

# charged Lepton Flavor Violation

A biased case study that *isn't* supersymmetry

Flip Tanedo

UCIRVINE

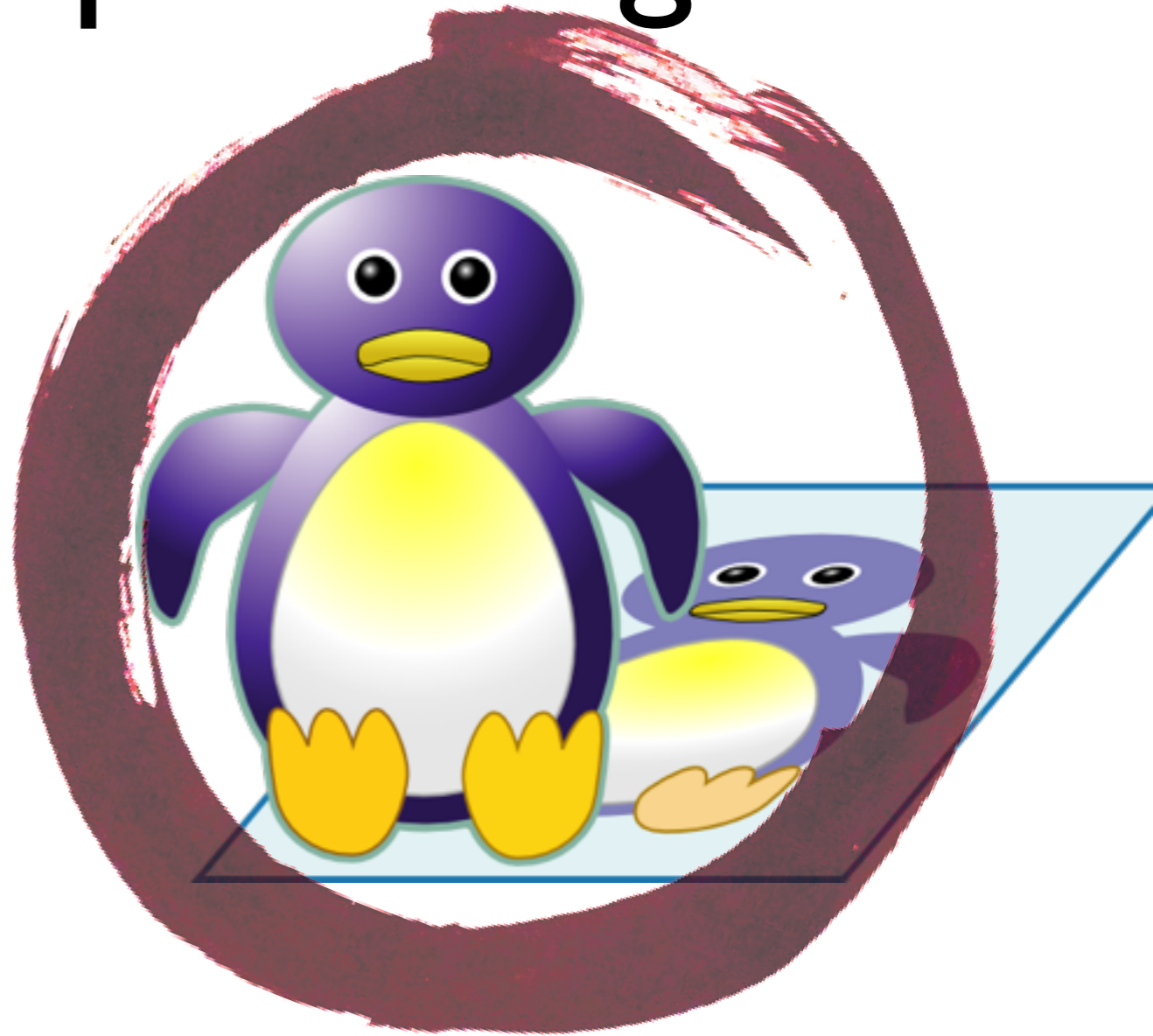
International Workshop on Charged Lepton Flavor Violation  
UC Irvine 13 May 2014

