Simplifying strong electronic correlations in uranium: Localized uranium heavy-fermion UM_2Zn_{20} (M=Co,Rh) compounds

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The physical properties including magnetic susceptibility, magnetization, specific heat, and dynamic susceptibility $\chi''(E)$ are reported for single crystals of the cubic UM_2Zn_{20} (M=Co, Rh) materials. Maxima in the thermodynamic data at $T_{max} \sim 10$ K for both compounds and a broad peak in $\chi''(E)$ at 5 K in UCo₂Zn₂₀ of width Γ =5 meV indicate a heavy-fermion state characterized by a Kondo temperature $T_K \sim 20-30$ K arising from weak hybridization of *f*- and conduction-electron states. Anderson impurity model fits to the data in the Kondo limit including crystalline electric-field effects corroborate an ionic-like uranium electronic configuration in UM₂Zn₂₀.

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I. INTRODUCTION

The essential physics of strongly correlated electron materials is deceptively simple: strong on-site Coulomb repulsion of d or f electrons promote localization while orbital overlap with neighboring ligands leads to d- (f-) electron itineracy. While the delicate balance between these two competing tendencies generate novel phenomena in both d-electron systems (e.g., cuprates¹ and ruthenates²) and *f*-electron heavy-fermion compounds,³ the complexity resulting from such competition is generally intractable. This insolubility is particularly evident in the actinide heavyfermion metals,⁴ where even the question of whether to treat the 5f electrons as localized or itinerant has not been answered because their orbitals are spatially extended and dispersive; hence, few exemplary systems have been found on the simpler localized side of the spectrum. As discussed herein, the new strongly correlated UM₂Zn₂₀ (M=Co,Rh) compounds represent a particularly simple limit of this complexity; their crystal chemistry leads to 4*f*-like behavior that allows straightforward insight into their underlying physics.

Uranium-based heavy-fermion (HF) metals share characteristic behavior with rare-earth-based HF materials,⁴⁻⁶ namely that their low-temperature Pauli paramagnetic susceptibility χ_0 and the linear coefficient of specific heat γ = C/T are large, reflecting a strongly renormalized mass of charge carriers that is 100–1000 times the free electron mass. Both χ_0 and γ scale as $1/T_{sf}$, where the characteristic spin fluctuation energy $k_B T_{sf}$ is small ($T_{sf} \sim 1-100$ K) and can be observed directly as the energy of a strongly damped peak in the dynamic susceptibility $\chi''(E)$, measured through inelastic neutron scattering.⁶ This common scaling behavior obscures an important underlying difference: the rare-earth 4f orbitals are highly localized, hybridizing weakly with the conduction electrons, while the uranium 5f orbitals are spatially extended, forming dispersive f bands with strong hybridization with neighboring orbitals. The local-moment character of rare-earth HF compounds allows for detailed fits of the specific heat, magnetic susceptibility, and dynamic susceptibility to the Anderson impurity model (AIM).^{7,8} On the other hand, sharp crystalline electric field (CEF) levels, a signature of the local character of the 4f electrons in rare-earth compounds, are almost never observed in uranium-based compounds in which the fluctuations of the 5f charge configuration make it impossible to characterize the 5f wave functions by welldefined valence states. It is more common in this case to view the heavy-fermion behavior as arising from spin fluctuations in the narrow but dispersive 5f bands. Therefore, essential differences (apart from the scaling laws) might be expected between the detailed behaviors of uranium- and rare-earth-based heavy-fermion materials. The discovery9 of new U-based heavy-fermion compounds UCo2Zn20 and URh₂Zn₂₀ provides a counter example to this expectation. The application of the local-moment (Kondo) limit of the Anderson model within the noncrossing approximation (NCA) gives a good account of the 5f-derived characteristics of these materials. Thus, these UM_2Zn_{20} (M=Co,Rh) materials are model systems with which to understand strongly correlated physics.

