



EUROPEAN FUSION DEVELOPMENT AGREEMENT



Current Hole Effect on Fast Ion Confinement in JET

**V.Yavorskij^{1,2}, V.Goloborod'ko^{1,2}, K.Schoepf¹,
S.Sharapov³, C.Challis³, N.Hawkes³, S.Reznik^{1,2}, D.Stork³**

**¹*Institute for Theoretical Physics, University of
Innsbruck, Austria, Association EURATOM-OEAW***

²*Institute for Nuclear Research, Kiev, Ukraine*

**³*Euratom/UKAEA Fusion Association, Culham Science
Centre, Abingdon, Oxfordshire OX14 BPUK***

San Diego, 6-8 October 2003, IAEA TCM on Energetic Particles

OUTLINE

- Introduction & motivation
- Current hole (CH) model B
- FO loss and confinement criteria of fast ions
- Neoclassical & cone losses
 - i) DT alphas & DD tritons
 - ii) NBI tritons
- CH effect on the distribution of confined energetic ions
 - i) distribution function in COM space
 - ii) density, bootstrap-current, bulk plasma heating profiles, NBI triton induced neutron emission
- Summary



EUROPEAN FUSION DEVELOPMENT AGREEMENT



• Motivation

Hollow current profiles typical for tokamak experiment scenarios with ITBs $\Rightarrow$

**improved plasma core energy confinement at reduced inductive current
plasma equilibrium states stable over remarkably long periods**

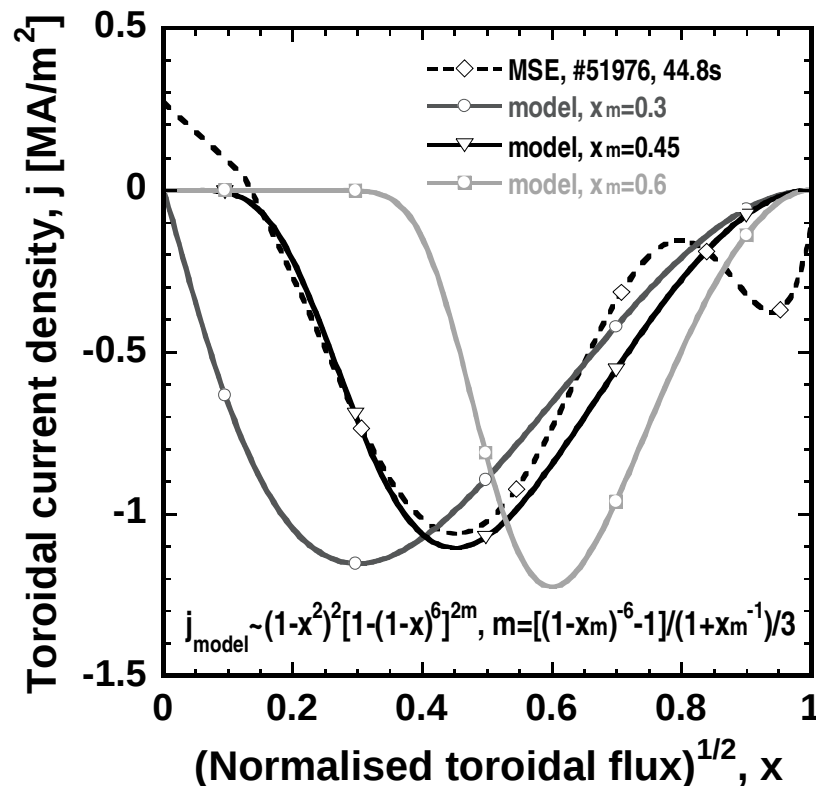
**$\Rightarrow$ hollow current configurations could be regarded as serious candidate for
stationary operation of a fusion tokamak-reactor**

confinement of charged fusion products (CFPs) and NBI ions - ?

Purpose:

- **examine the effect of toroidal current hole on FO loss and on the collisional loss of fast ions,**
- **predictive modelling of distribution function of CFPs (3.5 MeV α 's and 1MeV t's) and NBI ions in hollow current JET discharges**

• Model used

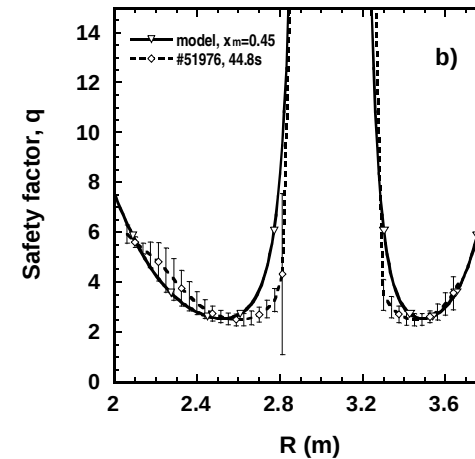
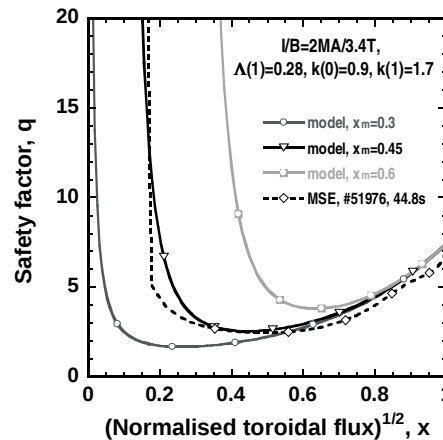
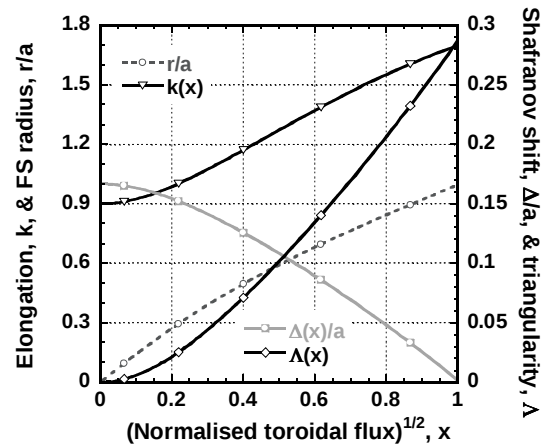


Model B with $j(r)$ and FS shape from MSE measurements for JET (#51976)

x_m radial position of maximum $j(r)$

reasonable approximation for measured $j(r)$ in JET ($x_m=0.45$, #51976) and JT-60 ($x_m=0.6$)

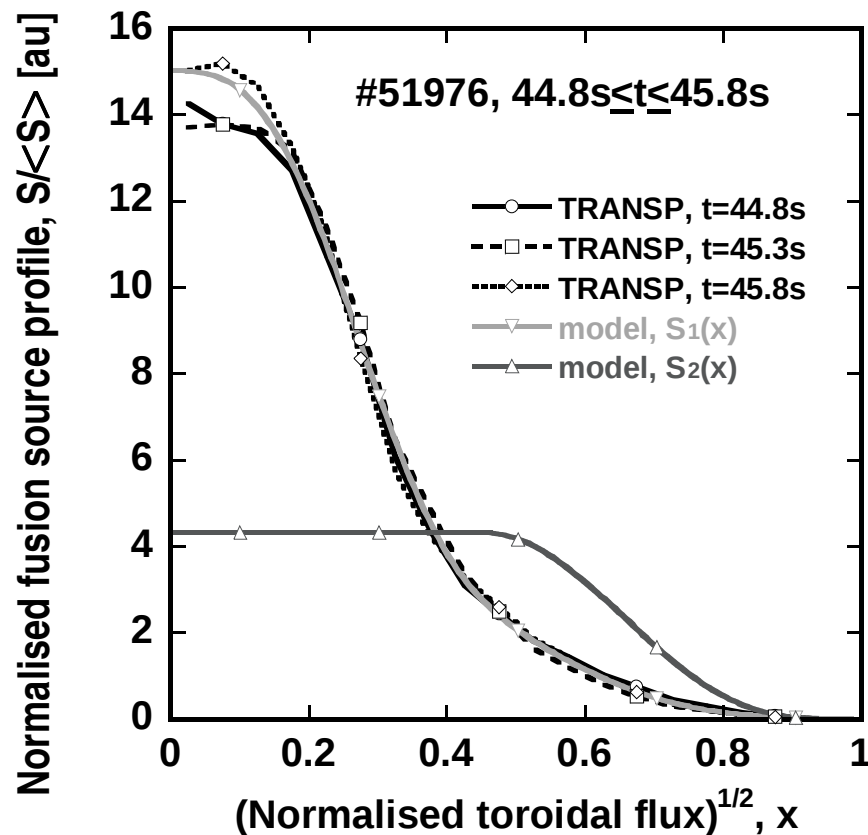
FS shape parameters and q -profiles



- a) Shafranov shift $\Delta(r) = \Delta_0[1-(r/a)^2]$,
 - b) elongation $k(r) = k_a - [k_a - k_0][1-(r/a)^2]^2 - 0.5 k_a'(r/a)^2[1-(r/a)^2]$,
 - c) triangularity $\Lambda(r) = \Lambda_a(r/a)^2$
- with $\Delta_0=0.15m$, $k_a=1.7$, $k_0=0.9$, $\Lambda_a=0.28$, $k_a'=0.8$

Reconstructed q -profiles are in satisfactory agreement with MSE measurements

CFPs source term & plasma parameters



$$S_1 \sim \exp(-33x^3) + 30.7x^4 \exp(-11x^2)$$

$$S_2 \sim n_d n_t \langle \sigma V \rangle$$

n_d, n_t - deuteron and triton density

$\langle \sigma V \rangle$ - fusion reaction rate

$$T_e = 10 p(x) \text{ keV}, T_d = T_t = 20 p(x) \text{ keV},$$

$$n_e = 0.5 \times 10^{20} p(x) \text{ m}^{-3}, n_d = n_t$$

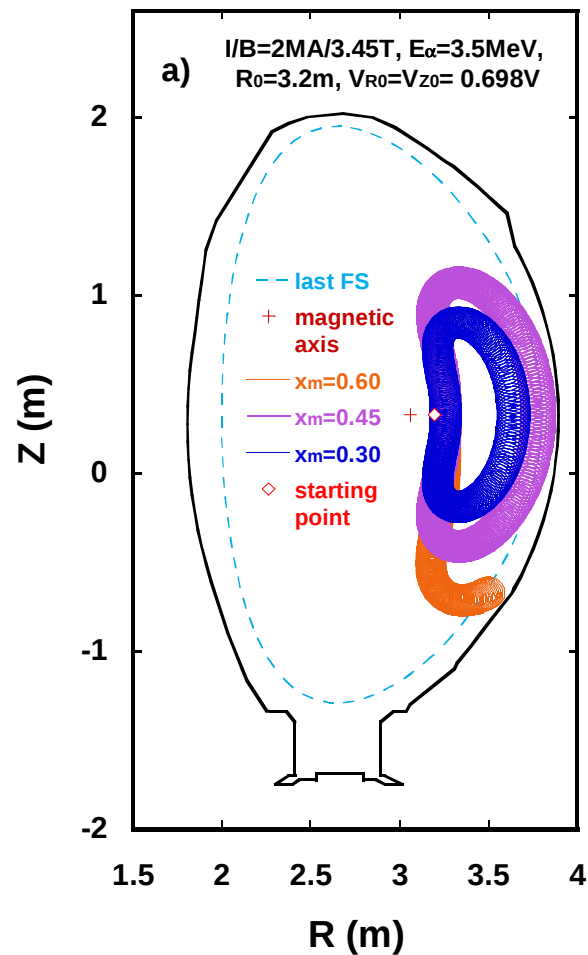
$$Z_{\text{eff}}(x) = 1.5 + 2.4x^2 / (1 + 4x^{20})$$

