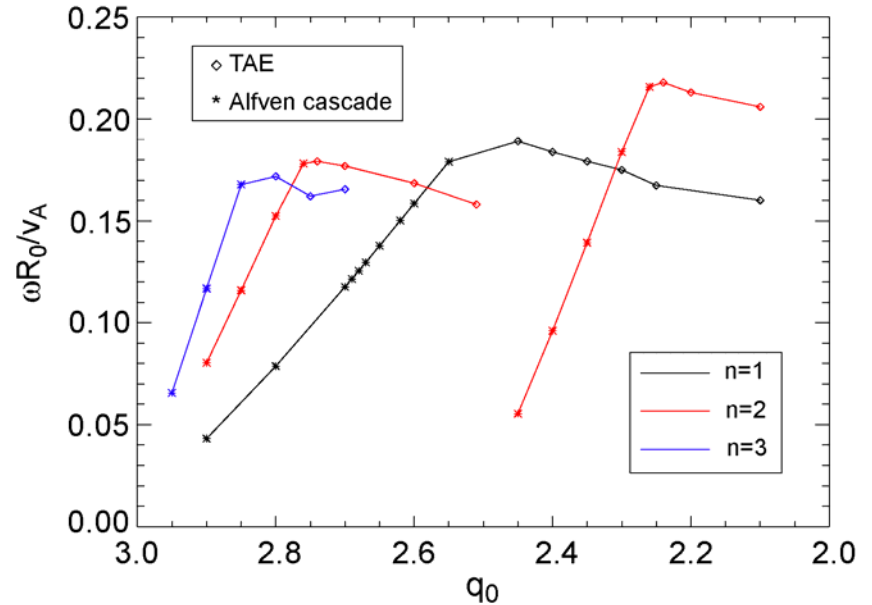
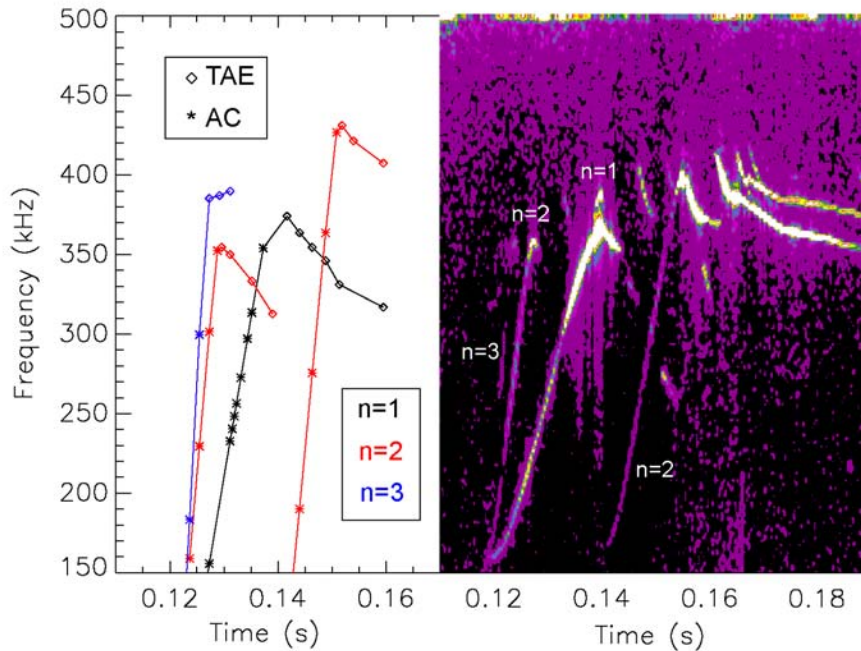
Damping rates are in the same range as those found in JET limited plasmas

Alfvén Cascades in the Current Rise



- Rapidly chirping Alfvén Cascades in the current rise with strong ICRF heating at low density indicate a reversed shear q profile and determine the minimum q value at the minimum mode frequency