apologies: no references in this talk; see your favorite theorists

# Case Study: Warped Penguins



SUSY  
not today



Flavor in Warped Extra Dimensions  
& why you should care

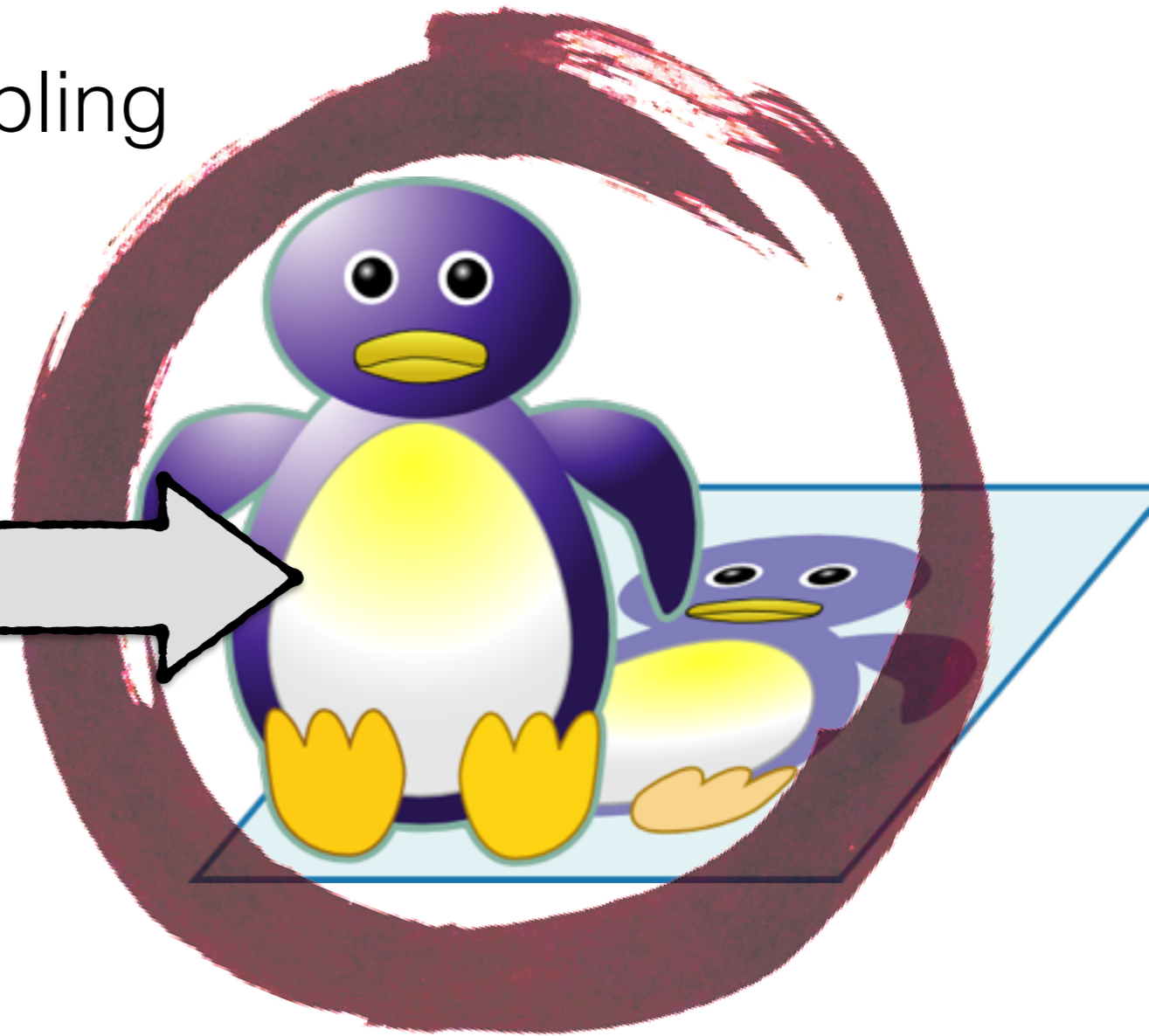
strong coupling

... XD in disguise



SUSY

a theory **with** flavor

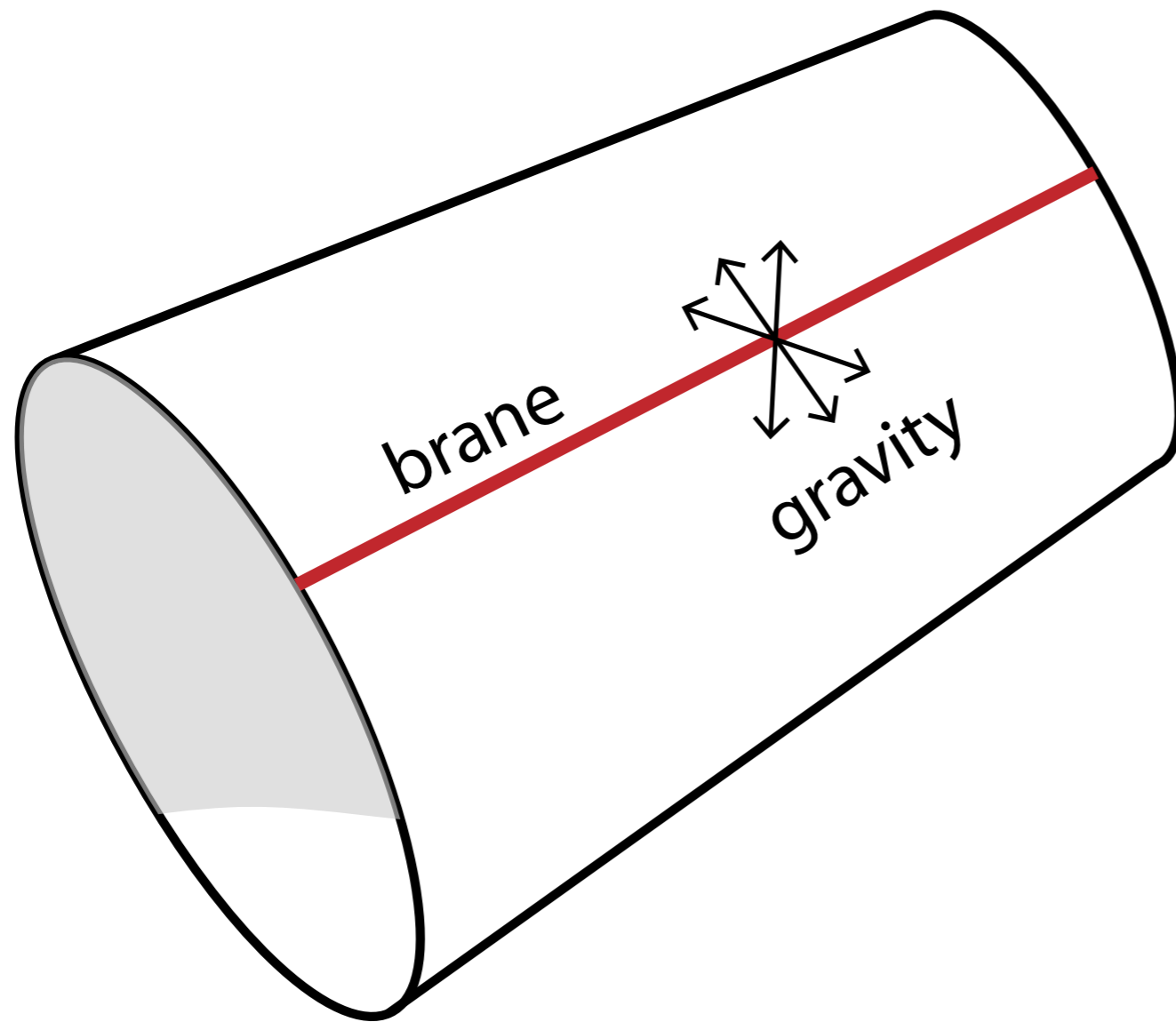


Extra Dimensions

a theory **of** flavor

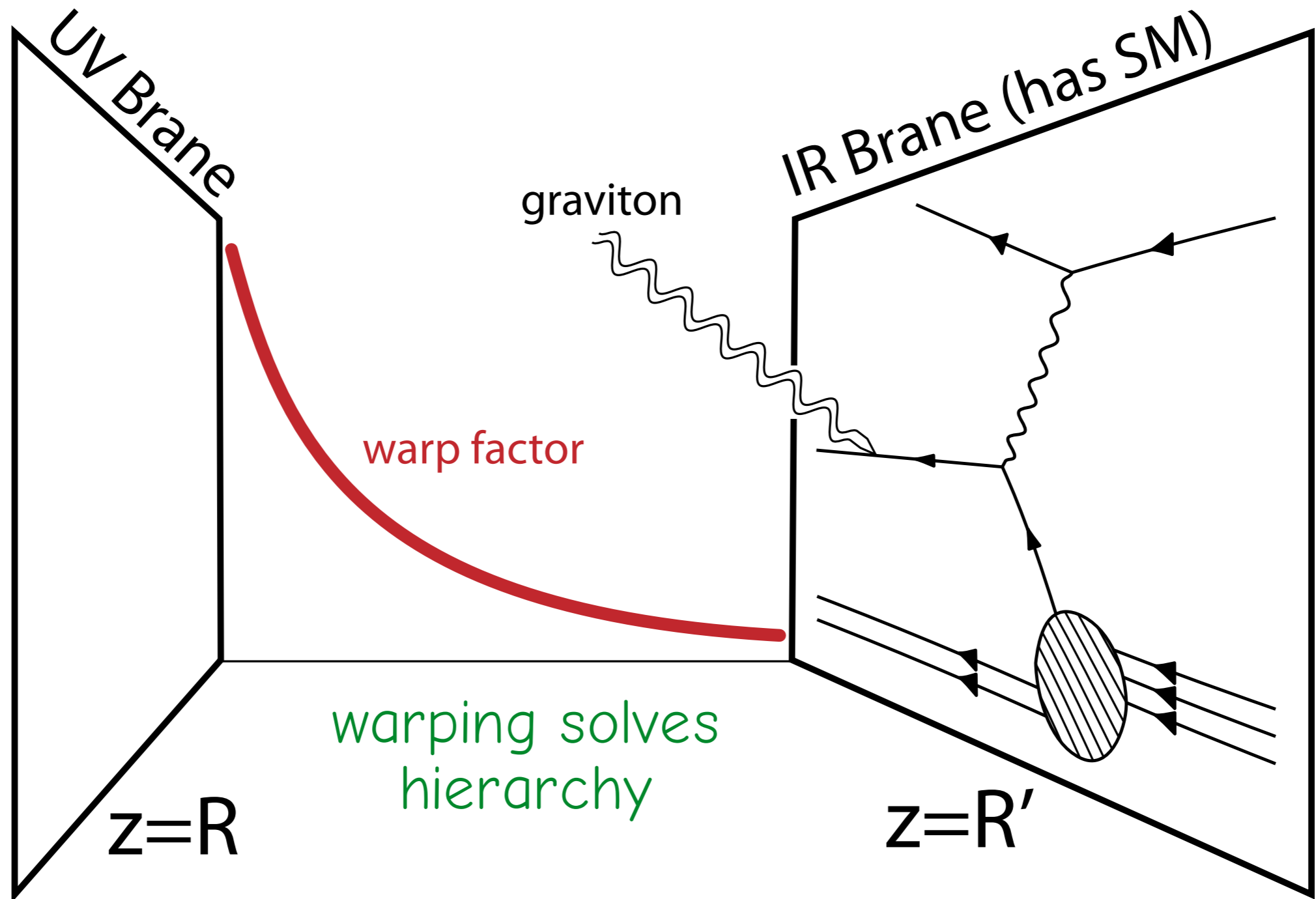
not “a model,” a theory paradigm for flavor