$$p(x) = 1 - ((x - x_m^*) / (1 - x_m^*))^2 \Theta(x - x_m^*),$$

$$x_m^* = 0.45$$

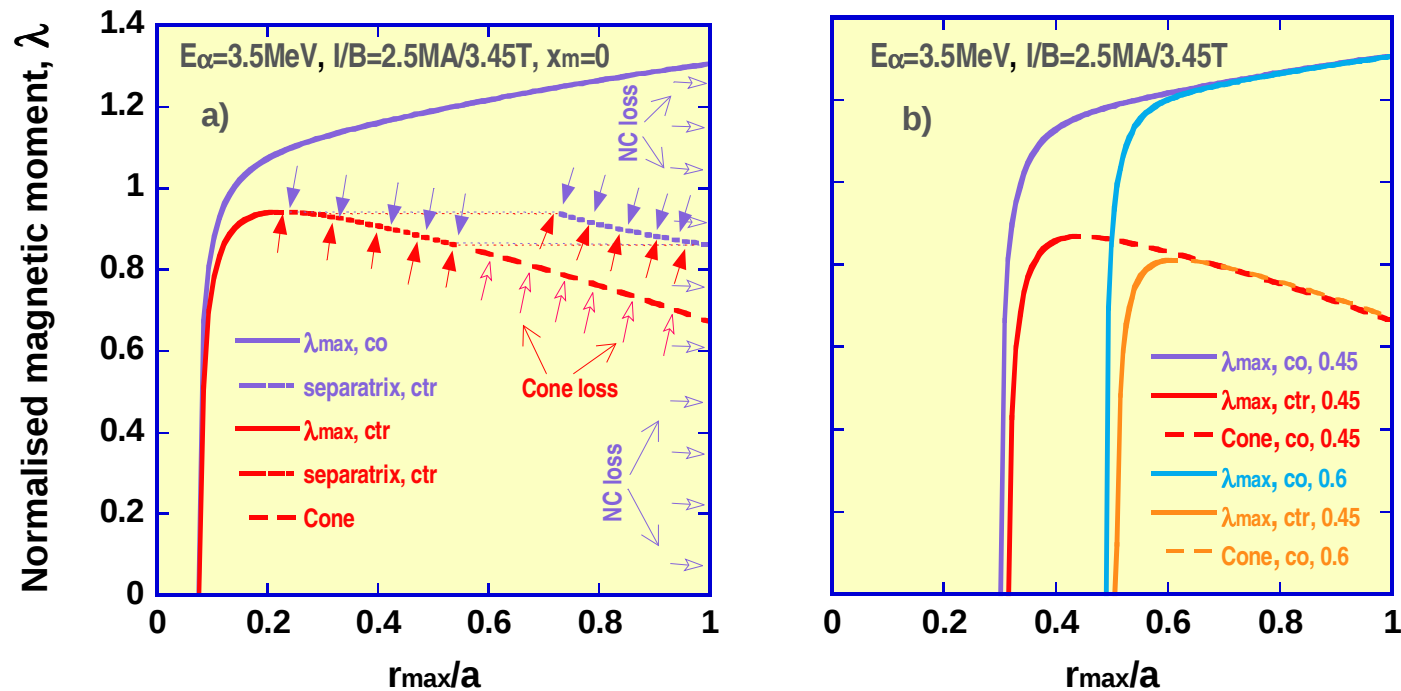
$\Theta(x)$ - Heaviside step function

3.5MeV alpha gyro-orbits



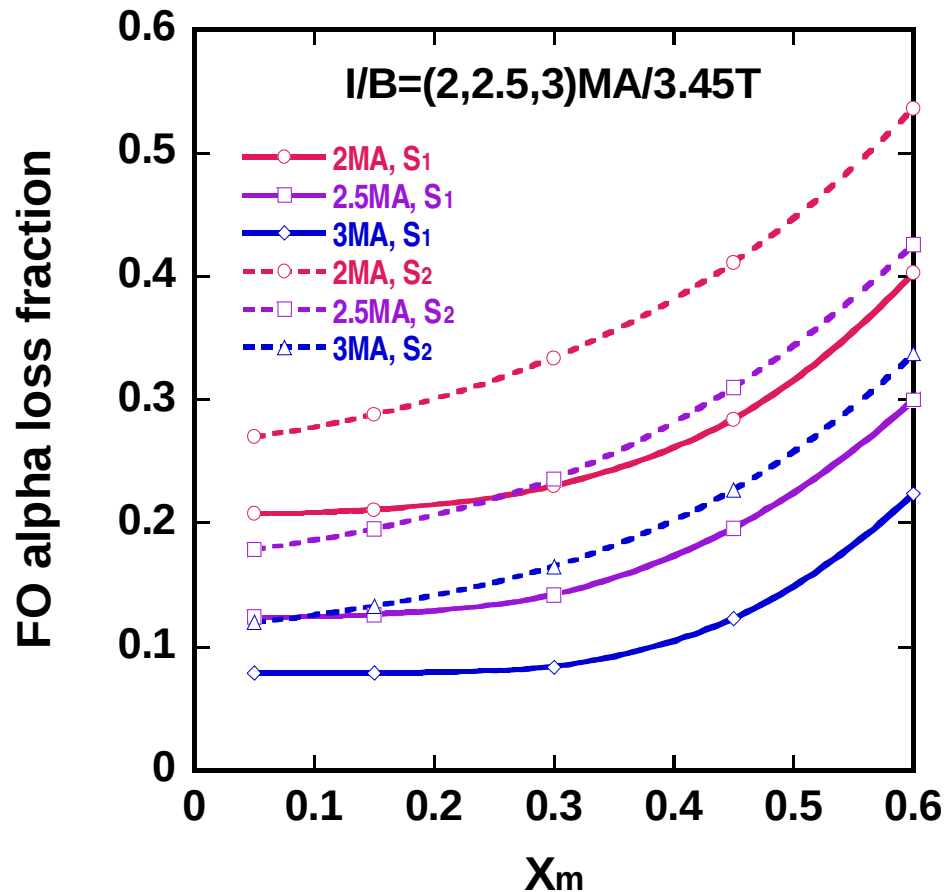
- Fixed FS shape & same initial conditions
- Effect of current hole is rather strong

Confinement domains



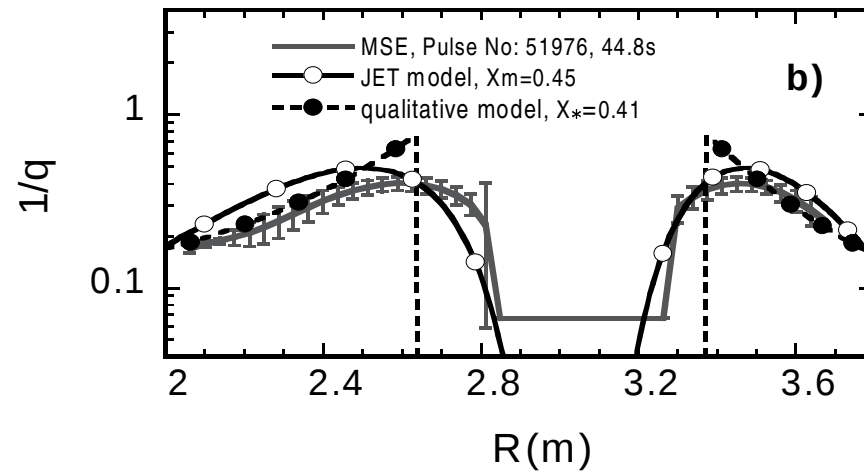
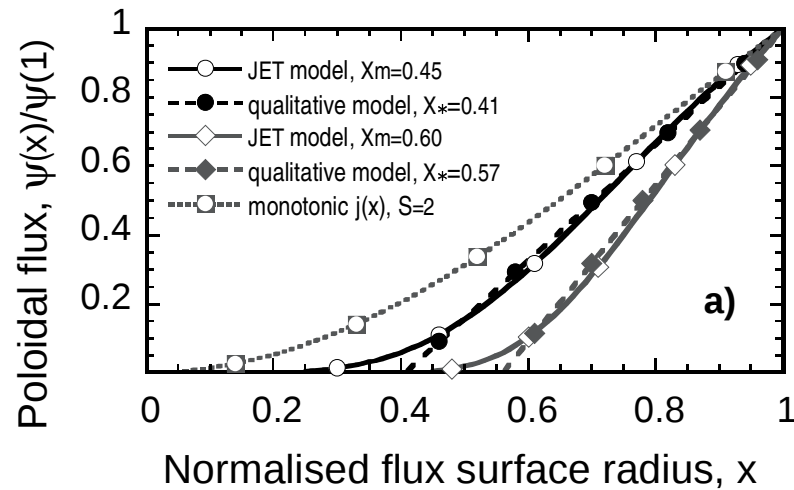
- substantial reduction of confinement domain of alphas as current hole region is enlarged (increasing x_m)

First orbit (FO) loss of alphas



- current hole enhances FO loss from (8-25)% at monotonic profile ($x_m \Rightarrow 0$) to (20-50)% at $x_m = 0.6$
- shift of current maximum from 0.45 to 0.6 corresponds to effect of current decrease of about 0.5MA

Confinement criteria (qualitative consideration)



$$\Psi(r) \cong a \Psi'_a \psi(x - x_*), \quad \psi(y) = \begin{cases} 0, & y \leq 0 \\ 0, & y > 0 \end{cases}$$

$x_* \cong 0.2 + 1.1x_m^2 - 0.3x_m^4$ - effective size of current hole

Critical currents & energies

- $I > I_{cr1}$; ($E < E_{cr1}$) particles crossing CH, $r < r_*$, are confined
- $I > I_{cr2}$; ($E < E_{cr2}$) particles crossing $r=0$ are confined