II. EXPERIMENTAL DETAILS

Single crystals AX_2Zn_{20} (A=Th,U) were grown in Zn flux.¹⁰ The crystal structure of the AX_2Zn_{20} (A=Th,U) materials was determined to be the cubic $Mg_3Cr_2Al_{18}$ type by means of single crystal x-ray diffraction.¹¹ Magnetic measurements were performed from 2 to 350 K in magnetic fields up to 6 T using a commercial superconducting quantum interference device (SQUID) magnetometer. Specificheat measurements were carried out in a commercial cryostat from 1.8 to 300 K in magnetic fields up to 9 T along the [111] direction for UCo₂Zn₂₀ and in a home-built cryostat



FIG. 1. (Color online) Polyhedral representation of the cubic $(Mg_3Cr_2Al_{18} \text{ type})$ structure of UM_2Zn_{20} (M=Co,Rh). The packing of the U-centered Zn_{16} clusters (blue) and the M-centered Zn_{12} icosahedra (yellow) is emphasized.

from 1.5 to 300 K in magnetic fields up to 15 T along the [110] direction for URh₂Zn₂₀. Inelastic neutron scattering was performed at low temperature (5-6 K) on 20-g powder samples of UCo_2Zn_{20} and $ThCo_2Zn_{20}$ on the high energy chopper spectrometer (HET) at ISIS. To obtain an adequate range of energy transfer $2 < \Delta E < 90$ meV, three incident energies (E_i =23, 60, and 100 meV) were used. The absolute cross-section was established by normalizing to vanadium. Measurements at lower energy transfer ($\Delta E < 2 \text{ meV}$) were carried out on the quasi-elastic neutron spectrometer (QENS) at IPNS. The QENS data have been corrected for absorption, which is significant for total energy (energy transfer plus final energy) below 10 meV, but have not been normalized for the absolute cross section. For both experiments, the data for ThCo2Zn20 have been directly subtracted from the UCo_2Zn_{20} data to obtain the magnetic scattering function $S_{\text{mag}}(\Delta E)$. This method is based on the observation that the total cross section and absorption cross sections of the two materials are essentially identical, so that direct subtraction removes both the nonmagnetic scattering (assumed equal in the two compounds) and the background (empty holder) scattering. In performing this subtraction, it was found that the phonon peaks at 6.96 meV in ThCo₂Zn₂₀ is shifted to 8.25 meV in UCo₂Zn₂₀. This shift undoubtedly reflects the 5fcontribution to the bonding, which increases the phonon energy. This shift was accounted for by fitting the phonon peak to a Gaussian, but shifting its peak energy appropriately when subtracting the Th compound data.

III. RESULTS AND DISCUSSION

The UM_2Zn_{20} (M=Co,Rh) compounds crystallize in a cubic structure in which the U coordination environment comprised exclusively of Zn atoms is nearly spherical (Fig. 1). In this structure,¹² each U atom is surrounded by a Zn_{16} cluster and each M atom by a Zn_{12} cluster, which, given a filled $3d^{10}$ configuration of Zn, should lead to weak hybrid-



FIG. 2. (Color online) Magnetic susceptibility $\chi(T)$ of UCo₂Zn₂₀ (red triangles) and URh₂Zn₂₀ (blue circles) measured in a magnetic field H=0.1 T. (a) Magnetization M vs H between 2 and 40 K of UCo₂Zn₂₀. (b) CEF energy scheme of UM₂Zn₂₀ (M=Co,Rh) discussed in the text. AIM fits (solid lines) to M(H) [(panel (a)] and $\chi(T)$ of UCo₂Zn₂₀ and URh₂Zn₂₀ discussed in the text [M(H) fits of URh₂Zn₂₀ similar to (a)].