# Extra Dimension

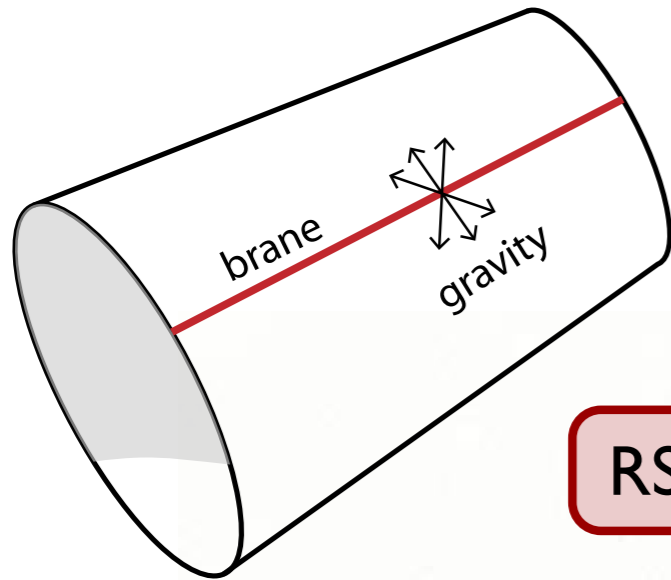


“bulk” particles have  
Kaluza-Klein excitations

# “Old” Randall-Sundrum



# Evolution of RS

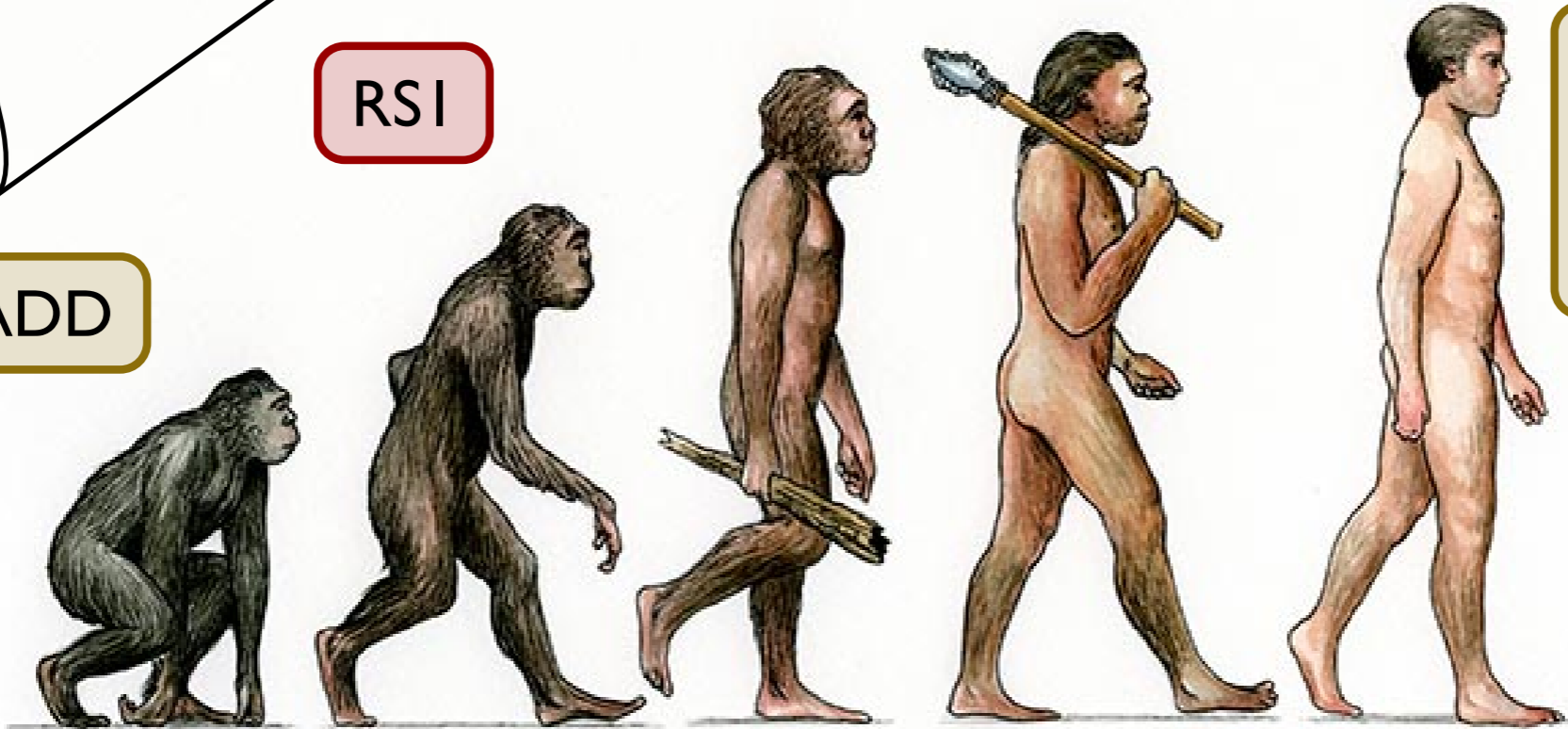


RSI with bulk fields  
Gauge fermions

Realistic RSI  
Custodial protection

RSI

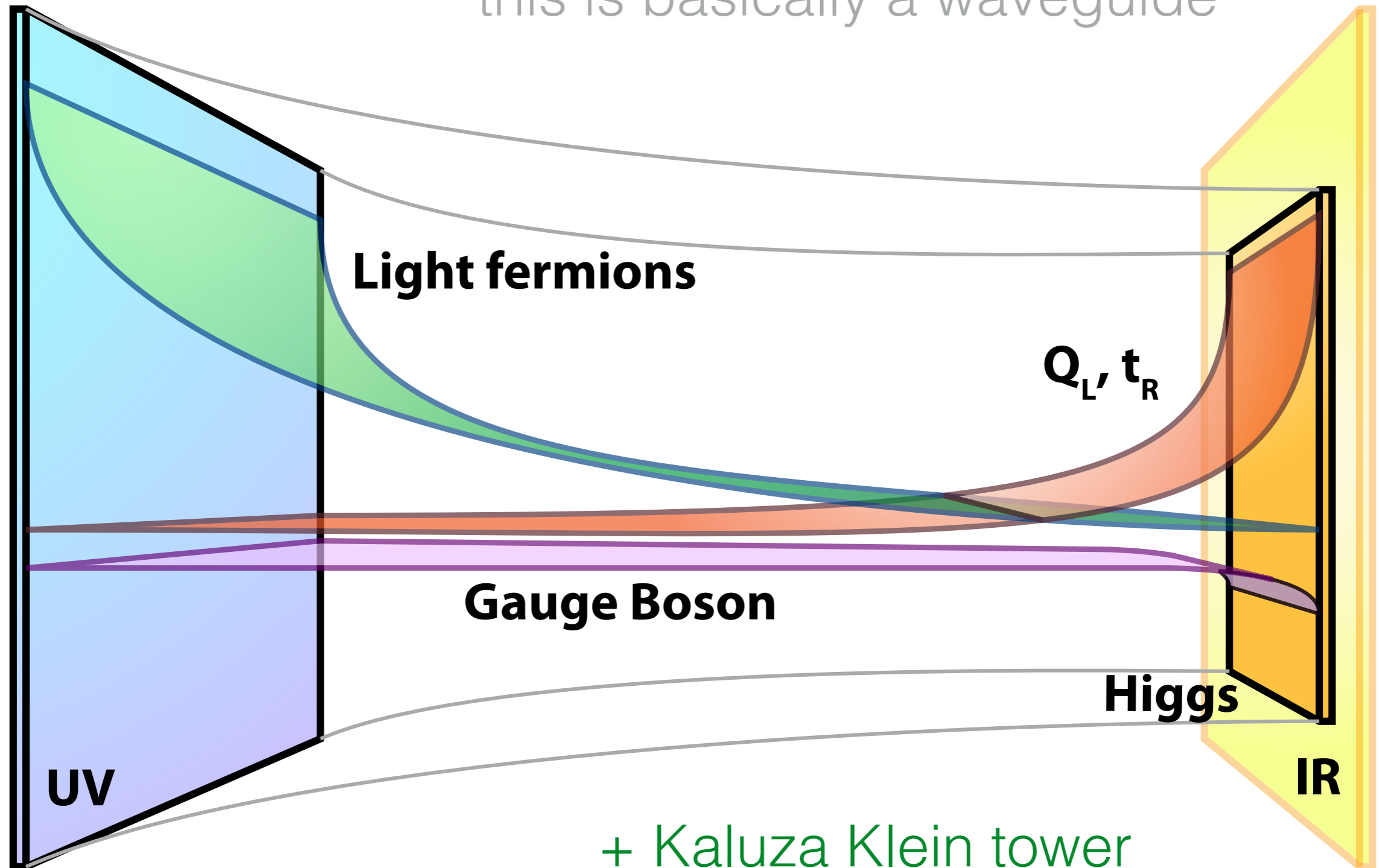
ADD



RSI+  
Little Higgs, Higgs-less, gaugephobic

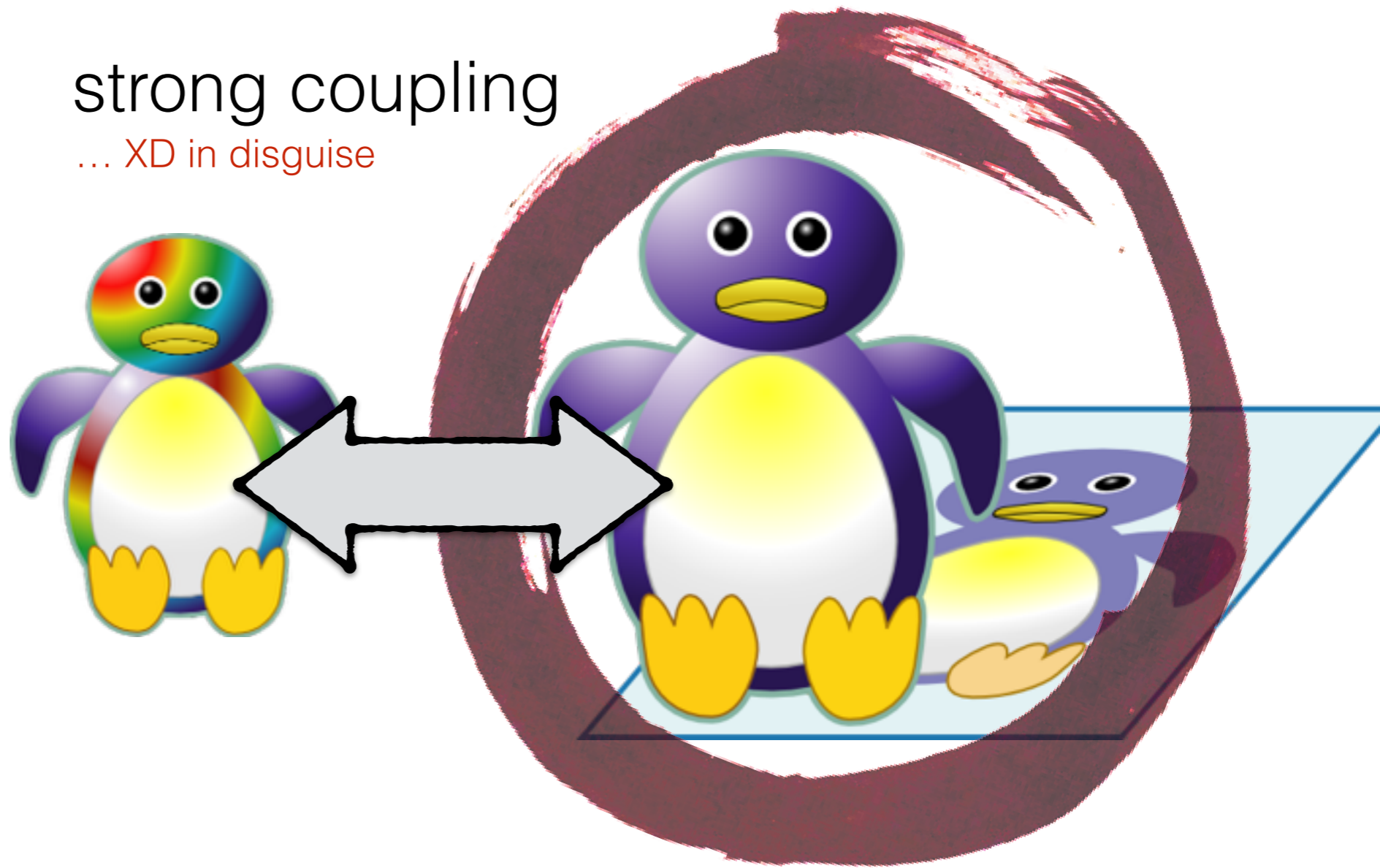
# Realistic Randall-Sundrum

this is basically a waveguide



strong coupling

... XD in disguise



Extra Dimensions  
a theory **of** flavor



# holographic principle

I have a theory of XD...