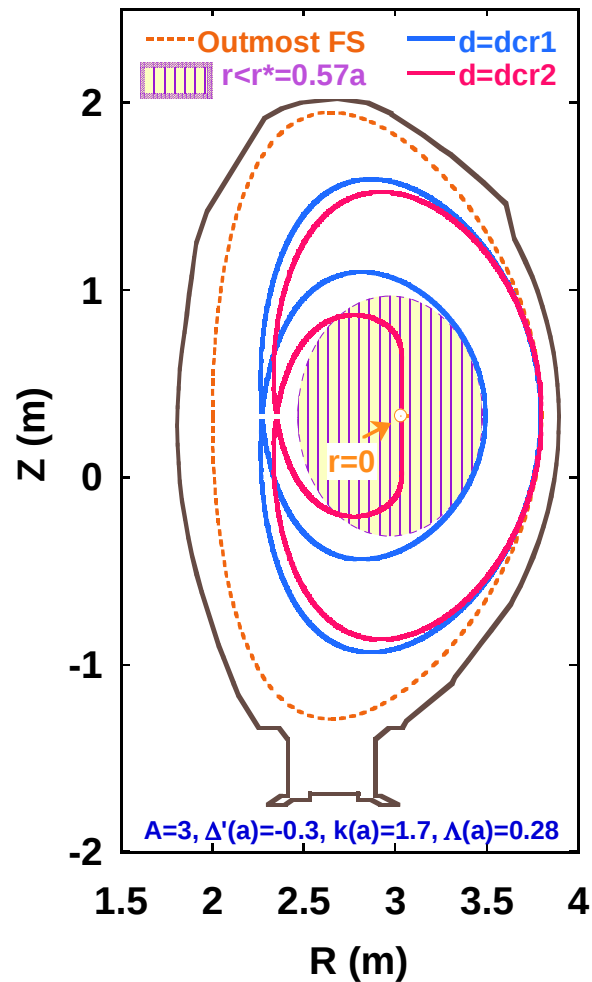
$$I_{cr1} \cong F \frac{1}{Z_i} \sqrt{\frac{\mu_i E}{A}} \frac{1}{1 - \sqrt{x_*}} = I_{cr2} f$$

$$E_{cr1} \cong \frac{A}{\mu_i} \left[\frac{Z_i I}{F} (1 - \sqrt{x_*}) \right]^2 = \frac{E_{cr2}}{f^2}$$

E in MeV, I in MA, Z_i and μ_i - fast ion charge & mass numbers
 $1 < F < 1.5$ – geometrical factor

$$1 \leq f(x_*) \approx (1 + 0.285\sqrt{x_*} - 0.107x_*) < 1.2 \quad I > \{I_{cr1}, I_{cr2}\}, \quad E < \{E_{cr1}, E_{cr2}\}$$

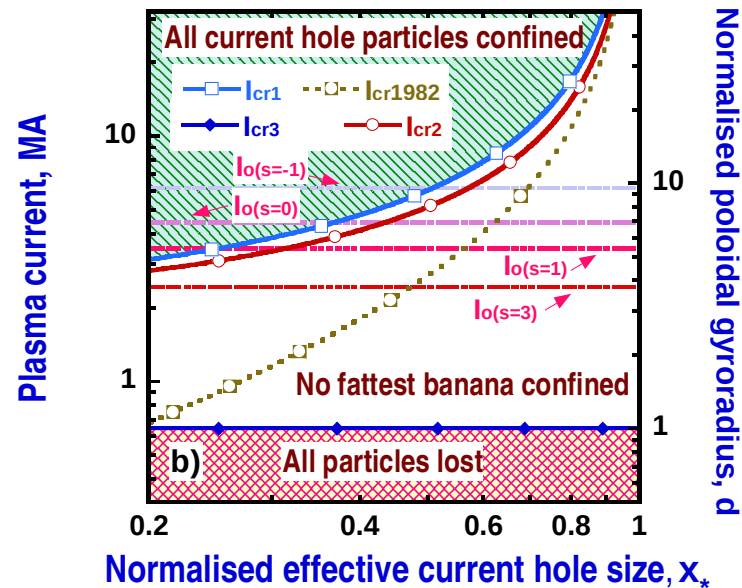
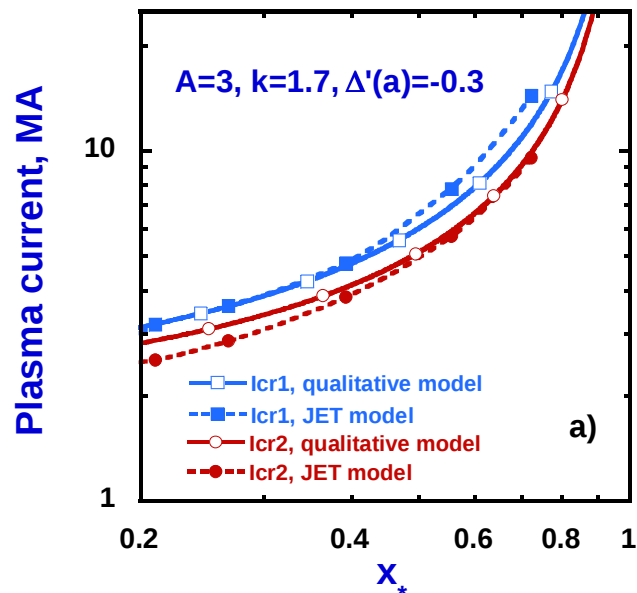
Orbits of marginally confined barely trapped particles for $x_* = 0.57$



- d – poloidal gyroradius/(plasma major radius)
- at $d < d_{cr1} = 0.08$ particles crossing current hole, $r < r_*$, are confined
- at $d < d_{cr2} = 0.108$ particles crossing $r=0$ are confined
- $I_{cr1} = 7.6\text{MA}$, $I_{cr1} = 5.6\text{MA}$ for alphas
- Essential improvement of confinement requires only $\sim 20\%$ reduction of d even in the case of rather large CH

Critical currents required to confine fusion alphas passing hollow

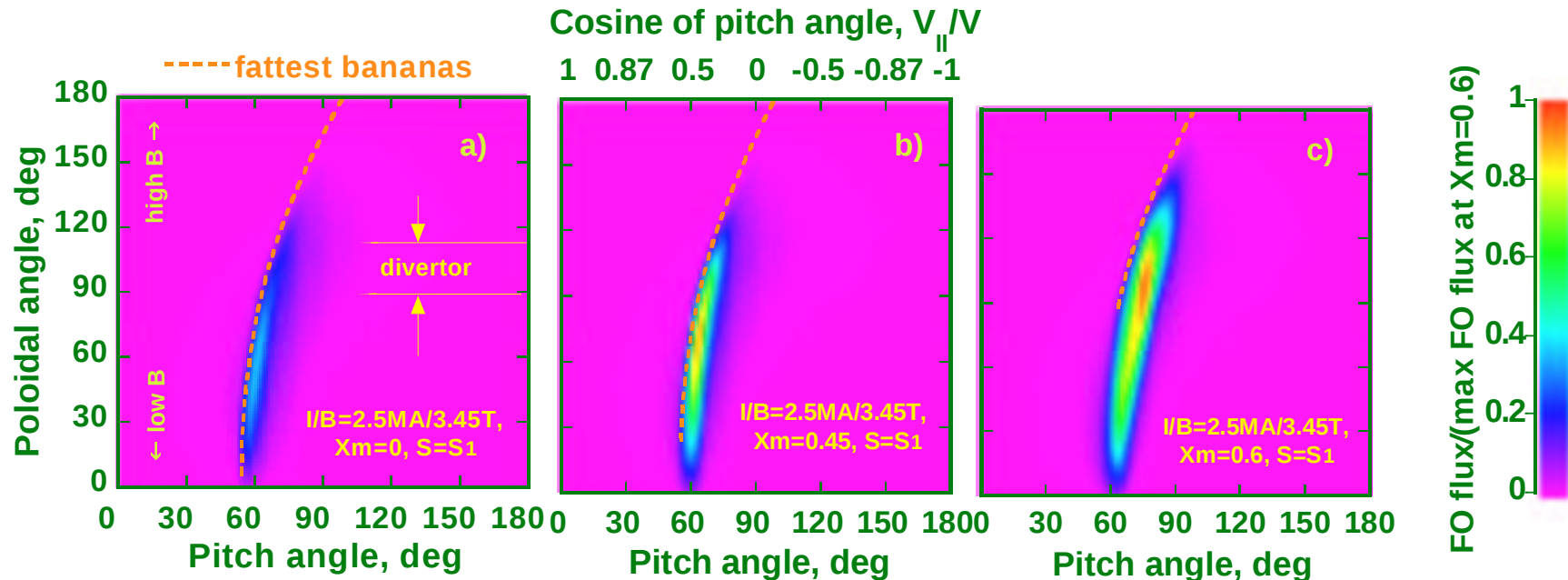
current plasma core, I_{cr1} , & plasma centre, I_{cr2}



➤ in ITER-like tokamak $I \geq 10\text{MA}$ will provide a good alpha confinement for hollow current scenarios with x_* up to ~ 0.7

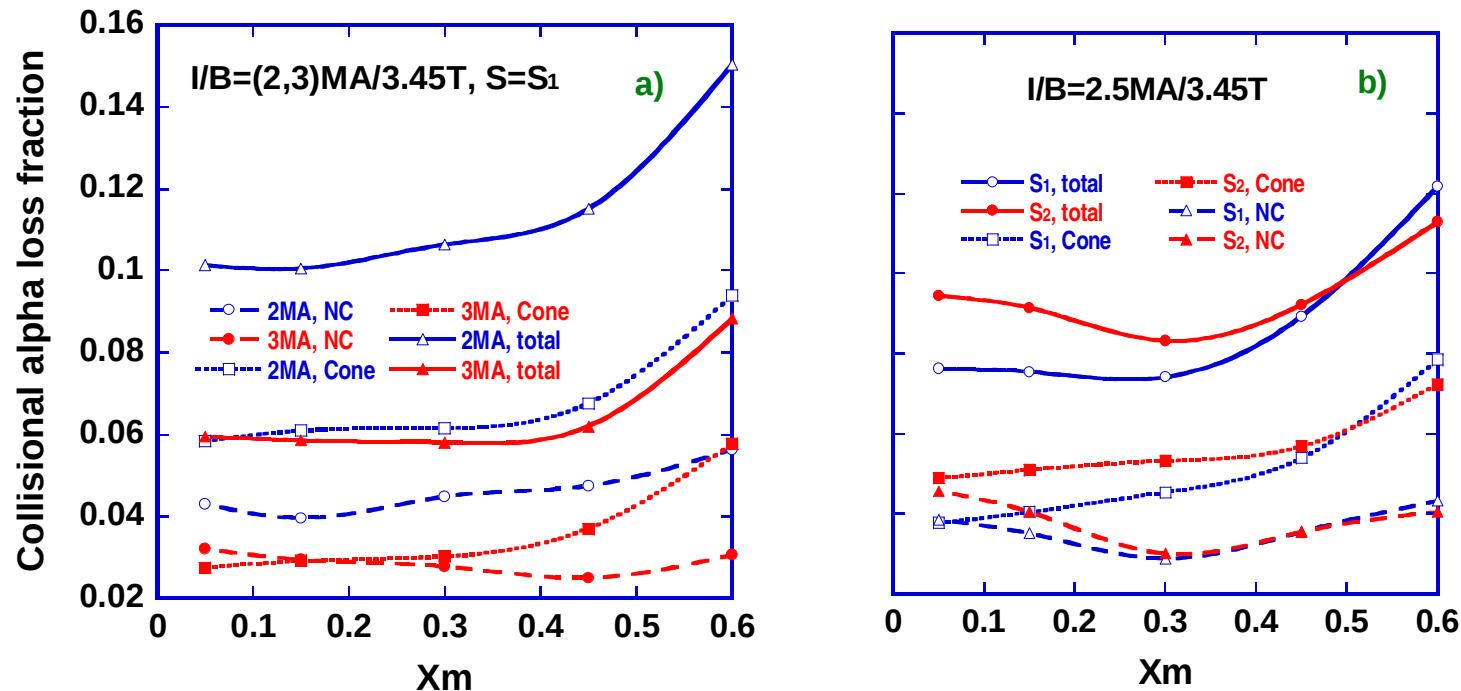
➤ current hole effect is equivalent to the reduction of total plasma current given by factor $1 - x_*^{1/2}$