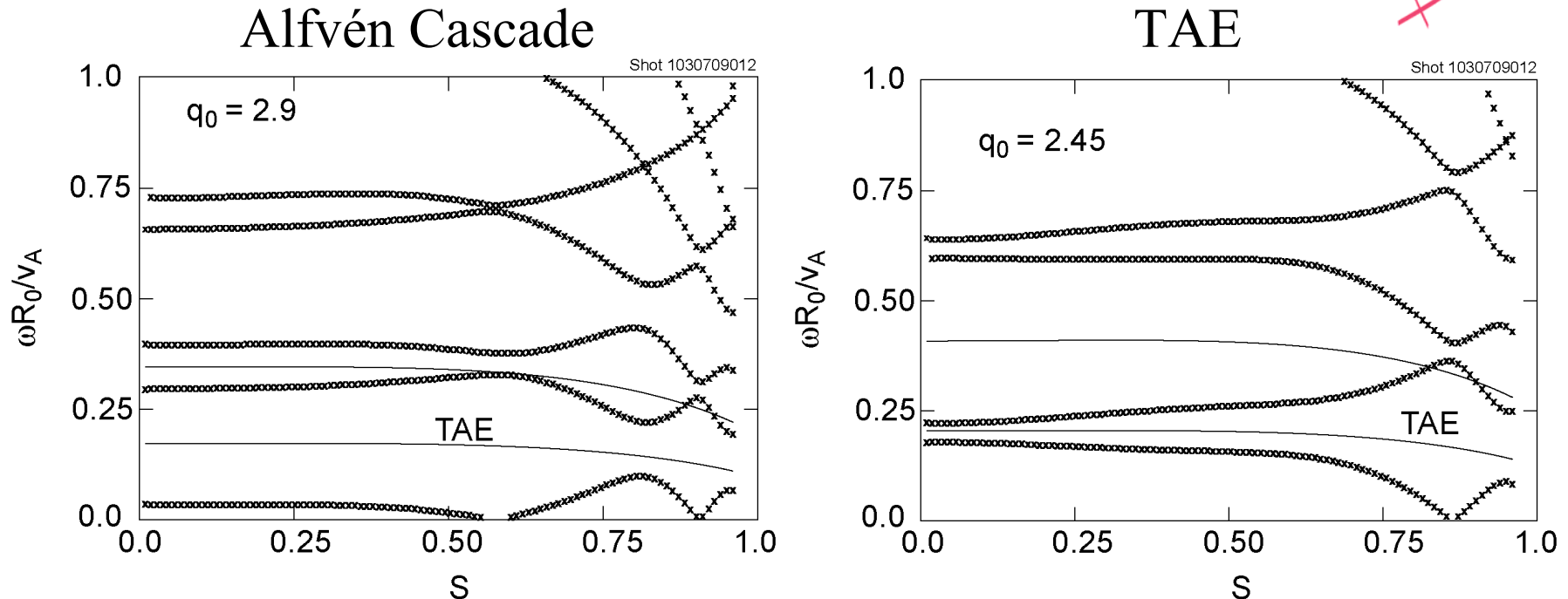
MISHKA Modeling of Alfvén Cascades



- From the frequency evolution of the Alfvén Cascades the evolution of the minimum q value can be modeled by the MISHKA¹ code
- The rapidly upward frequency chirping Alfvén Cascades develop into slowly varying TAE modes as the frequency peaks