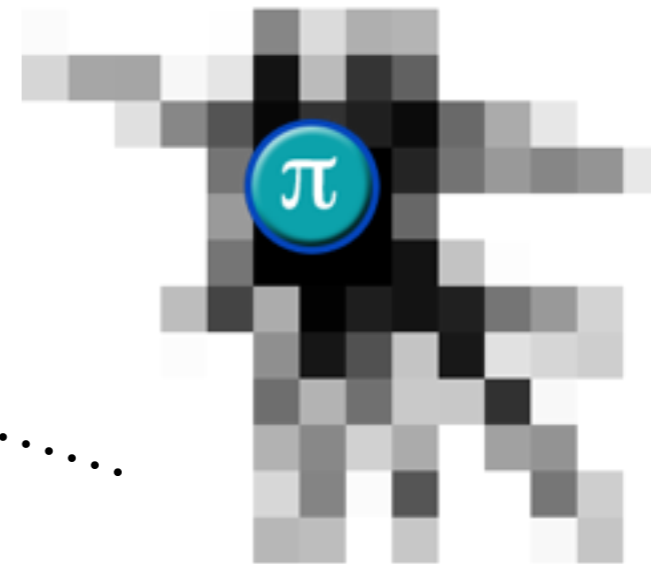
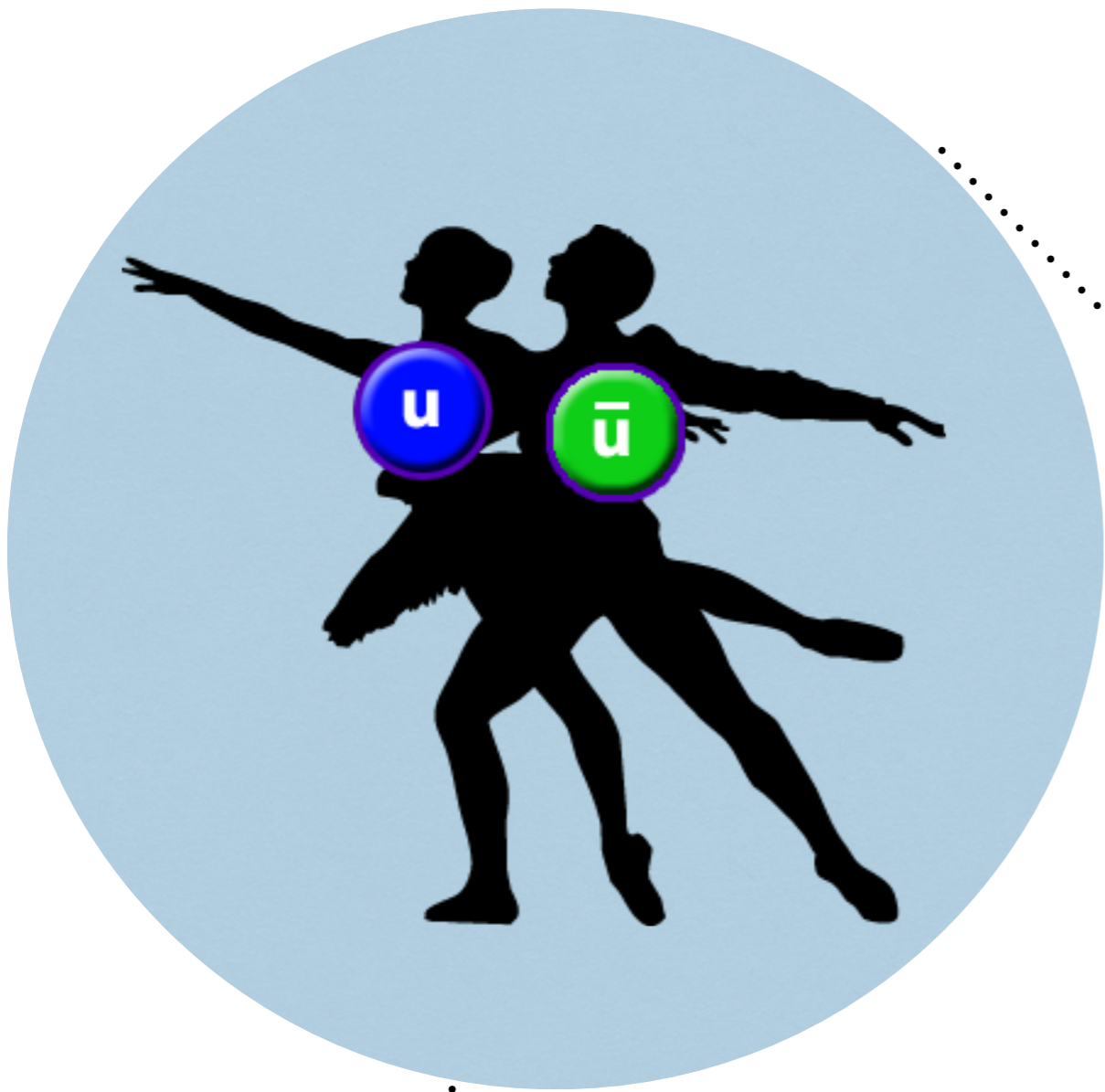
Tim

well, you have a tower  
of [KK] resonances...

Bill

Ok. What does it predict?

We already found that.  
It's called QCD.