Distribution of FO alpha flux over pitch and poloidal angles



- $\Gamma(\zeta, \theta) = [\text{number of particles lost per } 1\text{m}^2 \cdot (1\text{pitch angle deg}) \cdot 1\text{s}]$
Poloidal angle $\theta \Leftrightarrow \sin \theta = -Z/2.9\text{m}$ counted clockwise from min B at midplane ($R=3.9\text{m}$)
- Transition from $x_m=0$ to $x_m=0.6$ enlarges maximum FO loss about 2.5 times and shifts it from $\theta \approx 55^\circ \div 60^\circ$ below midplane to rather high $\theta \geq 100^\circ \div 105^\circ$ (divertor area)

Collisional loss fractions L_{NC} and L_{CONE} of alphas with $0.0625 < E/E_0 < 1$

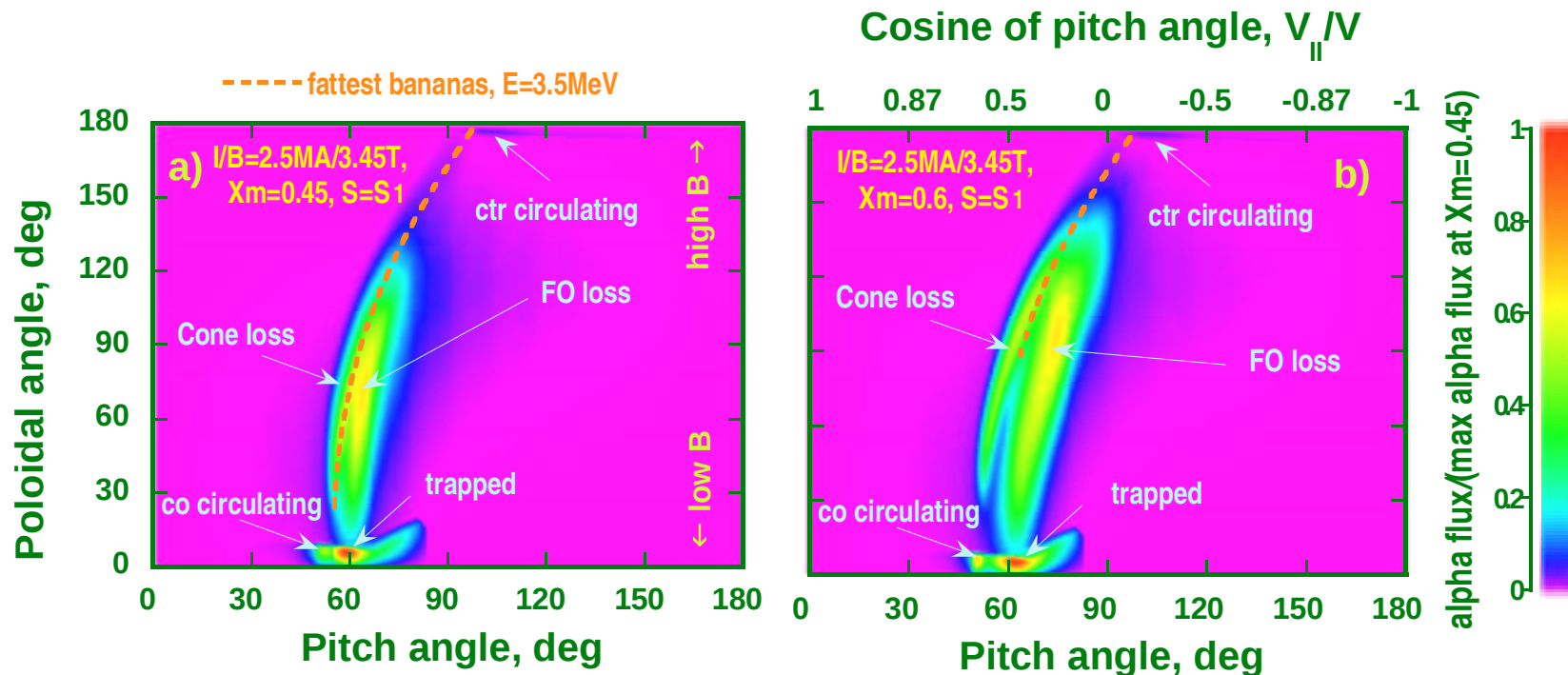


collisional loss fraction of fast alphas

$$L_{\text{coll}} \sim (D_{\lambda\lambda}/v_s)^{1/2} \sim (D_{rr}/[a-r_{\min}(\lambda=0, \sigma)]^2 v_s)^{1/2} \sim 0.1 \text{ for } v_{\perp}/v_s \sim 10^{-2}$$

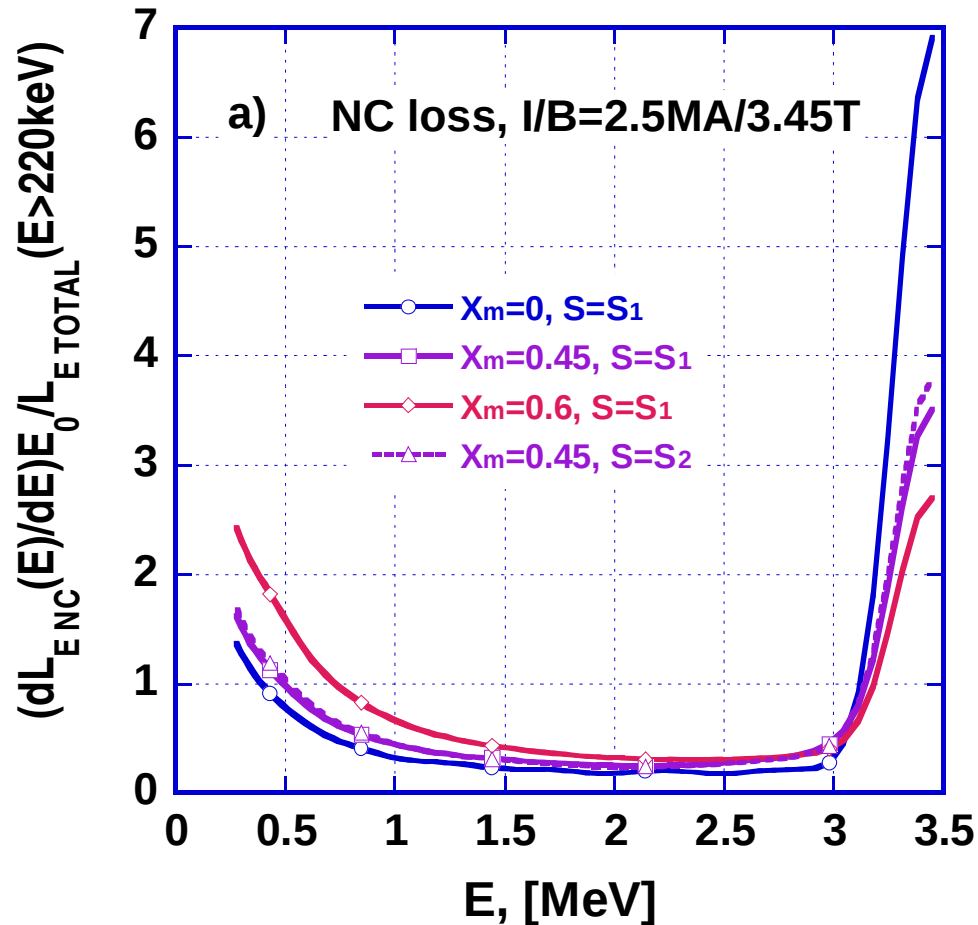
reason - rather steep initial distribution of confined alphas, $|\partial \ln f_{\alpha} / \partial \ln c_i| \gg 1$

Distribution of collisional + FO alpha flux over the pitch and poloidal angles



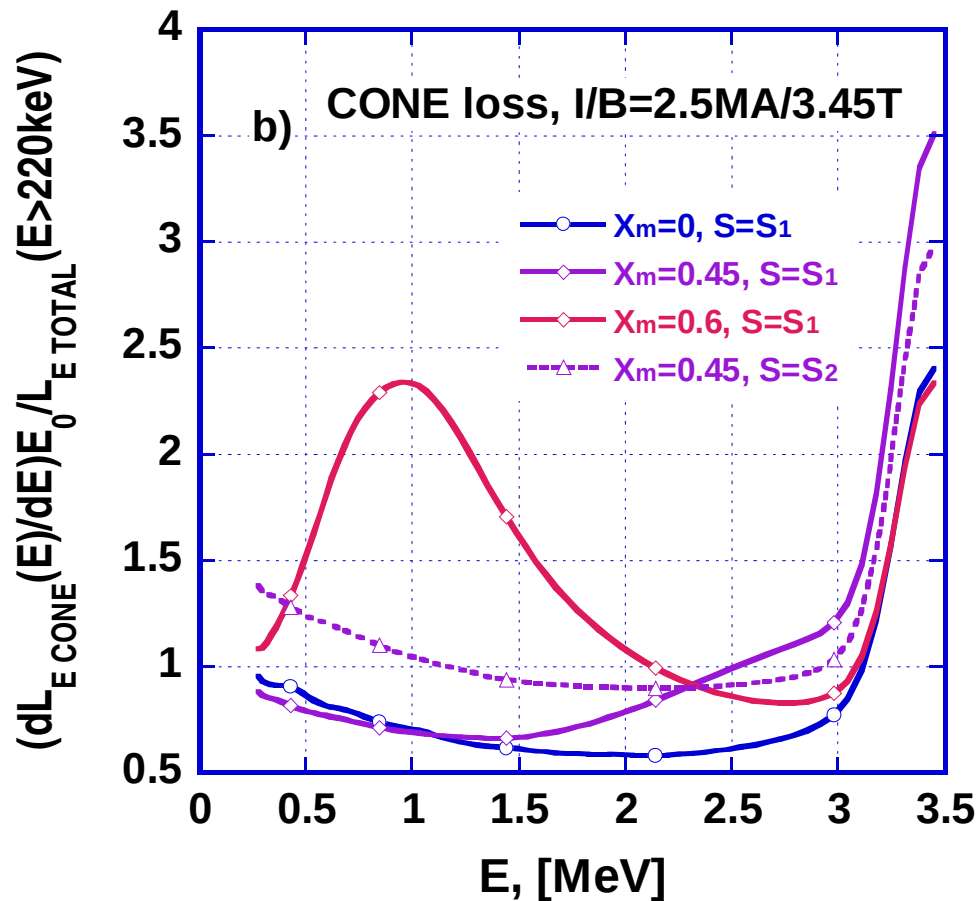
- maximum collisional fluxes result from NC loss of trapped alphas at poloidal angles $\sim 10^\circ$ and pitch angles $\sim 60^\circ$ and from cone loss of fattest bananas at pitch-angles $\sim 50^\circ - 70^\circ$