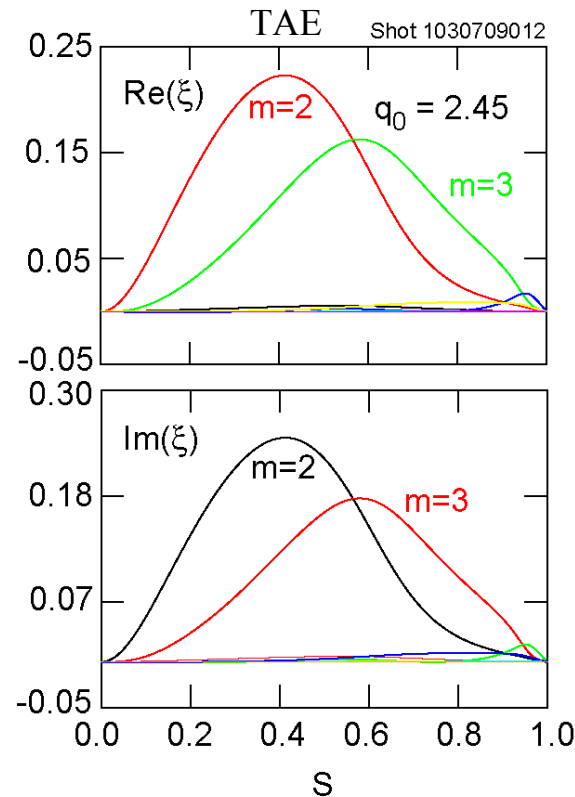
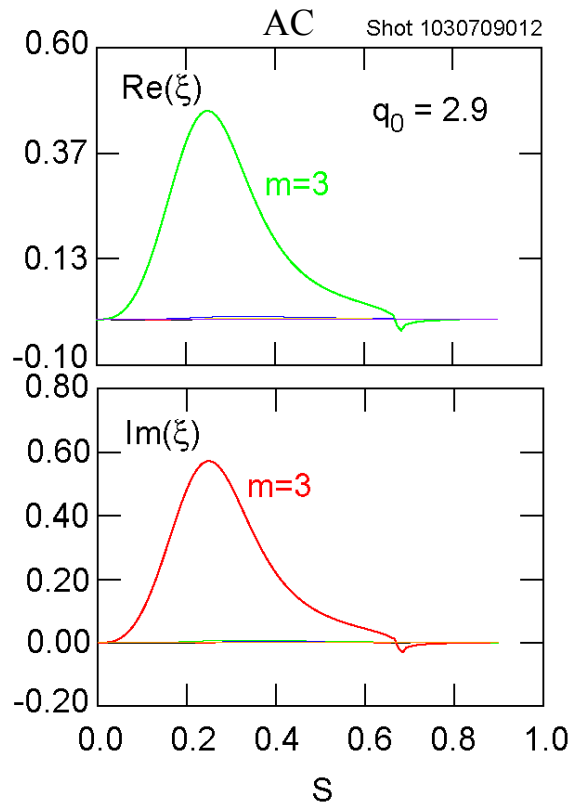
¹S E Sharapov

$n=1$ Alfvén Cascade Gap Structure



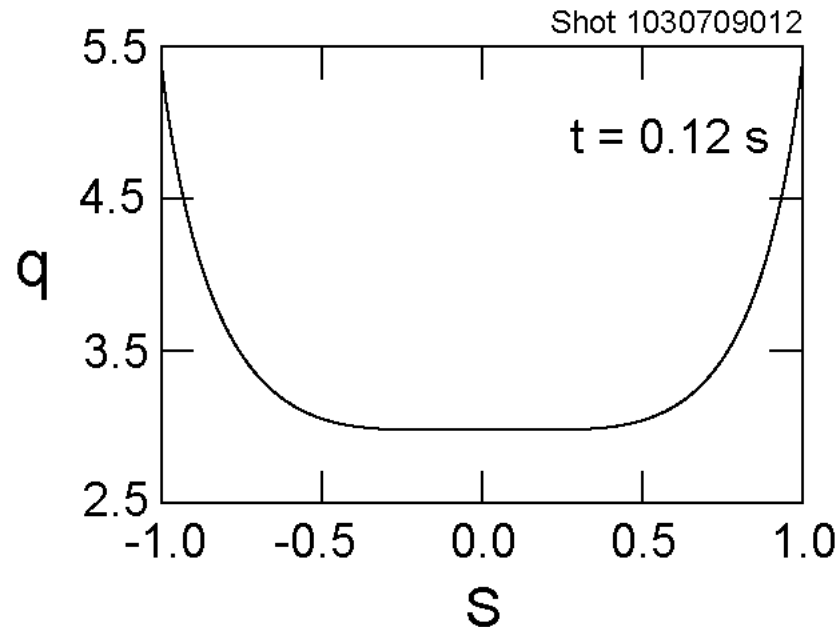
- At near integer q_0 the $n=1$ gap is wide allowing the Alfvén cascade frequency to sweep up to the TAE frequency
- As q_0 evolves to near a half integer value, the $n=1$ gap narrows to meet the TAE frequency as the Alfvén cascade becomes a TAE

$n=1$ Alfvén Eigenmode Radial Structure



- The MISHKA code calculated TAE has multiple m structure at $q_0 = 2.45$ and is closer to the edge than the single m Alfvén Cascade at $q_0 = 2.9$
- This agrees with the increasing amplitude $n=1$ mode as q_0 decreases