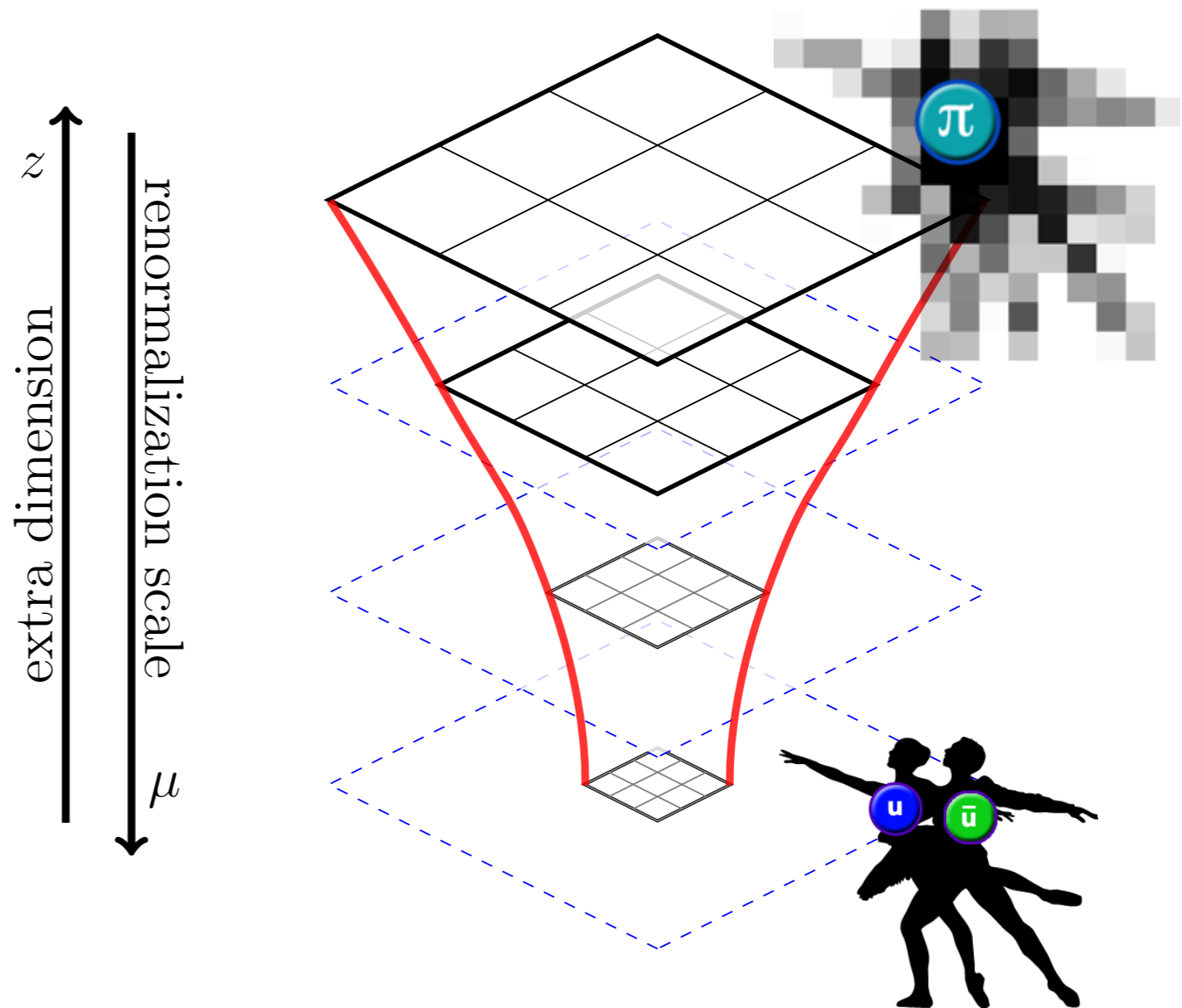
# RS = compositeness

Gravitational background enforces scale symmetry

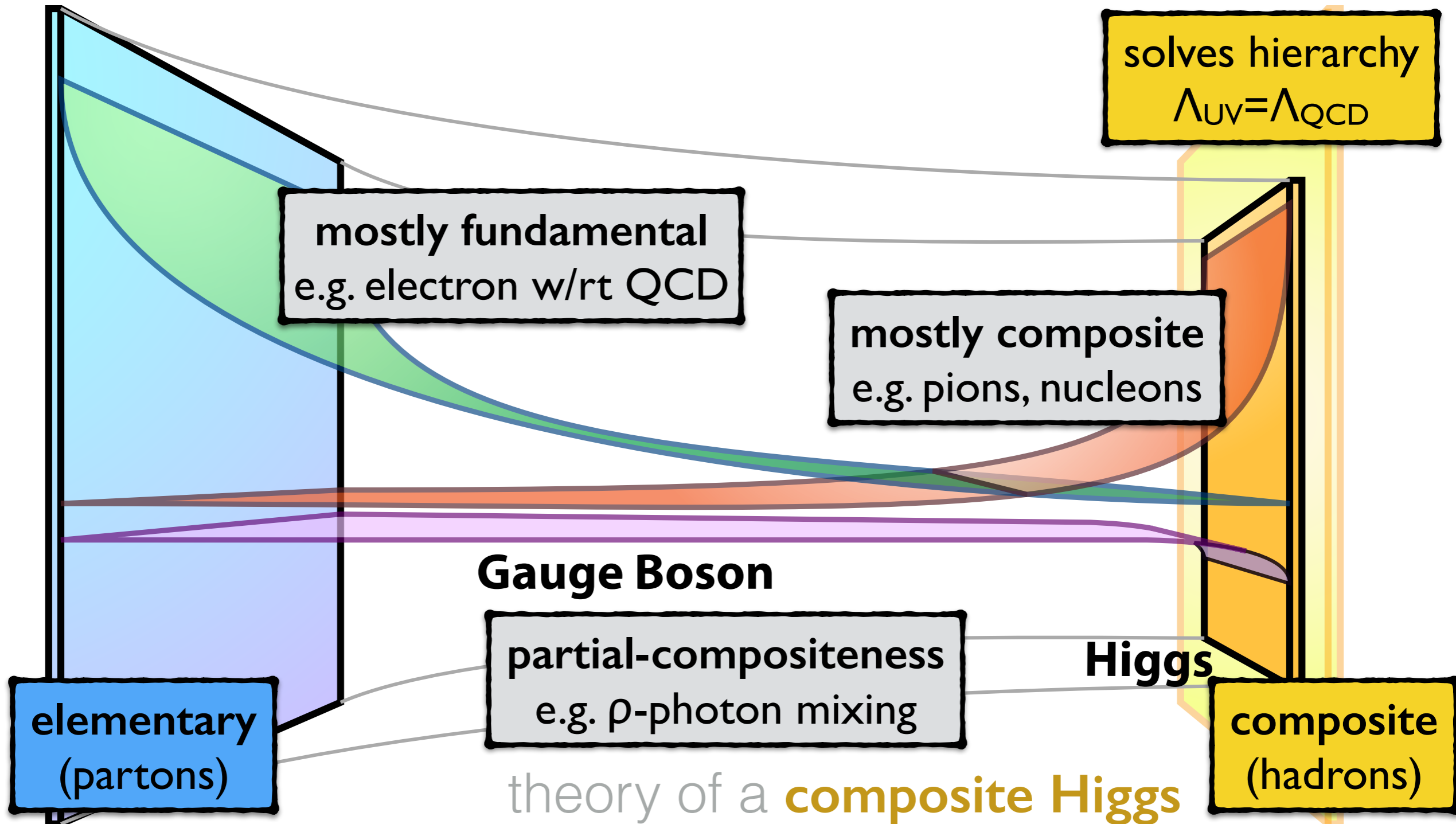
In this way, the 5th dimension *geometerizes* RG scaling and interpolates between “partons” and “hadrons”

so: RS is shorthand for **composite Higgs** + all the junk that comes along with it  
you don't have to “believe” in 5D

$$ds^2 = \left( \frac{R}{z} \right)^2 (dx^\mu dx_\mu - dz^2)$$



# RS = compositeness



The diagram shows a vertical cross-section of a warped extra dimension. The vertical axis represents energy, with 'UV' (ultraviolet) at the top and 'IR' (infrared) at the bottom. Several energy levels are shown as horizontal bands of different colors: a light blue band at the top, a light green band below it, a light purple band, a light orange band, and a light yellow band at the bottom. The bands are wider at the UV end and narrower at the IR end. The text 'RS is a shorthand for strong dynamics beyond the SM' is overlaid on the diagram. Faint labels 'Light fermions' and 'Gauge Boson' are placed near the green and purple bands respectively. The label 'Higgs' is placed near the orange band, and 'Q<sub>t</sub>' is placed near the purple band.

**RS is a shorthand  
for strong dynamics  
beyond the SM**

UV

IR

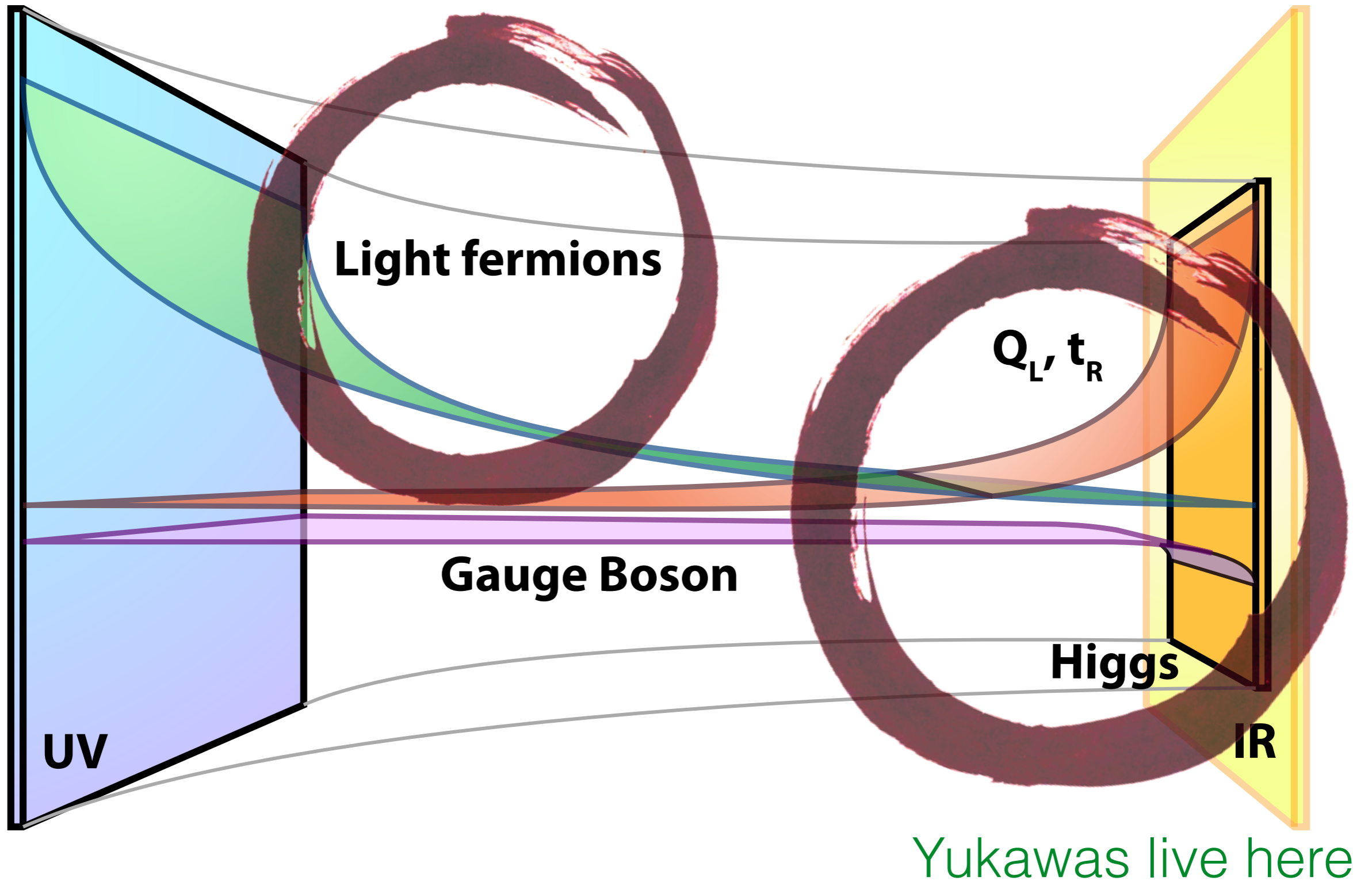
Light fermions

Gauge Boson

Higgs

Q<sub>t</sub>

# RS as a theory of flavor



# Anarchic Flavor

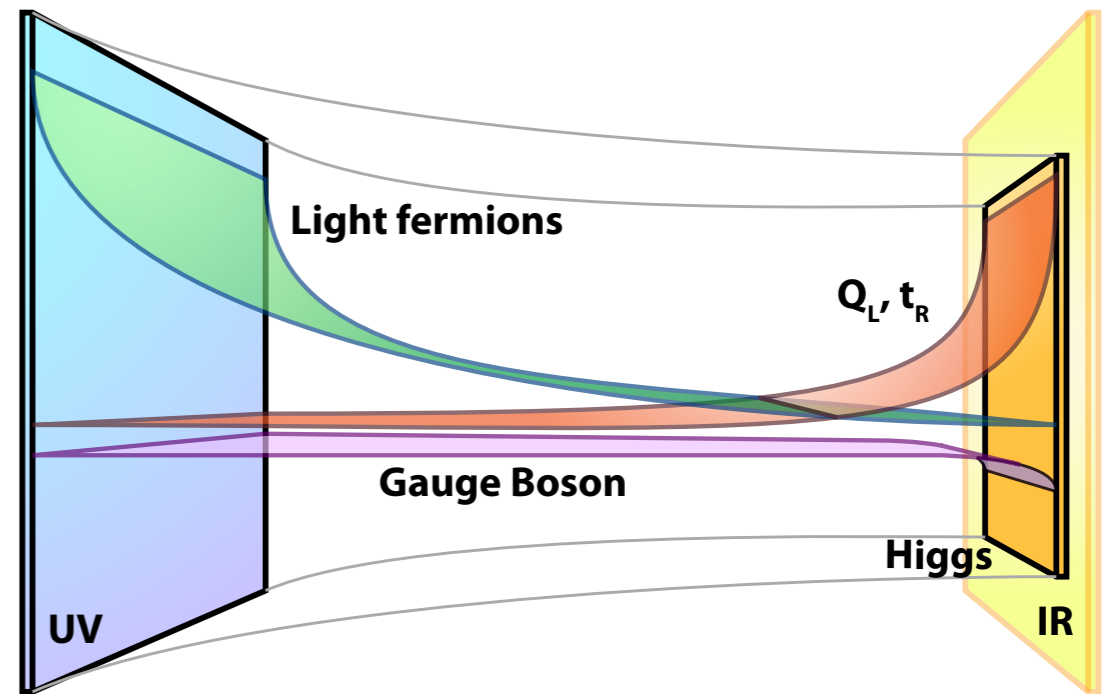
- Assume 5D Yukawas are **anarchic** (no hierarchy)