ization between the U 5f and ligand electrons of the M atoms. It is this special crystal chemistry that simplifies the 5fphysics of these materials and controls the physical properties of UCo₂Zn₂₀ and URh₂Zn₂₀ that are summarized in Figs. 2 and 3.9 The magnetic susceptibility $\chi(T)$ of the two compounds, displayed in Fig. 2, is typical of heavy-fermion systems with a small characteristic energy scale $(T_K \sim 30 \text{ K})$, proportional to the temperature of the maximum in $\chi(T)$ at $T_{\text{max}}^{\chi} \sim 7$ K (9 K) for UCo₂Zn₂₀ (URh₂Zn₂₀). The Curie-Weiss behavior above 200 K indicates a localized 5f electronic configuration and the (negative) Curie-Weiss temperature θ_{CW} =-65 K (-48 K) for UCo₂Zn₂₀ (URh₂Zn₂₀) is also consistent with $T_K = 20 - 30$ K ($\sim \theta_{CW}/4$). The specific heat, plotted as C/T vs T, of UM₂Zn₂₀ (M=Co,Rh) is shown in Fig. 3(a) and is enhanced below 10 K in both compounds. Subtraction of the specific heat of the nonmagnetic isostructural ThM₂Zn₂₀ (M=Co,Rh) reveals a broad maximum in the 5f contribution $\Delta C/T$ at $T_{\text{max}}^C \sim 4$ K and 6 K [inset of Fig. 3(a)] for M=Co, Rh, respectively. The extrapolated zero-temperature Sommerfeld coefficient is $\gamma \simeq 450$ (300) mJ/mol K^2 for M=Co (Rh). These properties, including the magnetization M(H) [Fig. 2(a)], are reminiscent of uranium magnetic "impurities" embedded in a metallic host described by the Anderson impurity model for a localized fmoment with angular momentum J > 1, where maxima in C(T) and $\chi(T)$ are predicted.¹³ These measurements permit an estimate of the Wilson ratio $\mathcal{R}_W = (\pi^2 R/3C_J)(\chi_0/\gamma)$,



FIG. 3. (Color online) (a) Specific heat C/T vs T of UCo₂Zn₂₀ (red squares) and URh₂Zn₂₀ (blue circles) and for ThCo₂Zn₂₀ (black line) below 20 K. Inset: 5f contribution to the specific heat $\Delta C/T$ vs T, for UCo₂Zn₂₀ (red squares) and URh₂Zn₂₀ (blue circles). (b) 5f specific-heat contribution ΔC vs T of UCo₂Zn₂₀ and URh₂Zn₂₀ in magnetic fields up to 15 T. The solid (zero field) and dashed lines (H=9 T and 15 T for M=Co and Rh, respectively) are fits of the RLM model discussed in the text to the $\Delta C(T)$ data.

where *R* is the gas constant and C_J is the U 5 f^3 Curie constant. Using the values at 2 K for χ_0 and γ , $\mathcal{R}_W \simeq 1.4$ for both compounds.

The momentum-averaged dynamic susceptibility $\chi''(\Delta E)$, determined from the scattering function via $S_{mag} = (n(E)$ $(+1)f^2(Q)\chi''(\Delta E)$, where $f^2(Q)$ is the U 5f form factor and (n(E)+1) is the thermal occupation factor,¹⁴ is plotted vs energy transfer ΔE in Fig. 4. A fit to an inelastic Lorentzian function $\chi''(\Delta E) = \Delta E P(\Delta E)$ with $P(\Delta E) = \chi'(0)(\Gamma / \pi) / [(\Delta E)$ $(-E_0)^2 + \Gamma^2$, with $E_0 = 3$ meV, $\Gamma = 5$ meV, and $\chi'(0) = 3.3$ $\times 10^{-2}$ emu/mol, appears to underestimate the data below $\Delta E < 5$ meV, but fits well at higher energy transfer; it slightly underestimates the measured uniform magnetic susceptibility (Fig. 2). A quasielastic scattering function with $E_0=0, \Gamma=5$ meV, and $\chi'(0)=5.9\times10^{-2}$ emu/mol fits well at low energy, but overestimates the data at high-energy transfer and overestimates the susceptibility. The actual line shape is likely intermediate between these two cases and suggests a Kondo energy scale of order $T_K \sim 20$ K.

Theoretical Anderson impurity model calculations within the NCA^{15–17} affirm a localized uranium electronic configuration in UM₂Zn₂₀(M=Co,Rh) and provide a realistic crystalline electric-field scheme in (semi-) quantitative agreement with experiment. The proposed model of the UM₂Zn₂₀ (M=Co,Rh) compounds is analogous to that applied to Ce-based heavy-fermion compounds in which the localized 4f¹ configuration is allowed to hybridize with a nonmagnetic 4f⁰ state at the Fermi energy E_F to create a Kondo resonance centered at $E_F+k_BT_K$.^{15,16} In the UM₂Zn₂₀ (M=Co,Rh) materials, the two relevant 5f configurations are 5f² and 5f³. Over a wide range of cubic CEF