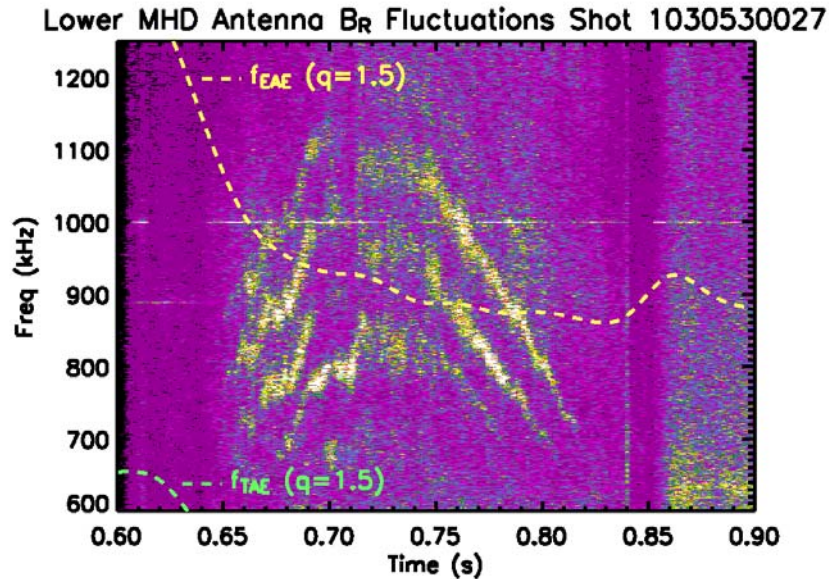
HELENA Equilibrium q Profile Calculation



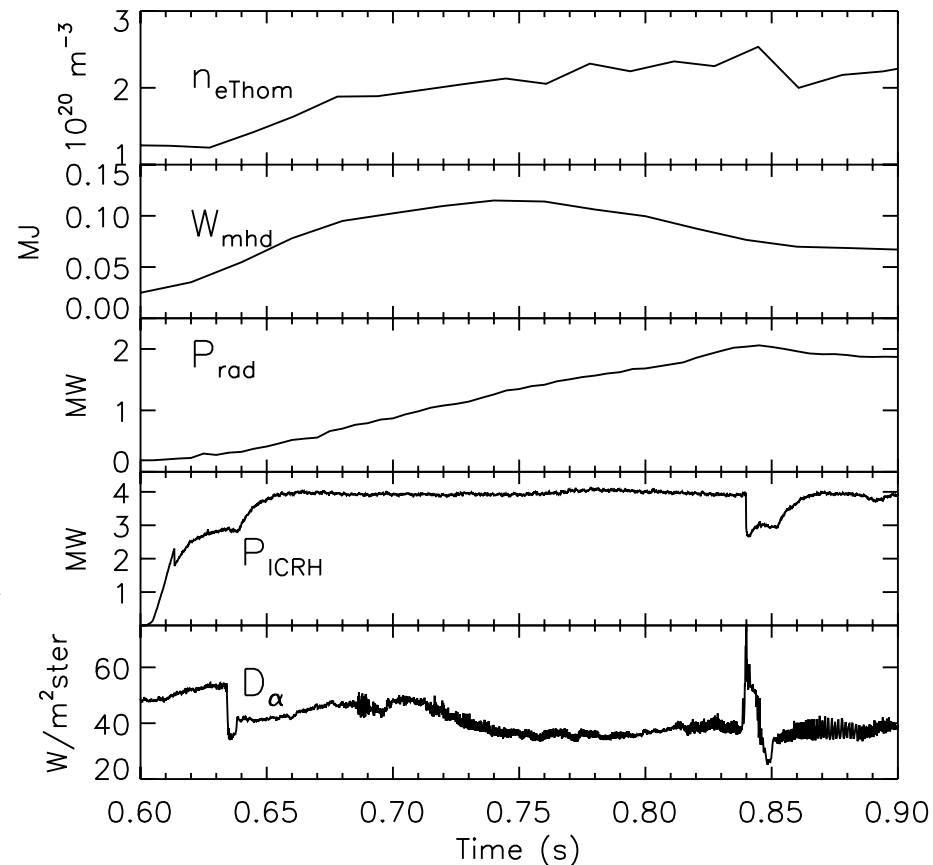
- The Alfvén Cascades together with some EFIT equilibrium parameters help to constrain an estimate of the q profile
- The data indicate a slightly reversed shear profile with $q_{\min} = 3$ at the bottom of the n=1 Alfvén Cascade (t = 0.12 s)

Unstable Modes in the EAE Frequency Range in Low Density High ICRF Heated EDA H-mode