Energy spectra of NC collisional loss



- For NC loss effect of current hole is important only at high, $E > 3\text{MeV}$, and low, $E < 1\text{MeV}$, energies

Energy spectra of cone collisional loss



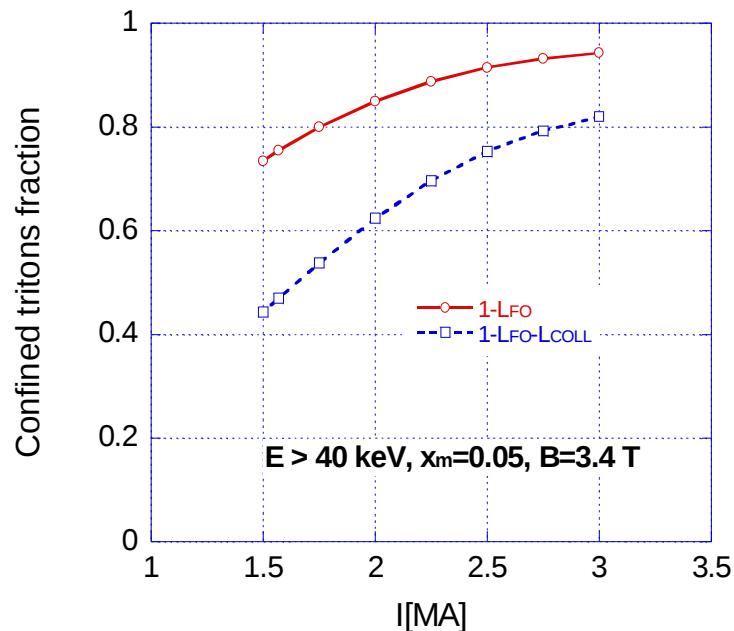
- cone loss is essentially affected by toroidal current shape also in moderate energy range $1\text{MeV} < E < 3\text{MeV}$
- peculiarities of cone loss spectra are due to increase of -loss cone size in phase space with enlargement of current hole area and -number of alpha particles contributing to loss at plasma periphery

$$\Gamma \sim D(1-L_{FO})d\ln f/d\ln c$$

Loss of DD Tritons ($40\text{keV} < E < 1.4\text{MeV}$) $S(r) = S_{\text{JET}}$ (#51976)

While $L_{\text{FO}} \text{ DD tritons} \approx L_{\text{FO}} \text{ DT alphas}$ (due to gyro radii $\rho_{\text{DD tritons}} = 0.93\rho_{\text{DT alphas}}$) the collisional loss L_{coll} of tritons is enhanced because of higher efficiency of pitch-angle scattering

$$\Rightarrow (v_{\perp}/v_s)_{\text{DD tritons}} \sim 7(v_{\perp}/v_s)_{\text{DT alphas}}$$

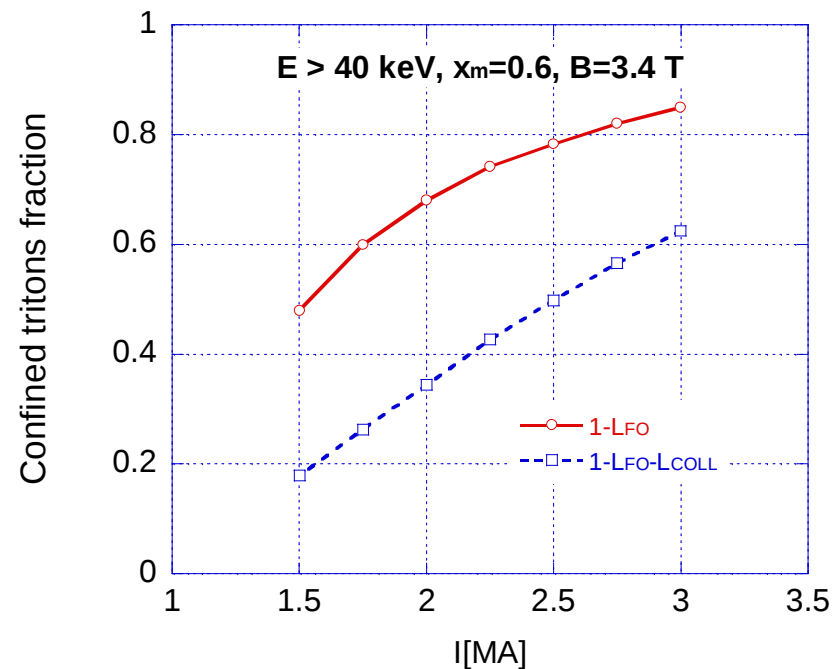
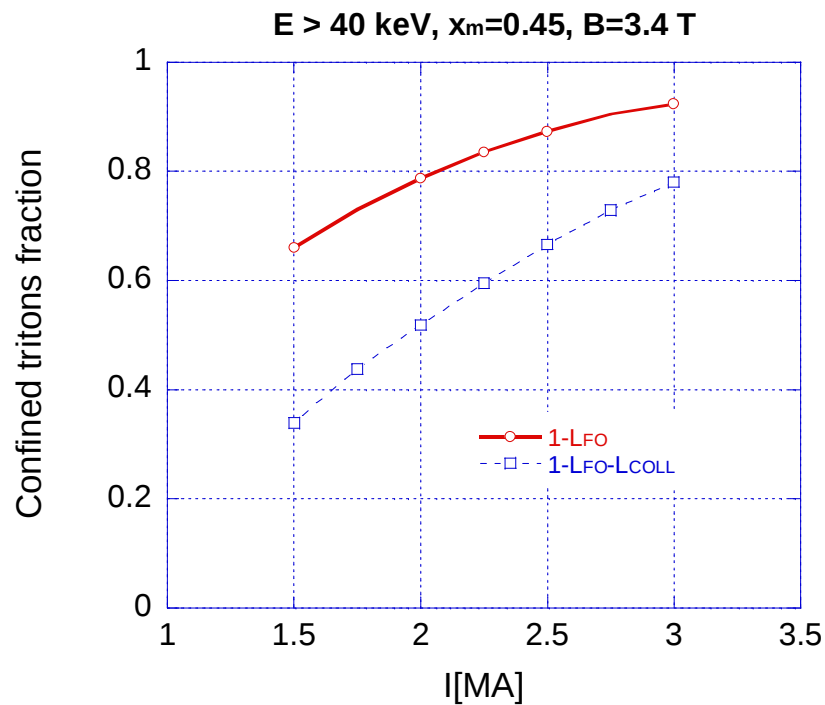


monotonic $j(r)$

$$L_{\text{coll}} \text{ DD tritons} > L_{\text{FO}} \text{ DD tritons}$$

$$L_{\text{coll}} \sim 15-30\%$$

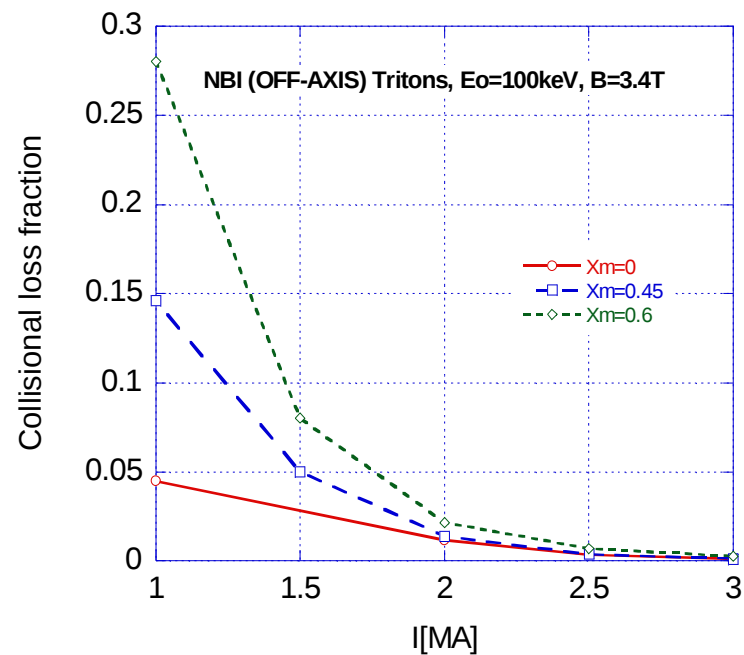
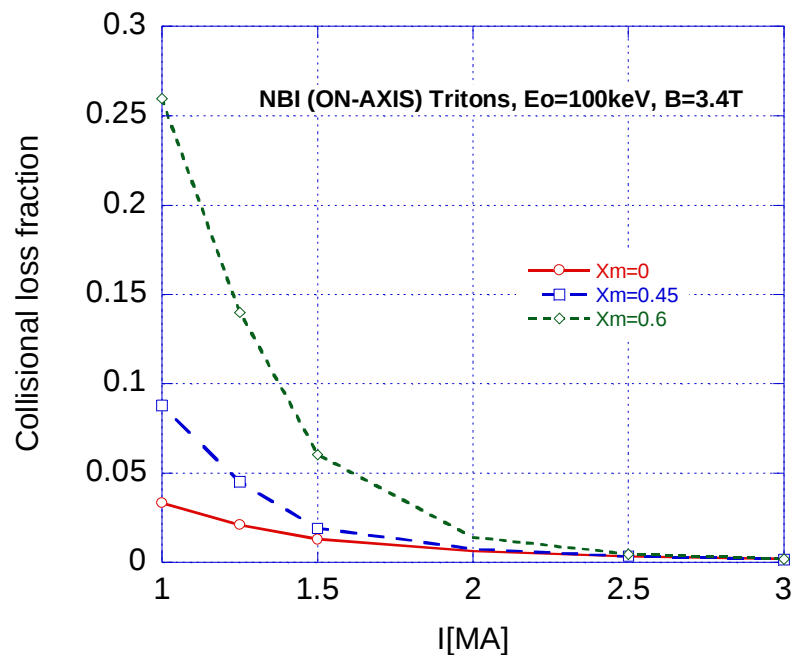
Current hole effect on the confinement of DD tritons