- SM Yukawas appear hierarchic due to overlaps:

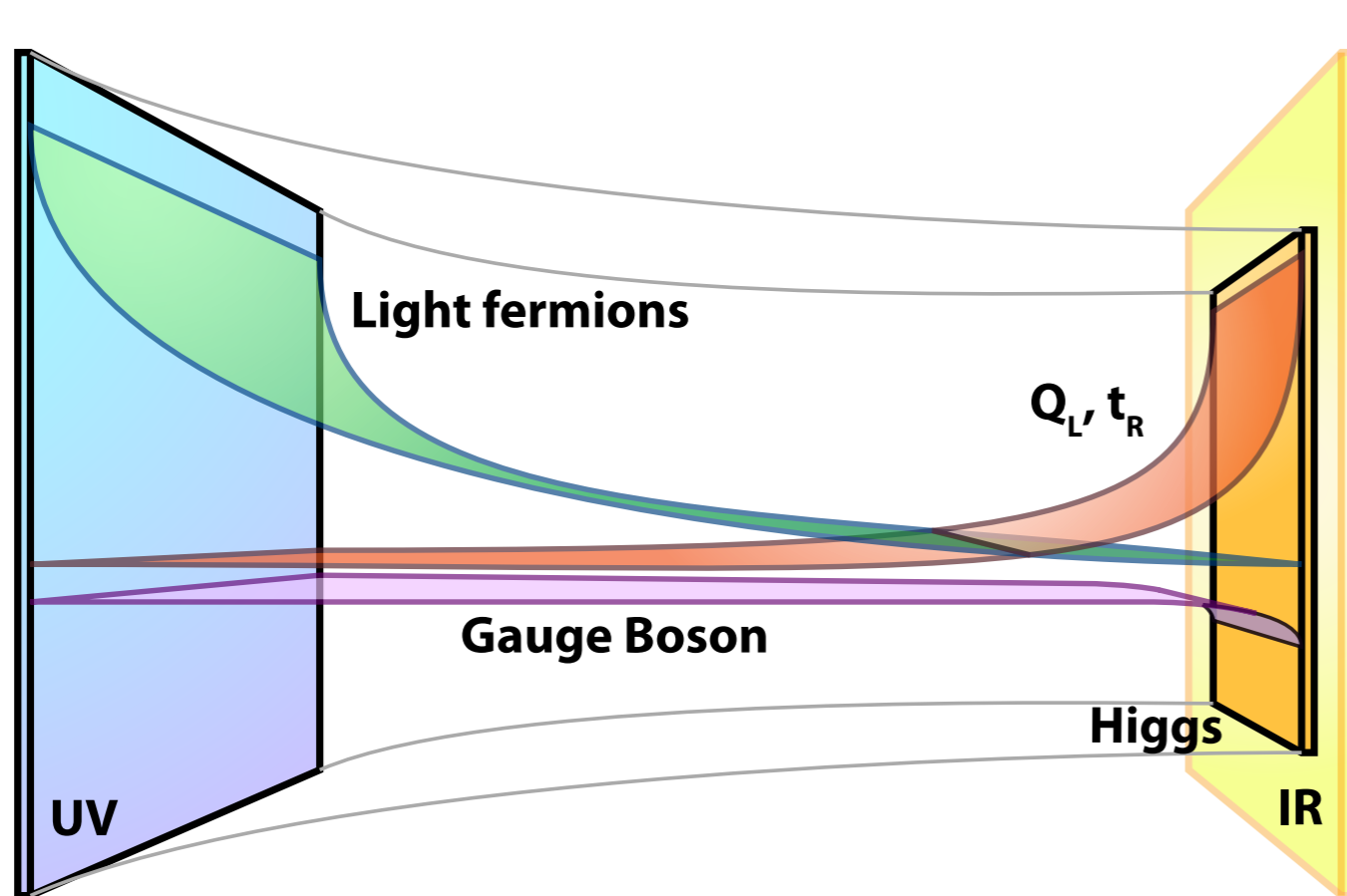
4D  $top_L$ - $top_R$ -Higgs coupling depends on the 5D Yukawa and the wavefunction overlap

Composite Higgs parlance: “conformal flavor” or “flavor from renormalization”

- Leptons are light because they’re ‘fundamental’
- Can even explain neutrino masses and mixing



# Anarchic Flavor



5D parameter  
 $O(1)$  and anarchic

$$y_{ij}^{(4D)} = f_i Y_{ij} f_j$$

$f_i$  encodes wavefunction  
 at the IR brane  
 i.e. degree of compositeness

Other parameter:  $M_{KK}$ , related to size of XD  
 smaller XD  $\rightarrow$  larger KK scale  $\rightarrow$  decoupled KK excitations



# Sources of LFV

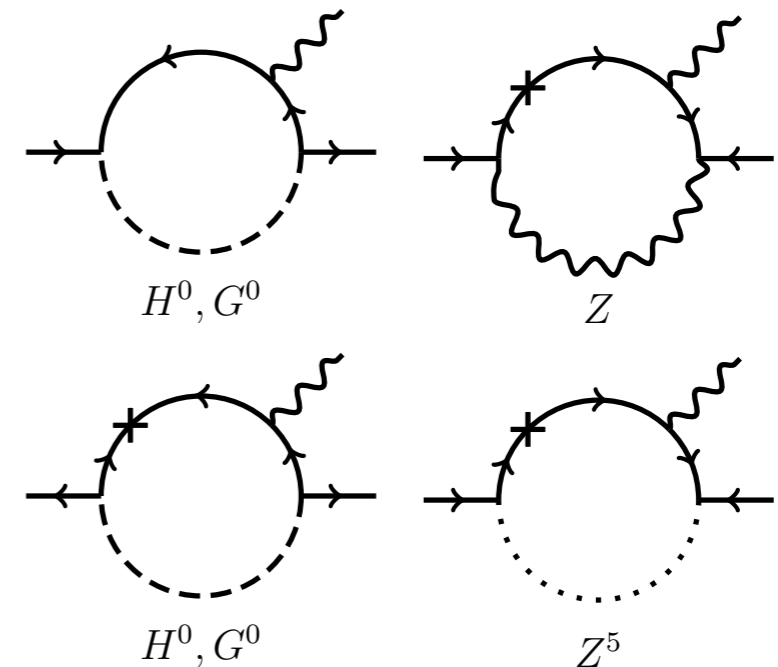
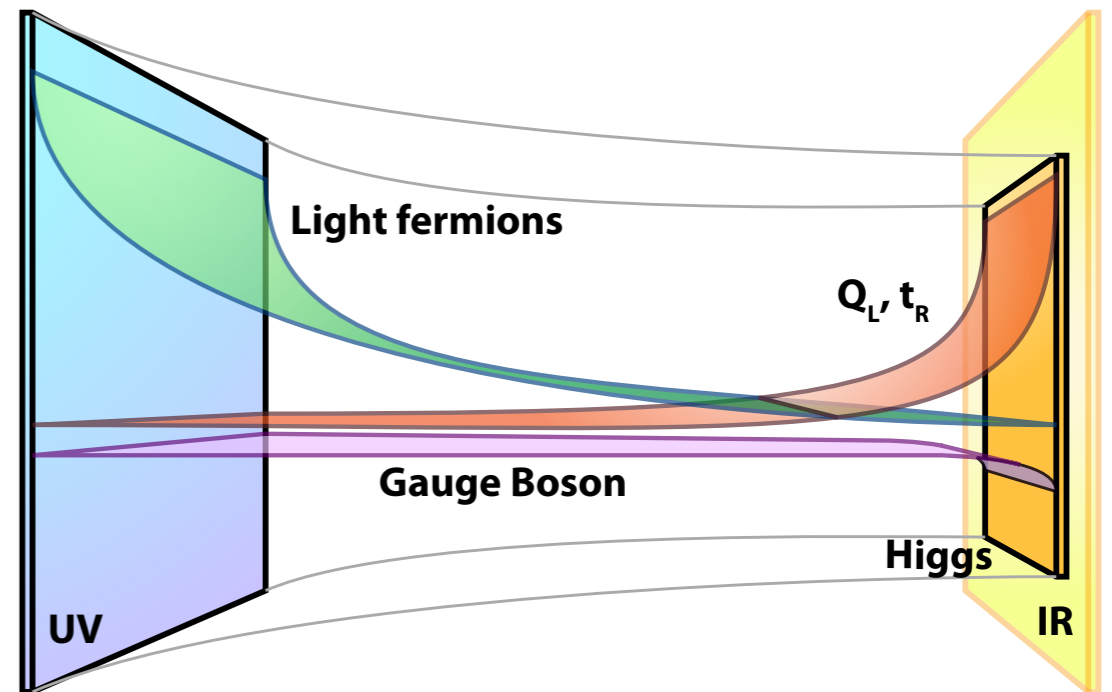
- **Tree level LFV**

Gauge bosons resonances  
 e.g.  $Z'$  (Kaluza-Klein  $Z$  boson)  
 Breaks plane wave orthogonality  
 (analog of Fourier transform)