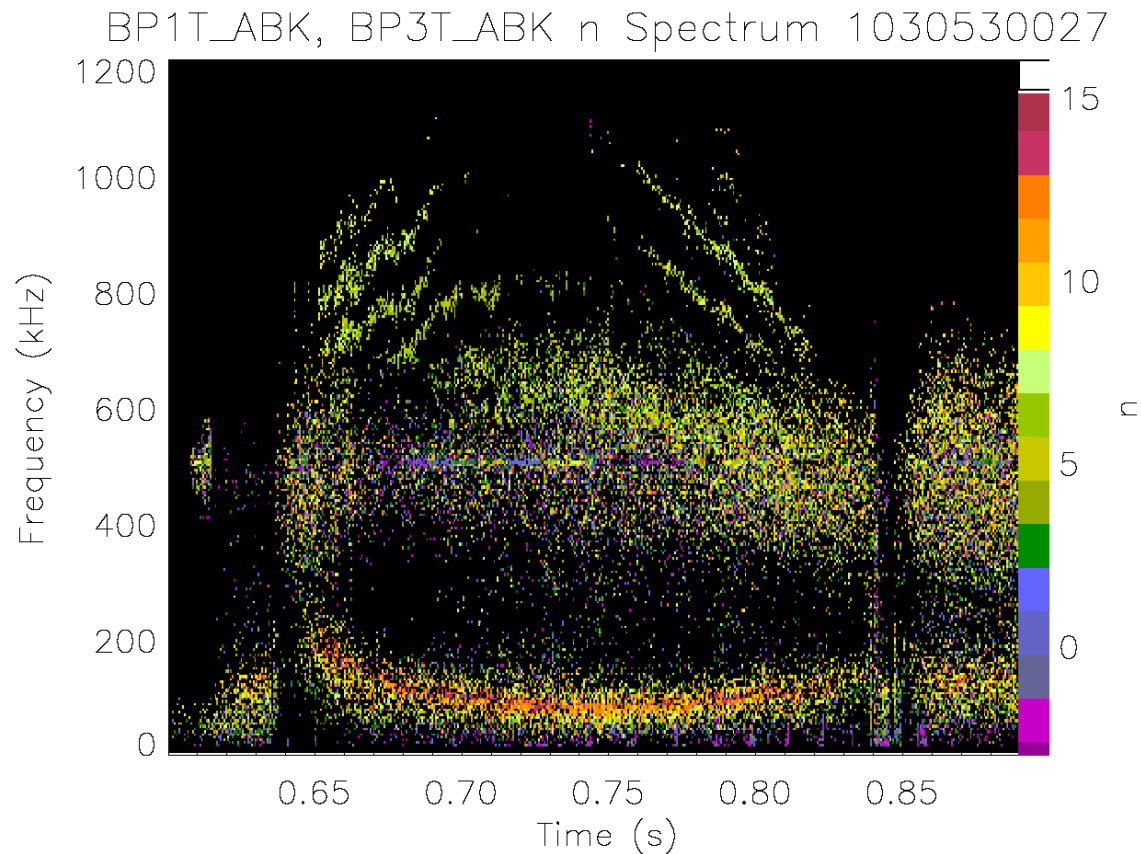
Alcator
C-Mod



- Multiple modes $700 < f < 1100$ kHz
- Low density ($n_e \approx 2 \times 10^{20} \text{ m}^{-3}$)
- High ICRF power (4 MW)
- Centered on the EAE gap at $q=1.5$