Essential effect of collisional transport on triton burn-up

San Diego, 6-8 October 2001 IAEA TCM on Energetic Particles

Collisional loss of 100keV co-injected NBI tritons



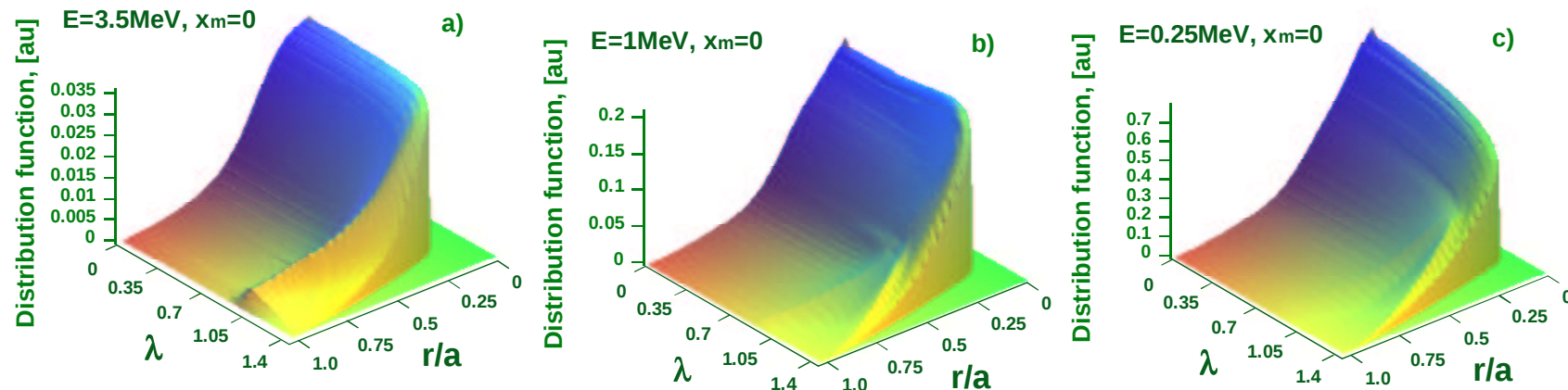
Collisional loss becomes essential ($\geq 10\%$) only at $I < 1.5\text{MA}$ and $x_m \geq 0.5$

$I_{\text{cr1}}(x_*=0.4) = 1.5\text{MA}!$

San Diego, 6-8 October 2003, IAEA TCM on Energetic Particles

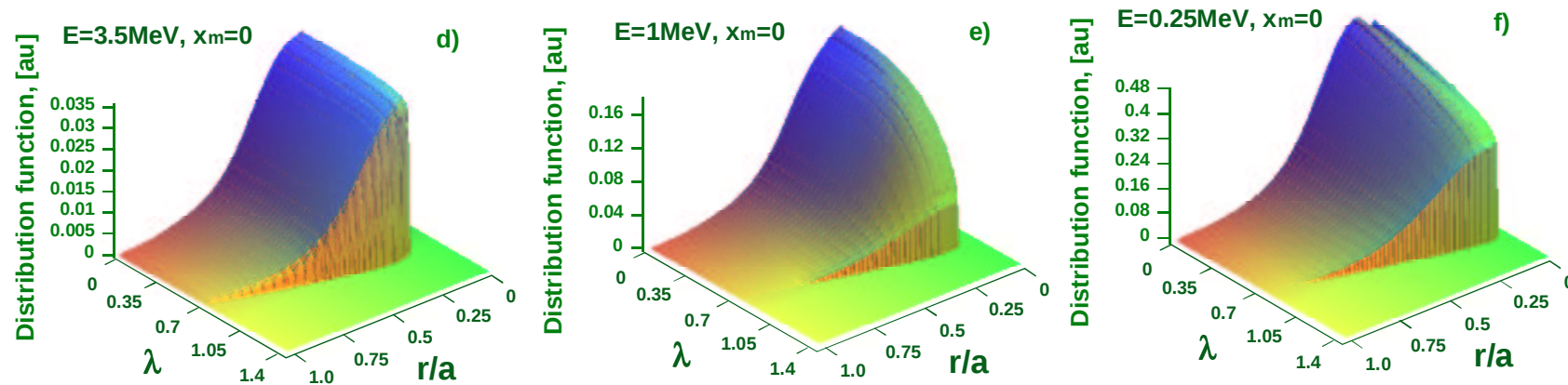
Distribution function of confined alphas at I/B=2.5MA/3.45T for monotonic $j(r)$

co-going particles, $x_m=0$



Normalized to $f_0=S_0/(4\pi V_0^3 v_0)$, S_0 - alpha source rate, $V_0=1.3 \cdot 10^9\text{cm s}^{-1}$,
 $v_0=0.03 \text{ s}^{-1}$, $S_{0\text{ DT}} \approx 10^2 S_{0\text{ DT}} \sim 10^{11}\text{cm}^{-3}\text{s}^{-1}$

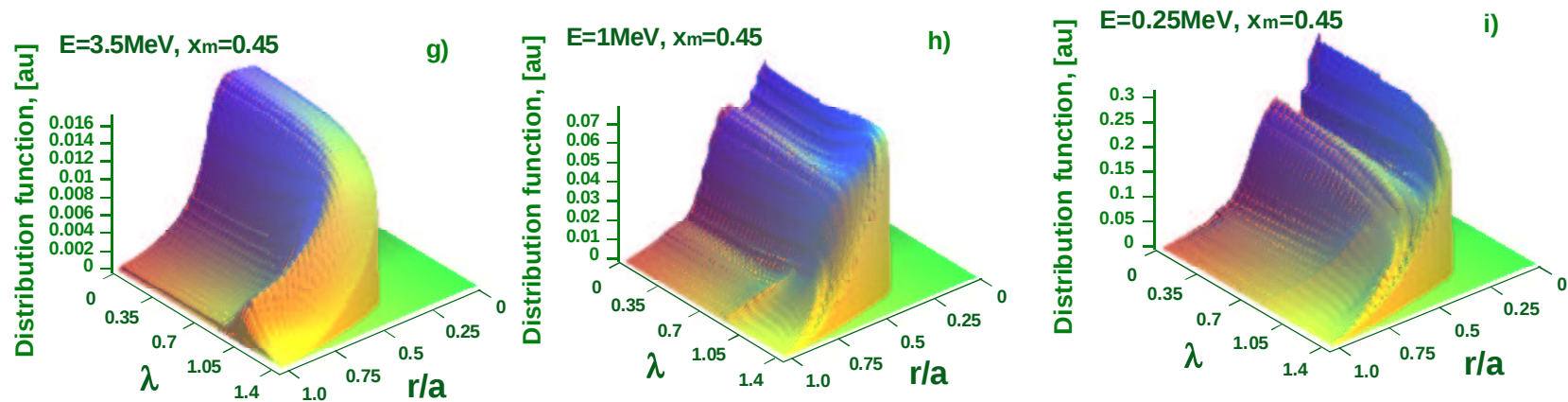
- counter-going particles, $x_m=0$



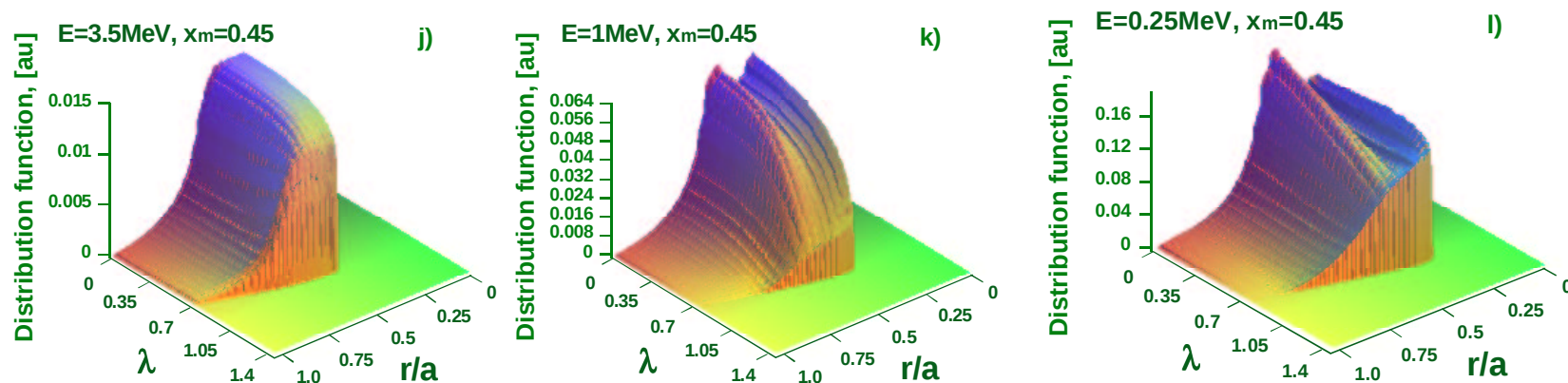
$f(r_{\max}, \lambda)$ - monotonic in “radial” coordinate with maximum corresponding to stagnation orbits

Distribution function of confined alphas at $I/B=2.5\text{MA}/3.45\text{T}$ for hollow $j(r)$

co-going particles, $x_m=0.45$



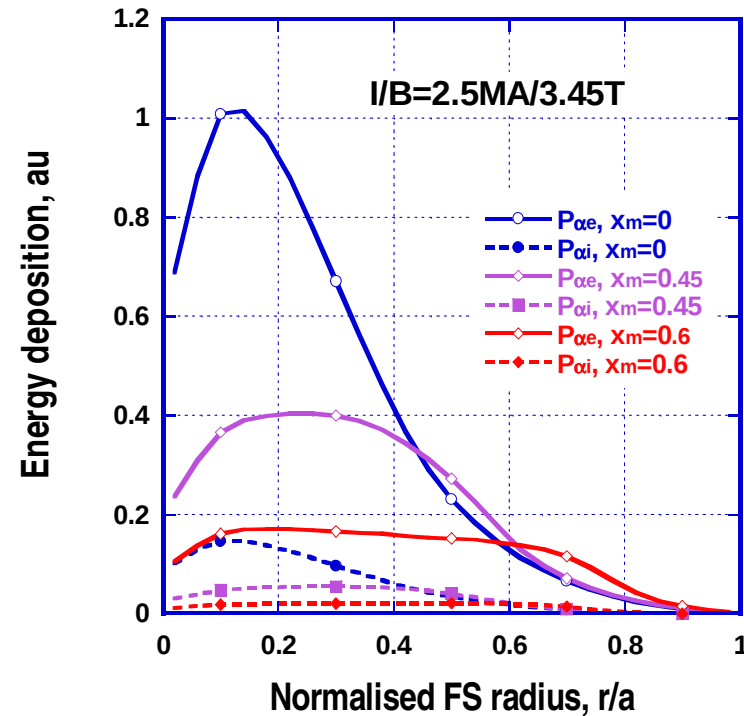
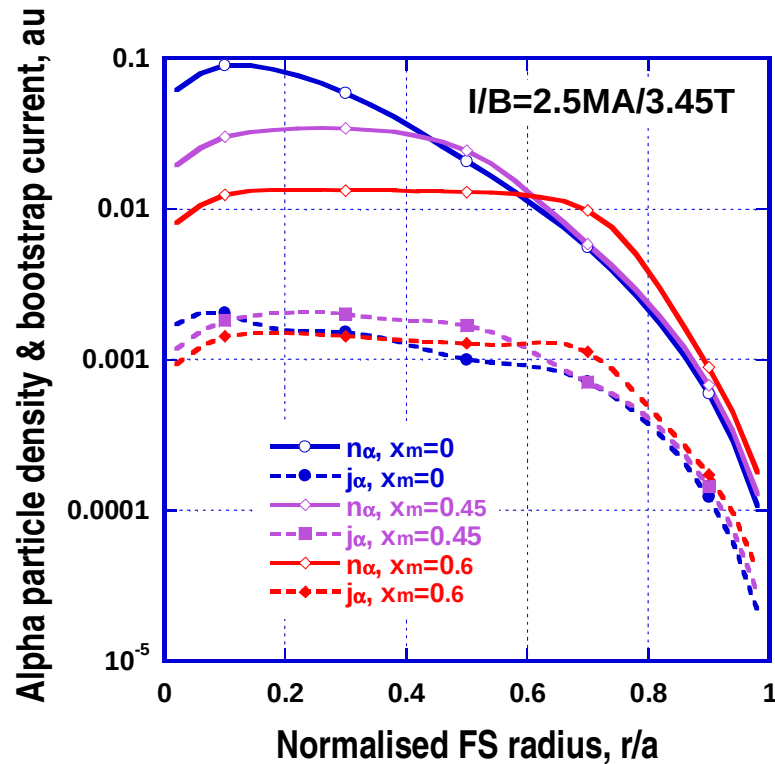
- counter-going particles, $x_m=0.45$