FIG. 4. (Color online) Dynamic susceptibility χ'' vs energy transfer ΔE of UCo₂Zn₂₀. Main panel: HET data at three incident energies at T=5 K. Inset: data from QENS at T=6 K. Blue line: inelastic scattering function with $E_0=3$ meV, $\Gamma=5$ meV, $\chi'(0)=3.3 \times 10^{-2}$ emu/mol. Red line: quasielastic scattering function with $\Gamma=5$ meV, $\chi'(0)=5.9 \times 10^{-2}$ emu/mol. Black line: AIM prediction as discussed in the text; the overall magnitude has been reduced for comparison with the data.

parameters, the ground state of the J=4, f^2 configuration is a $\tilde{\Gamma}_1$ singlet; for the same parameters, the ten-fold degenerate J=9/2, f^3 state splits into a doublet $\tilde{\Gamma}_6$ ground state and two excited $\tilde{\Gamma}_8$ quartets.¹⁸ Only these relevant states are retained and other excited states are neglected. Therefore, the impurity Hamiltonian hybridizes the f^2 singlet ground state with all states of the f^3 configuration and can be written as

$$H = \sum_{m} \varepsilon_{fm} |m\rangle \langle m| + \sum_{km} \varepsilon_{km} c_{km}^{\dagger} c_{km} + \sum_{km} (V_{km} |m\rangle \langle 0| c_{km} + \text{H.c.}).$$
(1)

Here $|0\rangle$ represents the f^2 singlet and $|m\rangle$ corresponds to the state *m* of the f^3 configuration. The operator c_{km}^{\dagger} creates an electron at the conduction band with the same symmetry as that of $|m\rangle$ and wave vector $k = |\mathbf{k}|$. The parameter ε_{fm} is the energy necessary to take an electron from the Fermi energy and add it to the f^2 configuration, leaving the state $|m\rangle$. The CEF effects are introduced explicitly through the relation $\varepsilon_{fm} = \varepsilon_0 + \Delta_m$, where ε_0 is the energy of the $\tilde{\Gamma}_6$ doublet (taken to be -2 eV) and Δ_m are the CEF excitation energies.

Shown as the solid lines in Figs. 2 and 2(a) are fits to the $\chi(T)$ and M(H) data of UCo₂Zn₂₀ by the Anderson impurity model. Excellent quantitative agreement is obtained with the CEF scheme displayed in Fig. 2(b) in which degenerate $\tilde{\Gamma}_6$ and $\tilde{\Gamma}_8$ states are well separated ($\Delta \sim 200 \text{ meV}$) from the other $\tilde{\Gamma}_8$ quartet. The fit to $\chi(T)$ reproduces the low-temperature peak near the Kondo temperature and the room-temperature susceptibility, but lies slightly above the experimental values at intermediate temperatures, which causes the theoretical M(H) curves for 20 and 40 K to be slightly larger than the experimental ones [Fig. 2(a)]. The two $\tilde{\Gamma}_8$ quartets are characterized by a mixing parameter $\alpha = -0.997$ of two angular momentum basis states belonging to the J=9/2

multiplet.¹⁸ The $\tilde{\Gamma}_1$ singlet of the $5f^2$ configuration hybridizes with this quasisextet CEF state with a hybridization strength Γ =97.6 meV, corresponding to a T_K =22 K [defined as the energy difference between the $\tilde{\Gamma}_1$ singlet and $\tilde{\Gamma}_6$ doublet of Eq. (1)] and a 5*f* occupation number n_f =0.96, consistent with an extreme Kondo limit in which fluctuations of the 5*f* charge configuration are suppressed. Similar results are obtained for URh₂Zn₂₀ (Fig. 2) with nearly identical parameters: α =-0.590, Γ =99.1 meV, and T_K =26 K. Using these same three parameters (ε_0 , α , and Γ) that accurately describe the magnetic properties [Figs. 2 and 2(a)] to calculate the dynamic susceptibility (Fig. 4) of UCo₂Zn₂₀, we find that the energy of the peak (2.64 meV) in $\chi''(\Delta E)$ in the theory is a factor of two smaller than that seen in the experimental data, and the theoretical width is too small by a similar factor.