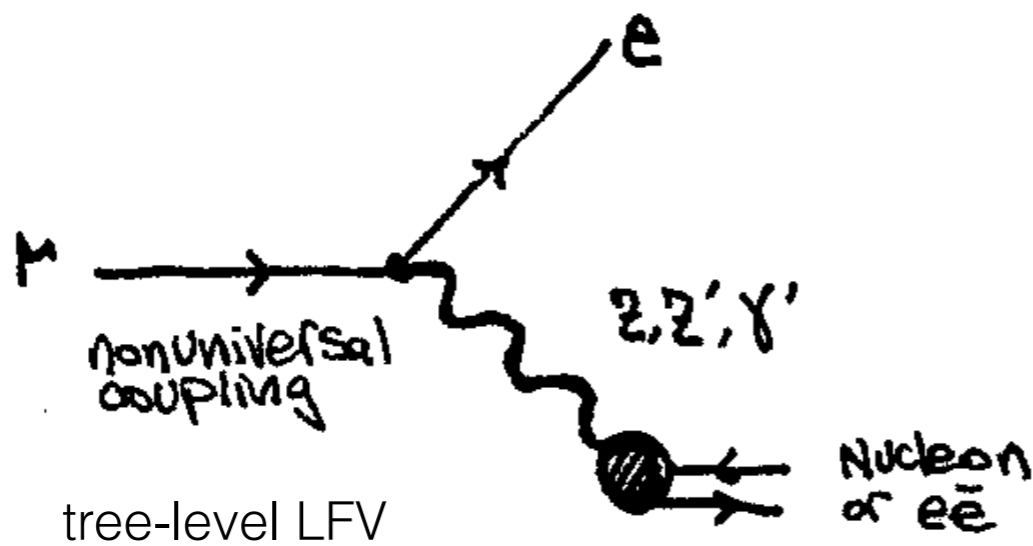
Even SM  $Z$  has small FCNC  
 EWSB affects boundary conditions

- **Loop level LFV**

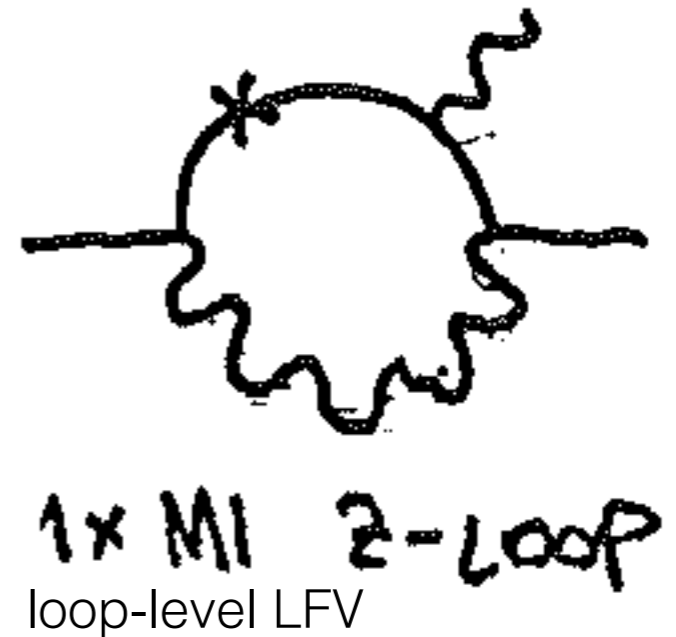
Penguin diagrams  
 SM fields + 5D excitations



# Tree vs Loop



Calculate as usual

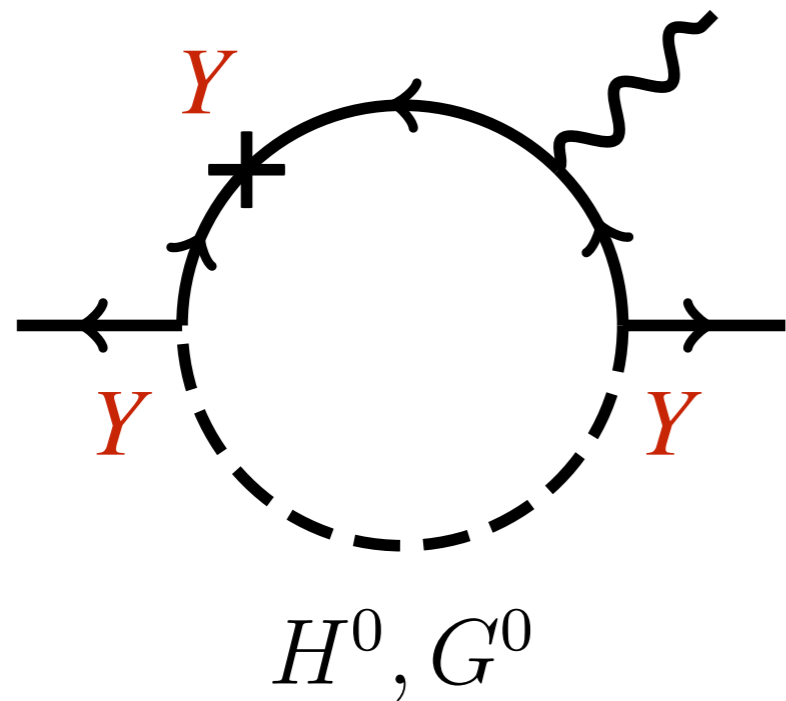


much more subtle!

- finite? **yes!**
- 5D covariance? **yes!**

... worth a Ph.D

# Tree vs Loop



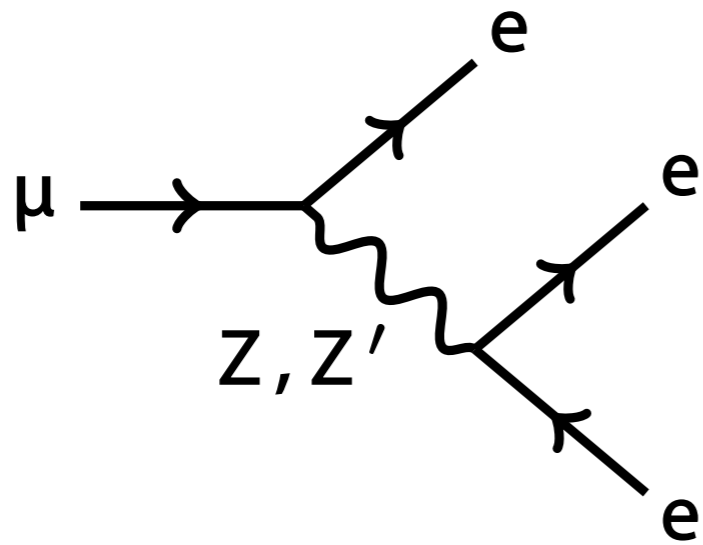
$$\sim \left( \frac{1}{M_{\text{KK}}} \right)^2 f_{\mu_L} Y^3 f_{e_R}$$

$$\sim \left( \frac{Y}{M_{\text{KK}}} \right)^2 m_\mu$$

This makes sense: positive power of coupling,  
negative power of the 5D scale

Bounds? Can either make 5D Yukawa small or make KK scale heavy.