$f(r_{\max}, \lambda)$ - nonmonotonic in “radial” coordinate with maximum corresponding to stagnation orbits

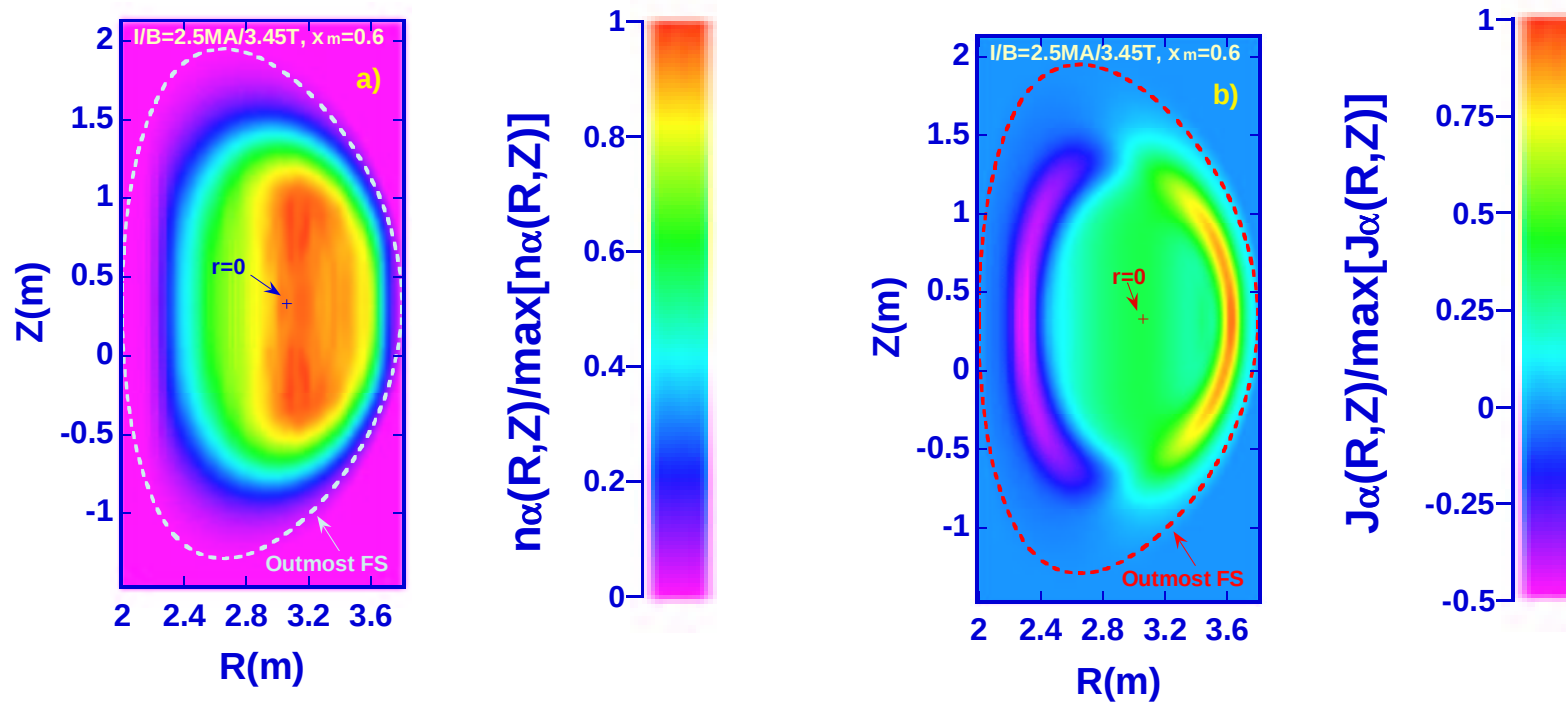
$r_{\max} \sim \min\{r_{\max}\}$ and at $r_{\max} \sim (0.6-0.7)a$

Alpha particle density, bootstrap current and energy deposition



hollow j profiles affect mainly n_α , $P_{\alpha e}$, $P_{\alpha i}$ and less j_α

Alpha particle density and alpha driven current, $I/B=2.5\text{MA}/3.45\text{T}$, $x_m=0.6$

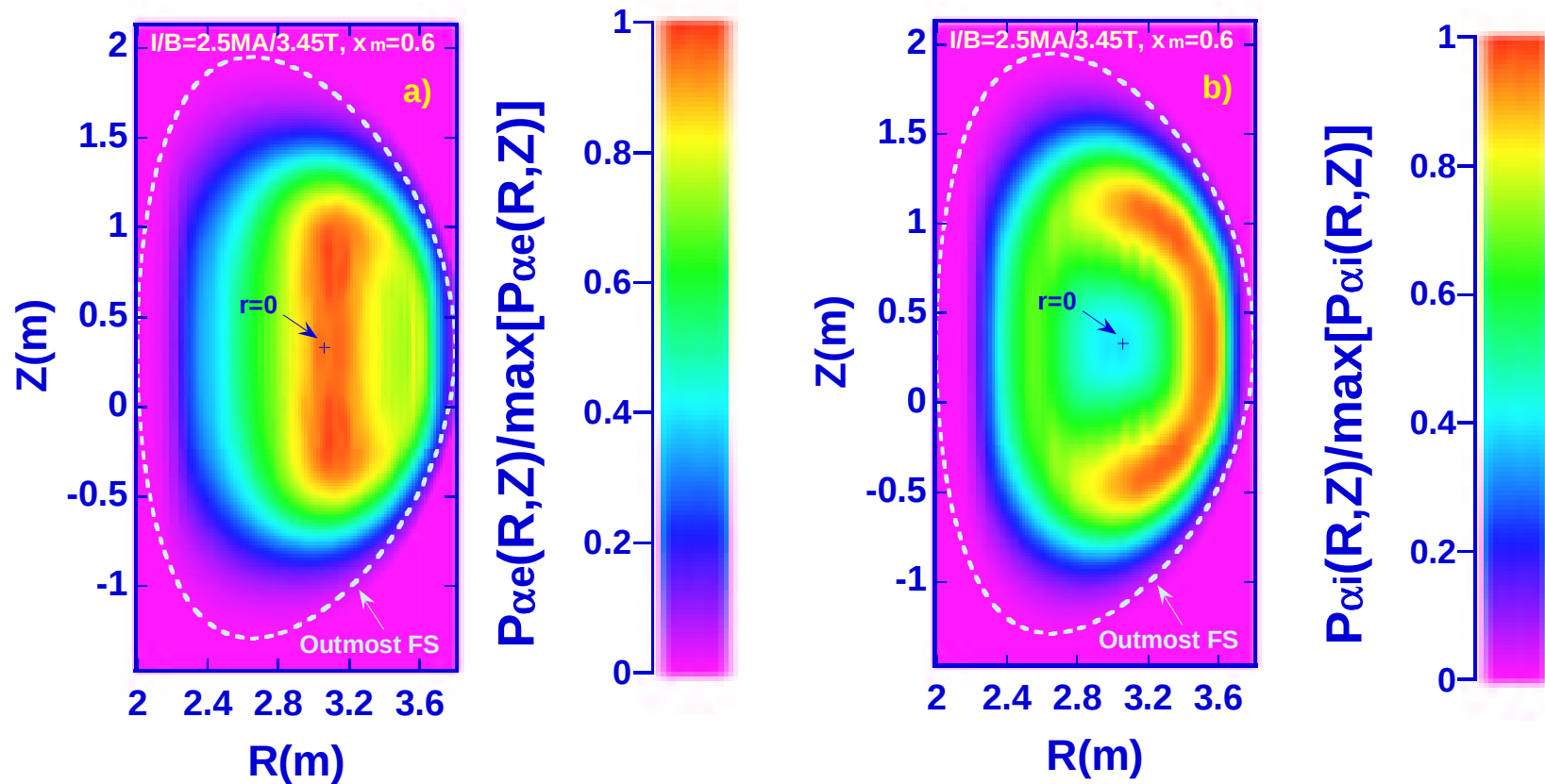


$$j_{\alpha tot} = j_\alpha [1 - (1 - G)Z_\alpha/Z_{eff}]$$

$j_{\alpha tot}$ – includes alpha current and electron reversed current;

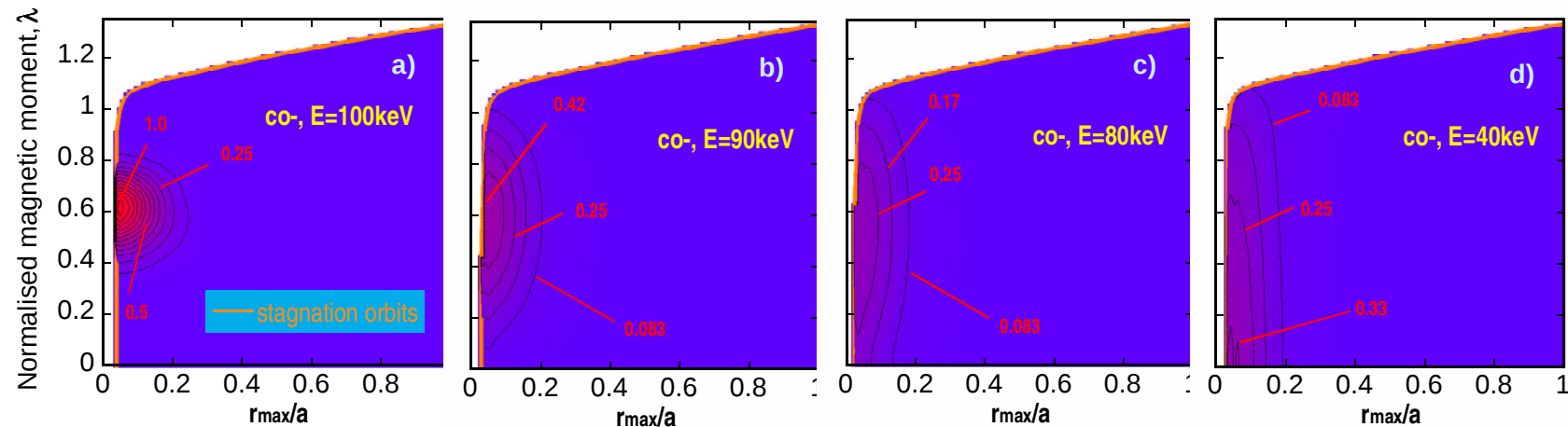
$G \sim (r/R)^{1/2}$ – trapped electron correction