Since the peak in specific heat is reminiscent of Kondolike behavior, the resonance level model¹⁹ (RLM) is used to describe the data, which has been shown to provide a reasonable description of a number of heavy-fermion metals and compares well with more exact treatments.^{13,20} In this model, the physical properties in an applied field are calculated assuming a Lorentzian density of states of width δ $(\sim k_B T_K)$ for arbitrary angular momentum J using the parameters δ , Landé g factor (=8/11), and an overall scale factor a. As displayed in Fig. 3(b), qualitative agreement is found between the 5f contribution to the specific heat of UCo_2Zn_{20} and the RLM with the parameters $\delta = 9$ K, J = 5/2, and a =0.8. Using these same parameters for UCo_2Zn_{20} , the calculated zero-temperature magnetic susceptibility χ_0 =0.031 emu/mol is in qualitative agreement with the experimental value (Fig. 2); moreover, the Wilson ratio¹³ \mathcal{R}_W $=(\pi^2 k_B^2 \chi(0)/\mu_{eff}^2 \gamma)[1+1/2J]=6/5$ is consistent with such a quasisextet CEF state. The field evolution of $\Delta C(T)$ is in rough agreement with the RLM predictions [Fig. 3(b)]; the experimentally observed decrease in magnitude of $\Delta C(T)$ may be a consequence of antiferromagnetic correlations, which would be suppressed in field. The 5f contribution to the entropy at 20 K is $S_{5f}(20 \text{ K}) = \int^T (\Delta C/T) dT$ ~4.0(2) J/mol K for UCo₂Zn₂₀, less than the $R \ln(6)$ expected for the quasisextet CEF state. However, the full entropy of this sixfold degenerate state is only expected to be released below ~ 80 K;¹³ unfortunately, the difference in the phonon spectra between UCo₂Zn₂₀ and ThCo₂Zn₂₀ observed in the neutron scattering spectrum [not shown] precludes a more accurate estimate of S_{5f} above ~20 K. Similar results are obtained for URh_2Zn_{20} using the RLM parameters δ =11 K, J=5/2, and a=0.9 [Fig. 3(b)].

It is particularly striking that these UM_2Zn_{20} (M = Co, Rh) compounds can be described in detail as localized heavy-fermion materials. While uranium-based semiconduc-

tors, such as U₃Sb₄Ni₃, show local-moment behavior, as evidenced by well-defined crystal-field levels in neutron scattering,²¹ this is rarely the case for uranium intermetallic compounds where a featureless inelastic line is typically observed²² in the dynamic susceptibility. In the case of UM_2Zn_{20} (M=Co, Rh), the maxima in $\chi(T)$, C(T), and $\chi''(\Delta E)$ are well described by the AIM calculations and are consistent with a heavy-fermion state characterized by a Kondo temperature $T_K \sim 20-30$ K arising from weak hybridization of conduction-electron states with a localmoment CEF ground state. The fact that virtually identical behavior is observed in the isostructural YbM₂Zn₂₀ (M =Fe,Ru) heavy-fermion compounds,²³ which are unquestionably local-moment systems, reinforces the observation of local-moment behavior in these UM_2Zn_{20} (M=Co,Rh) compounds. Furthermore, similar structural characteristics in U₃Pd₂₀Si₆, whereby both U atoms in two inequivalent sites are surrounded by cages of Pd and Si atoms, presumably lead to a localized uranium configuration as evidenced by the crystal-field excitation at 23 meV (Ref. 24) and localized long-range magnetic order at low temperature. The minimal overlap of the U ions with neighboring Zn ligands in these UM₂Zn₂₀ heavy-fermion metals creates an ideal system for thoroughly investigating the Anderson impurity model in actinide compounds.

IV. CONCLUSIONS

Measurements of magnetic susceptibility, magnetization, specific heat, and dynamic susceptibility of single crystals of UM_2Zn_{20} (M=Co,Rh) are reported. The maximum in the magnetic susceptibility and Sommerfeld coefficient at $T_{max} \sim 10$ K for both compounds and a broad peak in the dynamic susceptibility at 5 K in UCo₂Zn₂₀ of width Γ =5 meV suggest a heavy-fermion state characterized by a Kondo temperature $T_K \sim 20-30$ K arising from weak hybridization of *f*- and conduction-electron states due to isolation of the uranium and transition metal atoms in separate Zn cages. Anderson impurity model fits to the data in the Kondo limit including crystalline electric field effects corroborate an ionic-like uranium electronic configuration in these UM_2Zn_{20} materials.

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