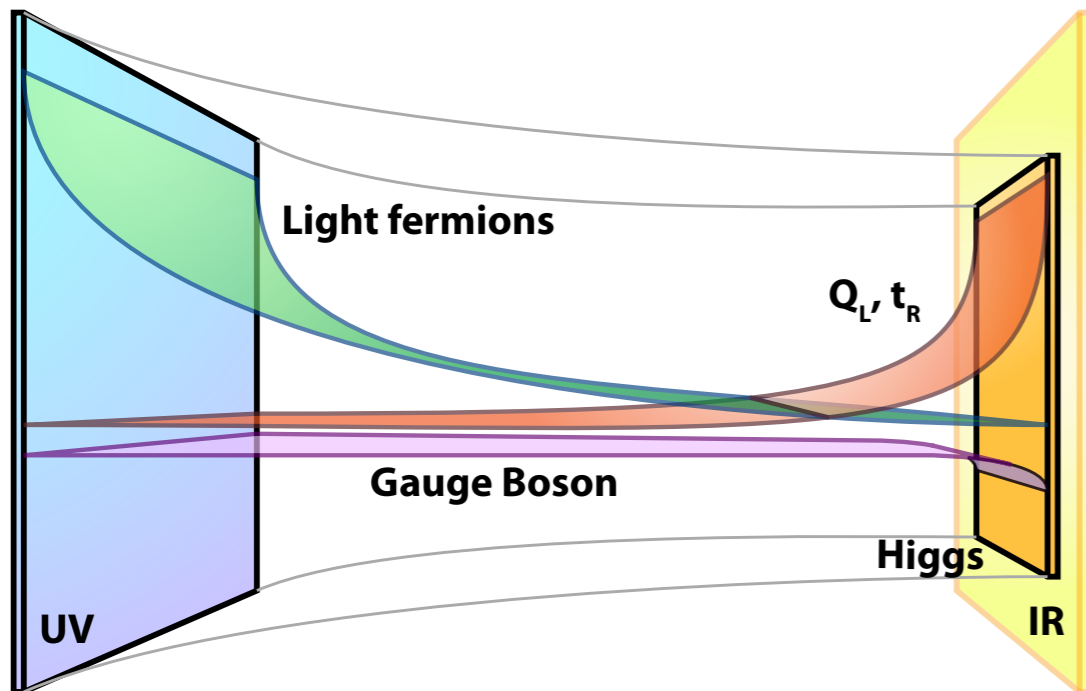
# Tree vs Loop



$$\sim \left( \frac{1}{M_{\text{KK}}} \right)^2 \left( \frac{1}{Y} \right)$$

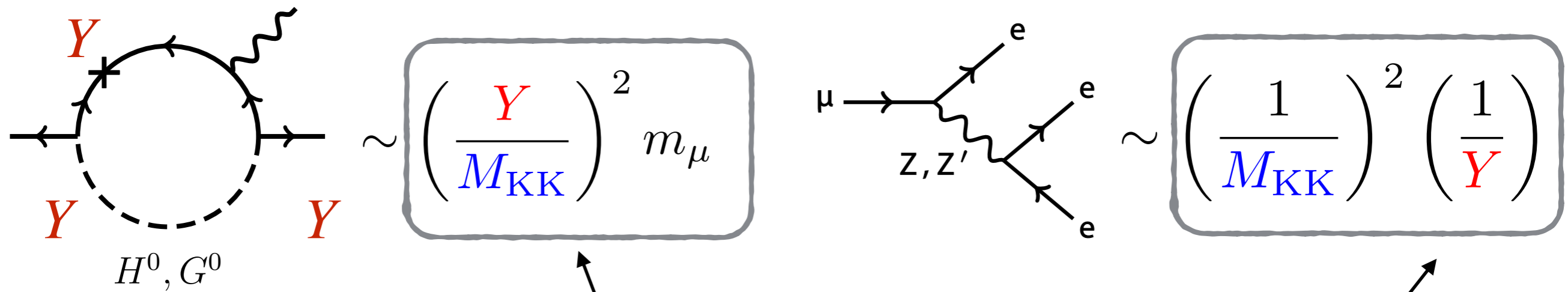
Inverse power of  $Y$

increase  $Y$ , push profile to UV  
less overlap with FCNC part of  $Z$



$$y_{ij}^{(4D)} = f_i Y_{ij} f_j$$

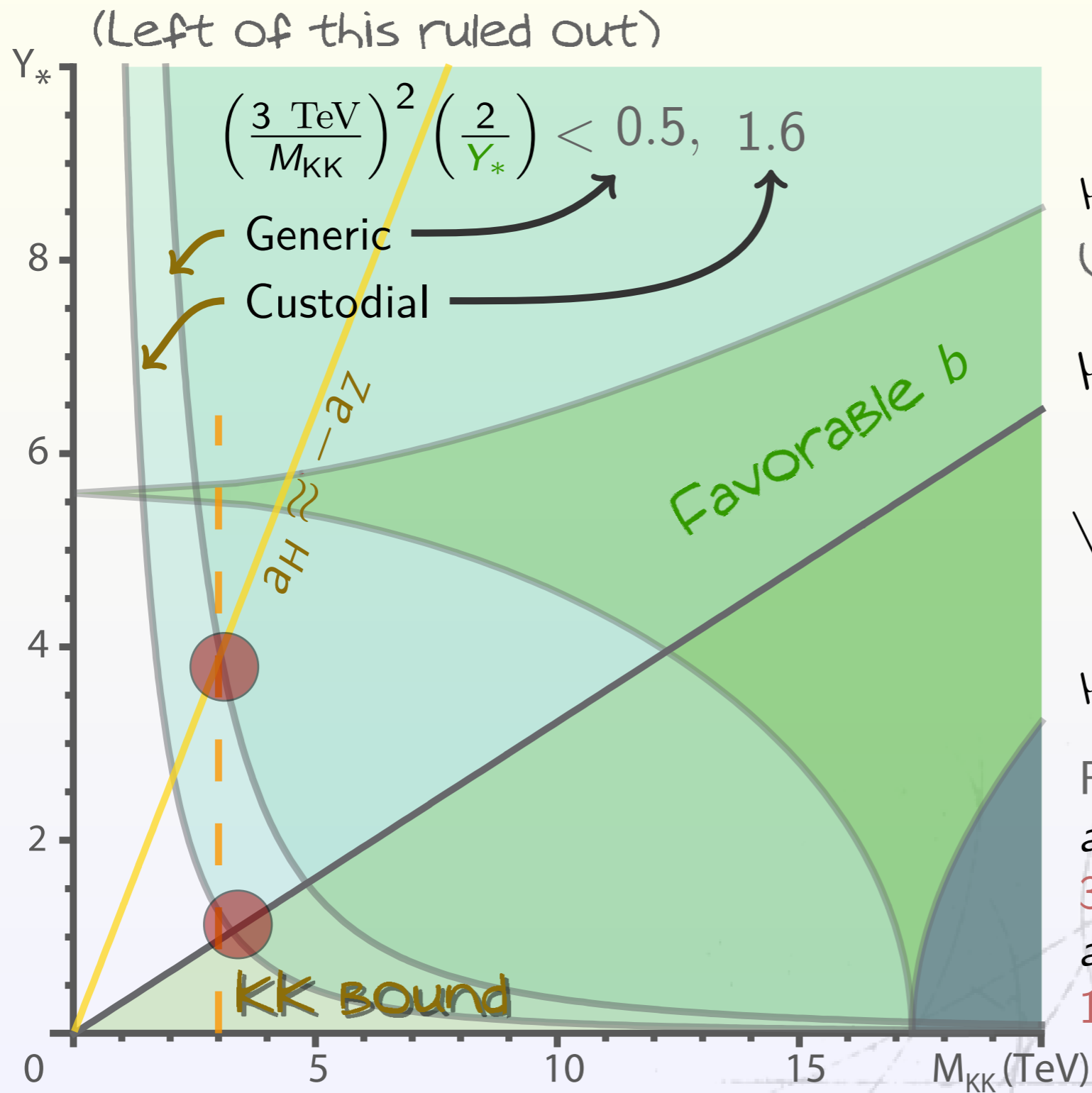
# Tree vs Loop



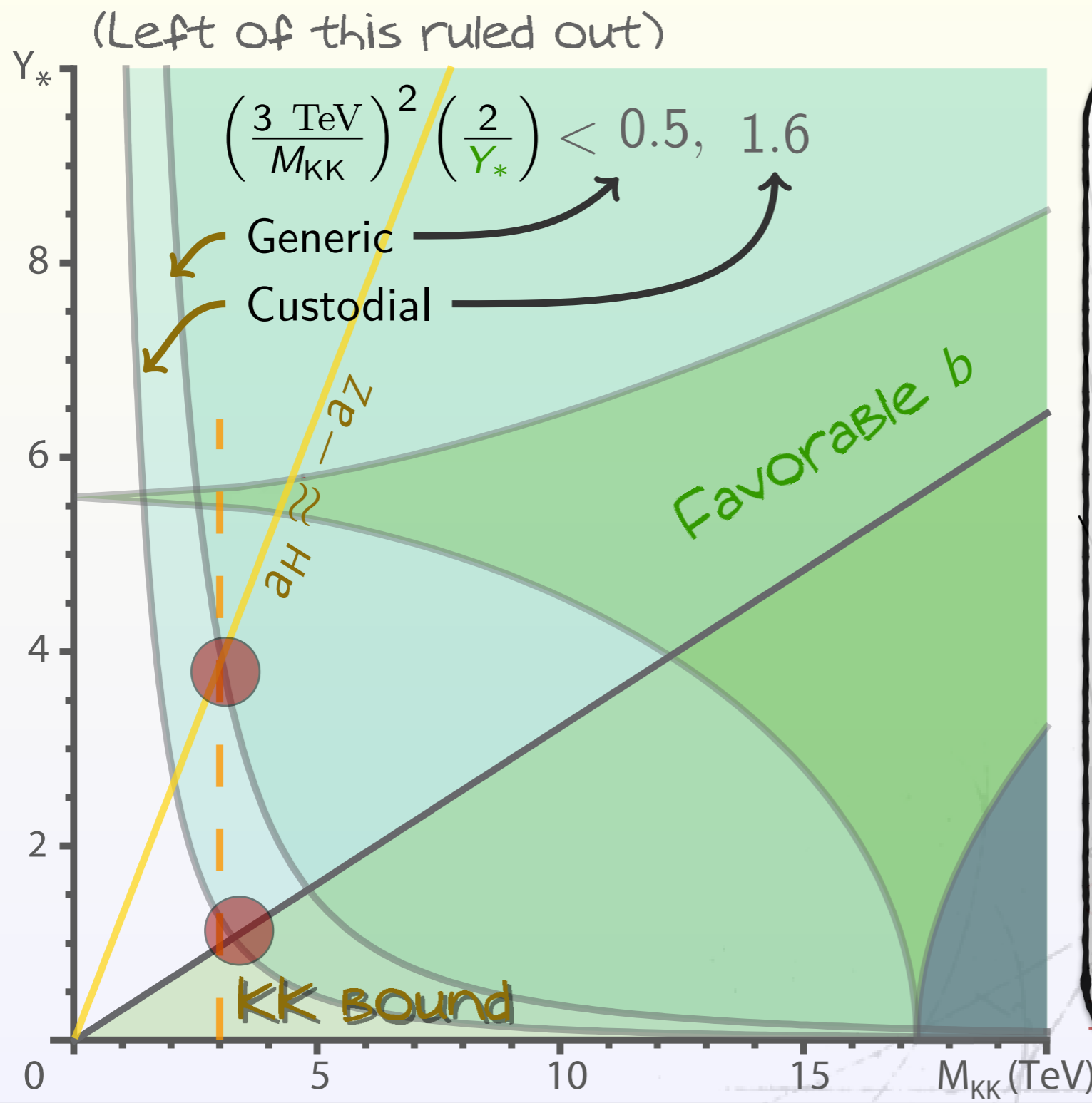
Complementary bounds on  $Y$   
 constrains the anarchic flavor picture

# subtlety: large flavor space

Three coefficients ( $a_H$ ,  $a_Z$ ,  $b$ ) with arbitrary relative signs  
 Defined  $aY_*^3 = \sum_{k,l} a_{kl} Y_{ik} Y_{kl}^\dagger Y_{lj}$  and  $bY_* = \sum_{k,l} (U_L)_{ik} b_{kl} Y_{kl} (U_R^\dagger)_{lj}$



$\mu \rightarrow e\gamma, b = -|b|_{1\sigma}$   
 (ABOVE this ruled out)  
 $\mu \rightarrow e\gamma, \text{ average}$   
 $|aY_*^2 + b| \left(\frac{3\text{TeV}}{M_{\text{KK}}}\right)^2 < .015$   
 $\mu \rightarrow e\gamma, b = +|b|_{1\sigma}$   
 For  $M_{\text{KK}} = 3 \text{ TeV}, b = 0$   
 $a = .001$  and generic  
 $3.7 \lesssim Y_* \lesssim 4$   
 $a = .016$  and custodial  
 $1 \lesssim Y_* \lesssim 1$



complimentary  
**tree vs loop**  
 bounds

can really test  
**anarchic flavor**  
*paradigm*

Not "just another model"  
 For  $M_{\text{KK}} = 3 \text{ TeV}, b = 0$   
 Warped Extra Dimensions  
 Composite/Little/etc. Higgs  
 ... even SUSY versions  
 $a = .001$  and generic  
 $a = .016$  and custodial  
 $1 \lesssim Y_* \lesssim 10$