$P_{\alpha e}$ & $P_{\alpha i}$ power depositions, $I/B=2.5\text{MA}/3.45\text{T}$, $x_m=0.6$



$$P_{\alpha e \text{ max}} \sim 10 P_{\alpha i \text{ max}}$$

Distribution function of NBI tritons at monotonic current (on-axis co-injection, $x_m=0$, $I/B=3\text{MA}/3.45\text{T}$)

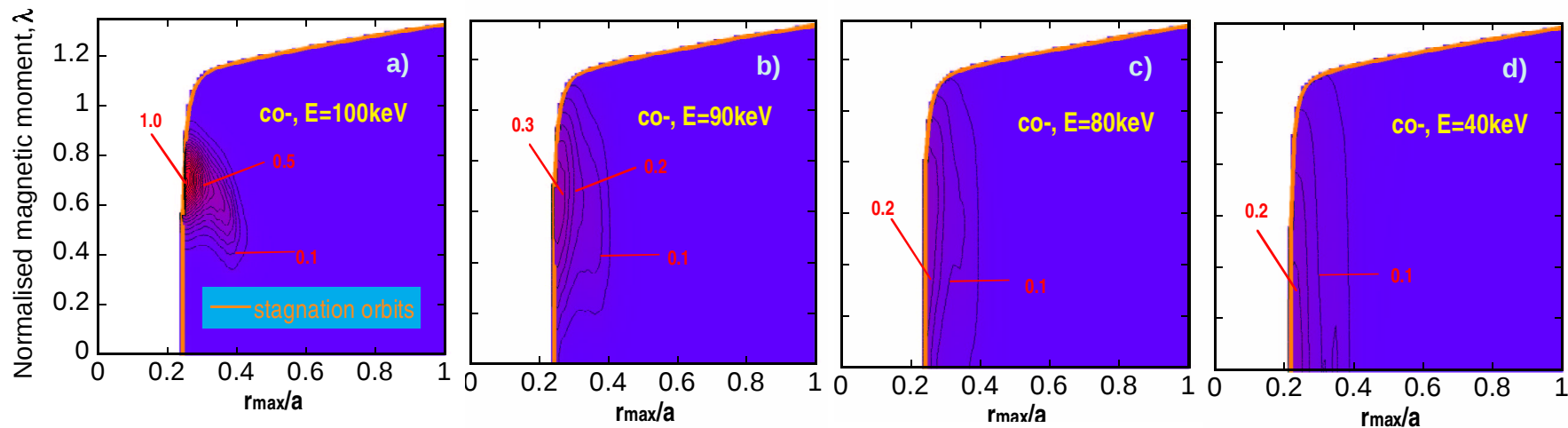


■ f ($40\text{keV} < E < 100\text{keV}$) is localized near the confinement domain boundary corresponding to the stagnation orbits with $0.03 < r/a < 0.1$

reason: beam is rather thin and is injected in mid-plane

➤ at monotonic current the distribution of NBI tritons in plasma cross-section is maximum near magnetic axis

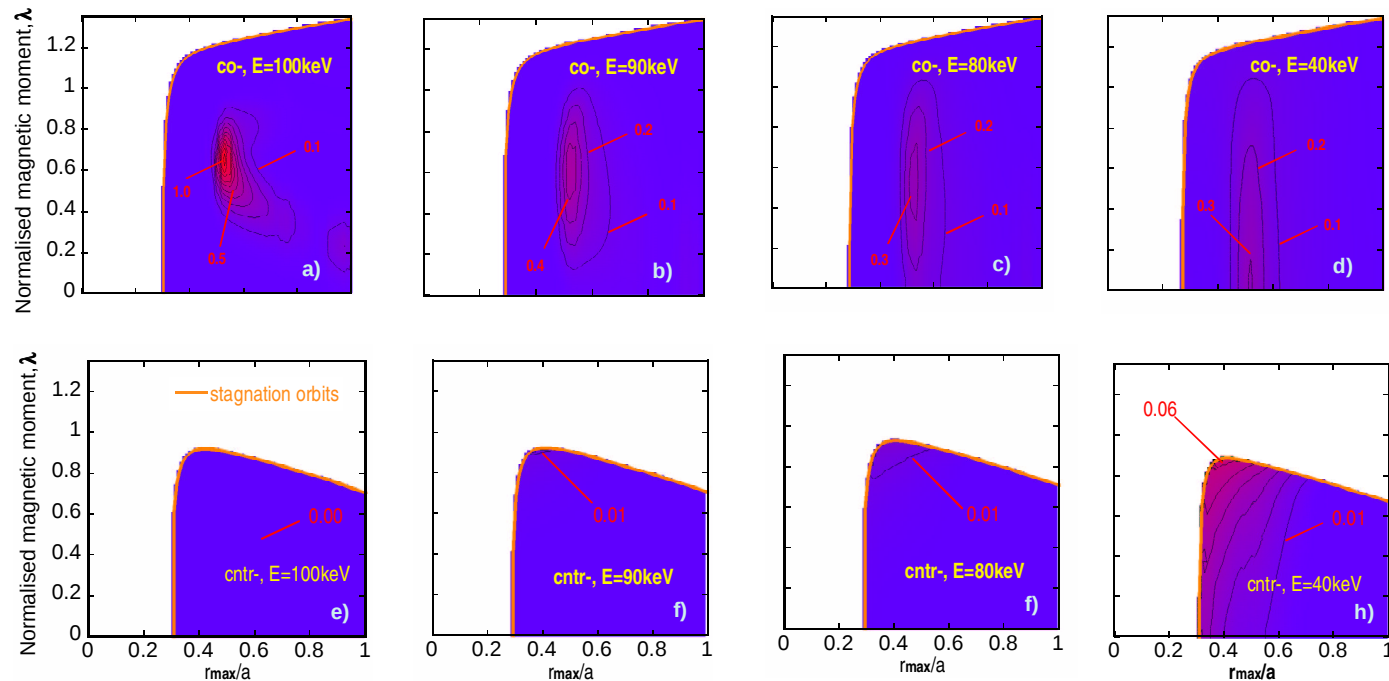
Distribution function of NBI tritons in CH JET equilibrium (on-axis co-injection, $x_m=0.45$, $I/B=3\text{MA}/3.45\text{T}$)



■ f ($40\text{keV} < E < 100\text{keV}$) at $x_m=0.45$ is localized near the confinement domain boundary corresponding to the stagnation orbits with $0.25 < r/a < 0.3$

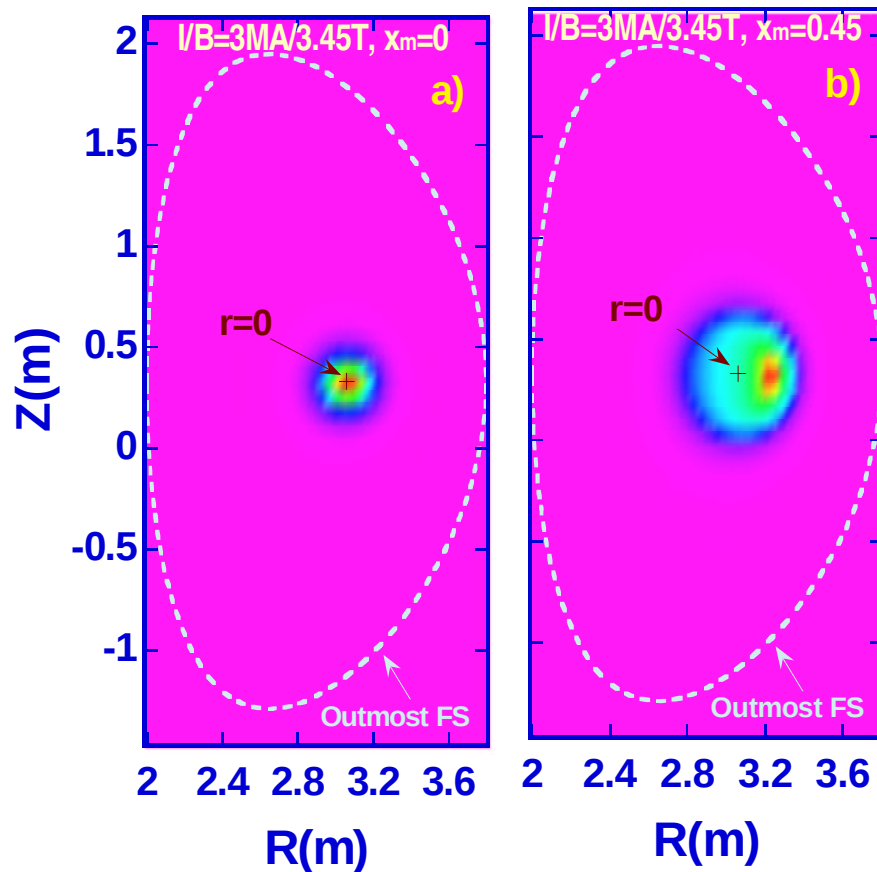
➤ distribution of NBI tritons in plasma cross-section is strongly dependent on poloidal angle with maximum value at $r/a \sim 0.3$ in midplane

Distribution function of off-axis NBI tritons in CH JET equilibrium (co-injection, $x_m=0.45$, $I/B=1\text{MA}/3.45\text{T}$)



- f ($40\text{keV} < E < 100\text{keV}$) at $x_m=0.45$ is localized at $r/a \sim 0.5$
- population of counter-going tritons is small even at $E=40\text{keV}$ in spite of rather strong pitch-angle scattering ($v_{\perp}/v_s \sim 0.5-1$)
- distribution of NBI tritons in plasma cross-section is essentially nonmonotonic with maximum value at $r/a \sim 0.5$

CH effect on NBI triton induced neutron emission



❖ distribution of 14MeV neutron emission induced by NBI tritons in JET is expected to be essentially affected by the current hole

❖ in the case of on-axis injection CH seen to result in i) outward shift ($\sim x_*$) of the neutron emission maximum and ii) broadening of emission profile in plasma cross section

• Summary

- hollow current profiles in JET result in a moderate increase of FO & collisional losses of CFPs if current hole region is rather small, $r_m/a < 0.5$
- at $I > 2\text{MA}$ FO loss fraction of CFPs is $< 30\%$ and collisional loss fraction is $< 10\text{-}12\%$ for DT alphas (with $E > 220\text{keV}$) and $< 20\text{-}25\%$ for DD tritons (with $E > 40\text{keV}$);
maximum alpha particle flux is comparable and even exceeds the neutron flux and maximum alpha loss induced heat load is $\sim 30\text{-}40\%$ of neutron first wall load
- flux of lost CFPs is strongly localised both in poloidal and pitch angle; loss distribution is essentially affected by the current hole
- current hole effect is equivalent to the reduction of total plasma current in accordance with $I \Rightarrow I(1-x_*^{1/2})$
- distribution function of confined CFPs and NBI ions is essentially affected by hollow current profiles $\Rightarrow$ affects fast particle density, bootstrap current and energy deposition profiles, distribution of 14MeV neutron emission induced by NBI tritons