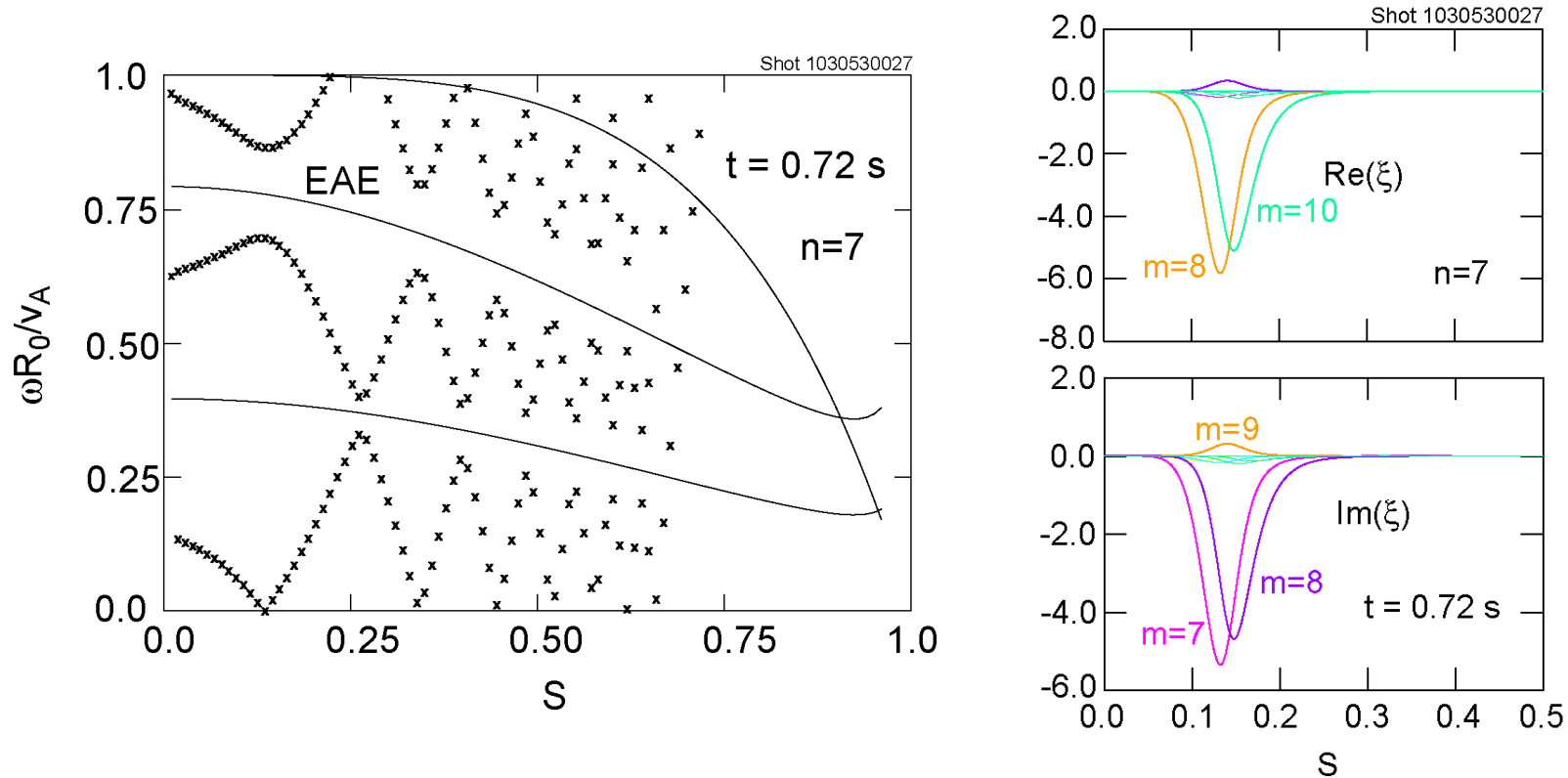


EAE Frequency Modes have $4 < n < 9$



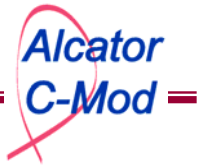
- EAE frequency modes have $4 < n < 9$ and rotate in the electron diamagnetic drift direction similar to the $n \sim 15$ quasi-coherent mode

MISHKA Finds Core Localized EAE's



- MISHKA modeling finds core localized EAE's, e.g., $n=7$ EAE at $\omega R_0/v_A \sim 0.75$ which corresponds to $f_{\text{EAE}} \approx 1$ MHz

Conclusions



- Stable TAE resonances at $q=1.5$ are actively excited with a single high n antenna in both limited and diverted discharges in the range of toroidal fields and densities expected in ITER
- Software synchronous detection provides good fits to the stable TAE resonances on multiple pick-up coil signals with $0.5\% < \gamma/\omega < 4\%$
- Diverted discharges require an outer gap < 1 cm to see the resonance
- Alfvén Cascades are observed in the current rise at low density with strong ICRF heating indicating slightly reversed shear with $q_{\min} = 3$
- Results agree well with MISHKA modeling of the Alfvén Cascades
- Modes are also observed in the EAE frequency range ~ 1 MHz in relatively low density EDA H-modes rotating in the electron direction